

FROM ALGORITHMS TO ASTROPHYSICS: MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

NIKOLAOS STERGIOULAS

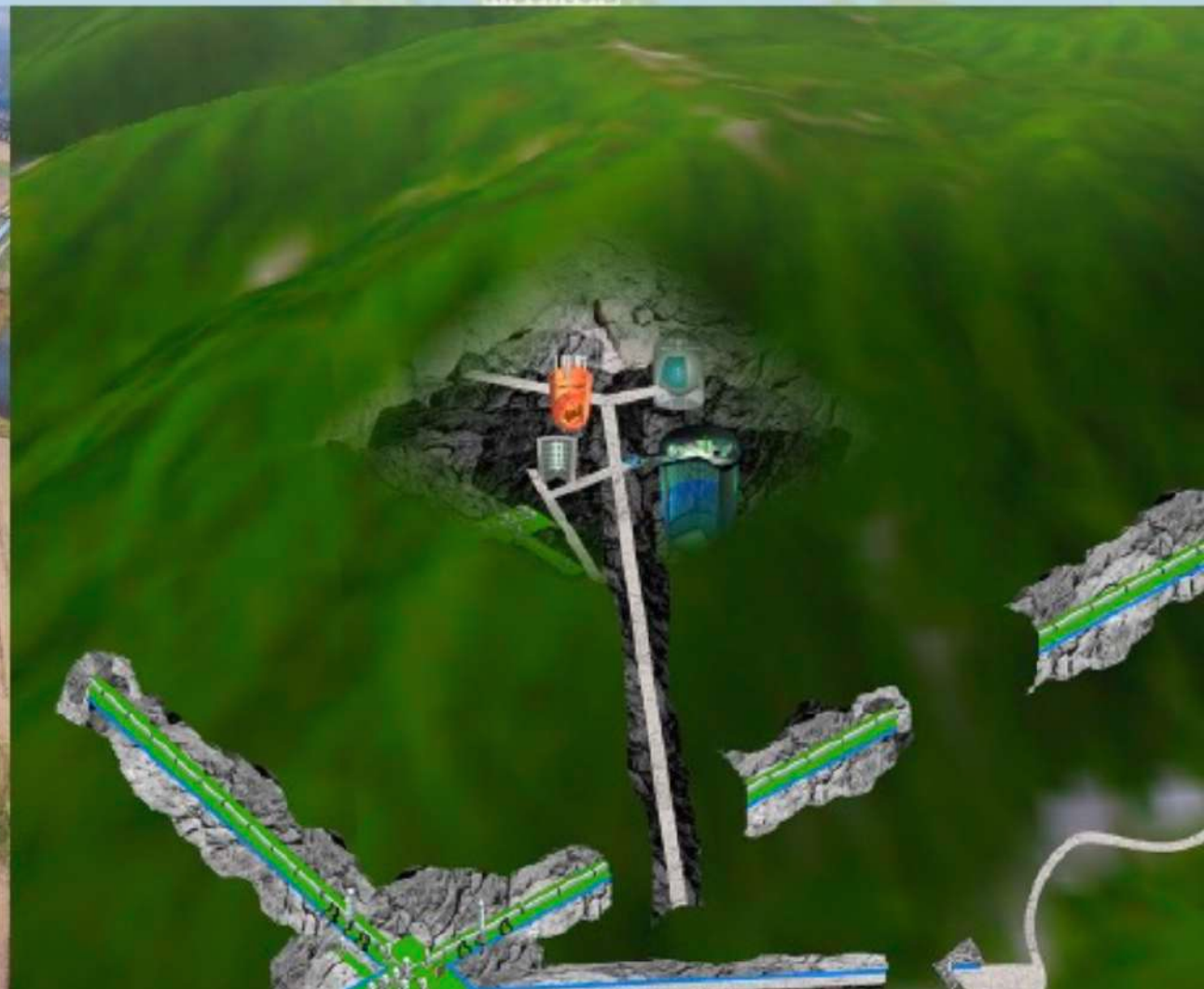
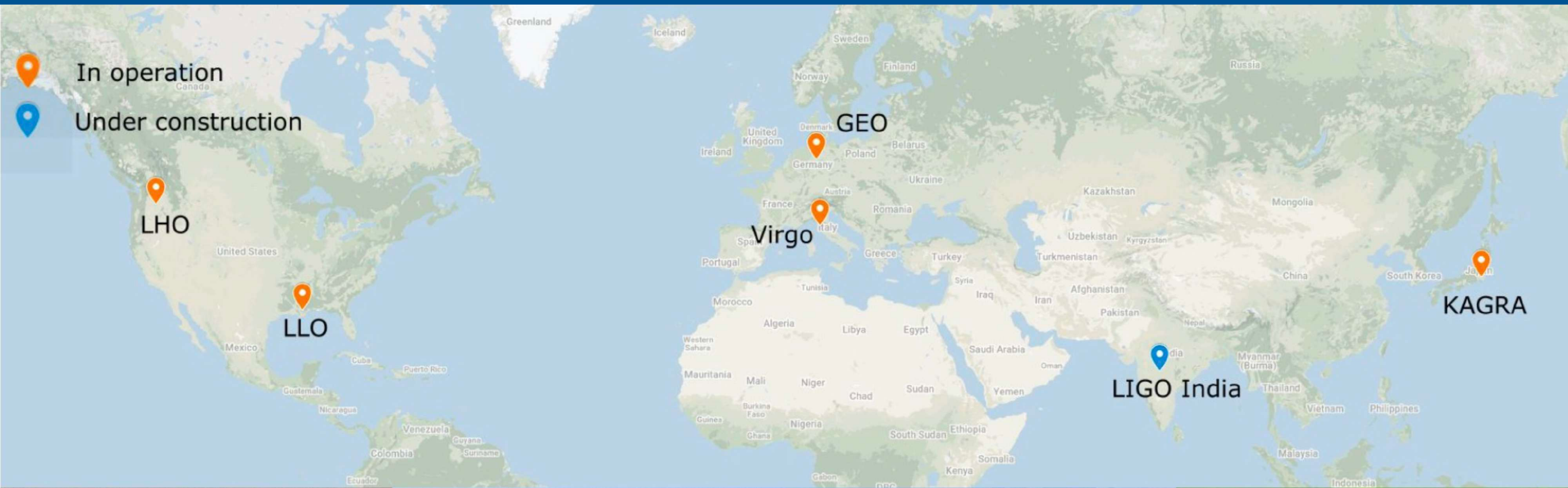
DEPARTMENT OF PHYSICS

ARISTOTLE UNIVERSITY OF THESSALONIKI

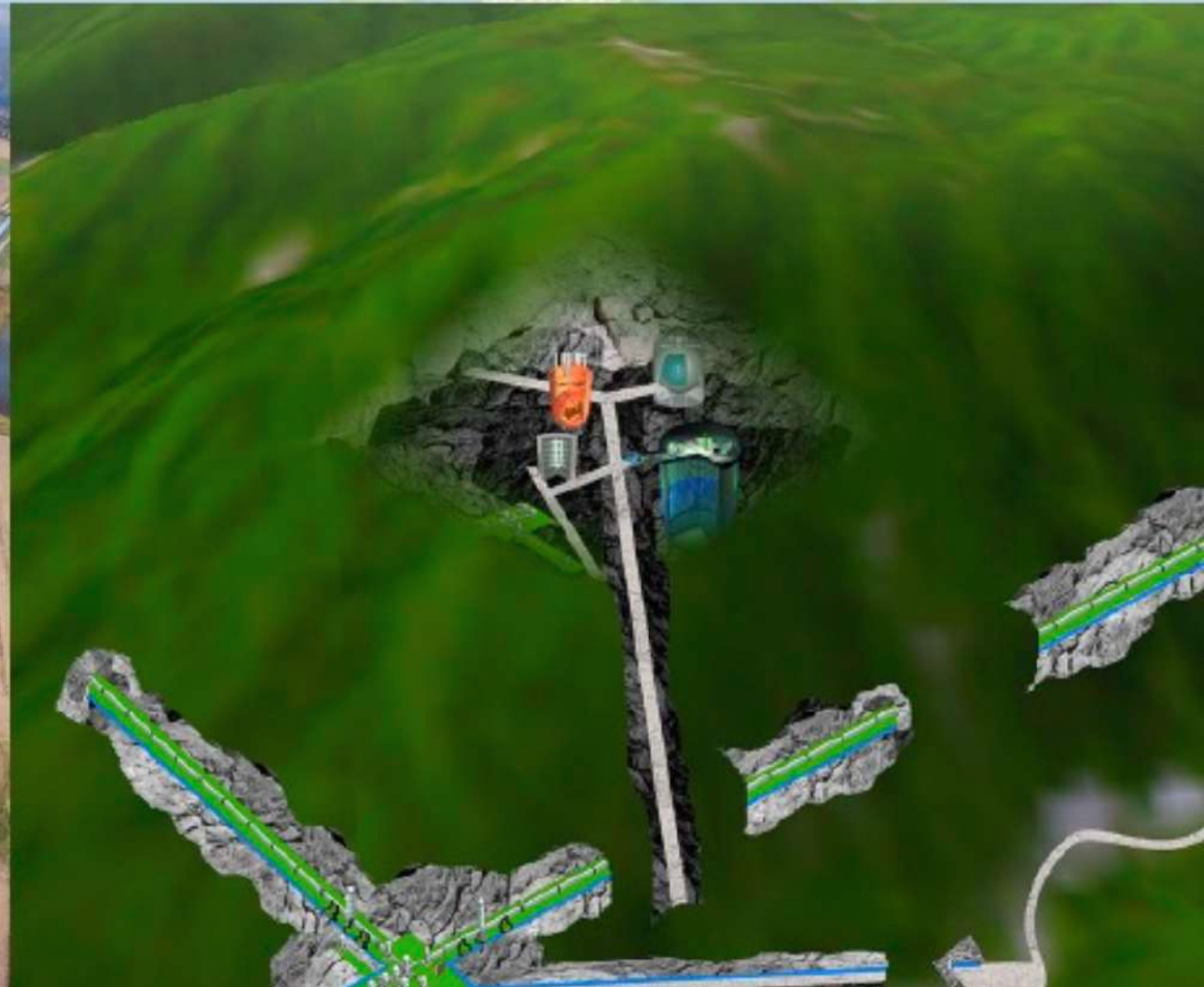


PART A. BINARY BLACK HOLE MERGERS

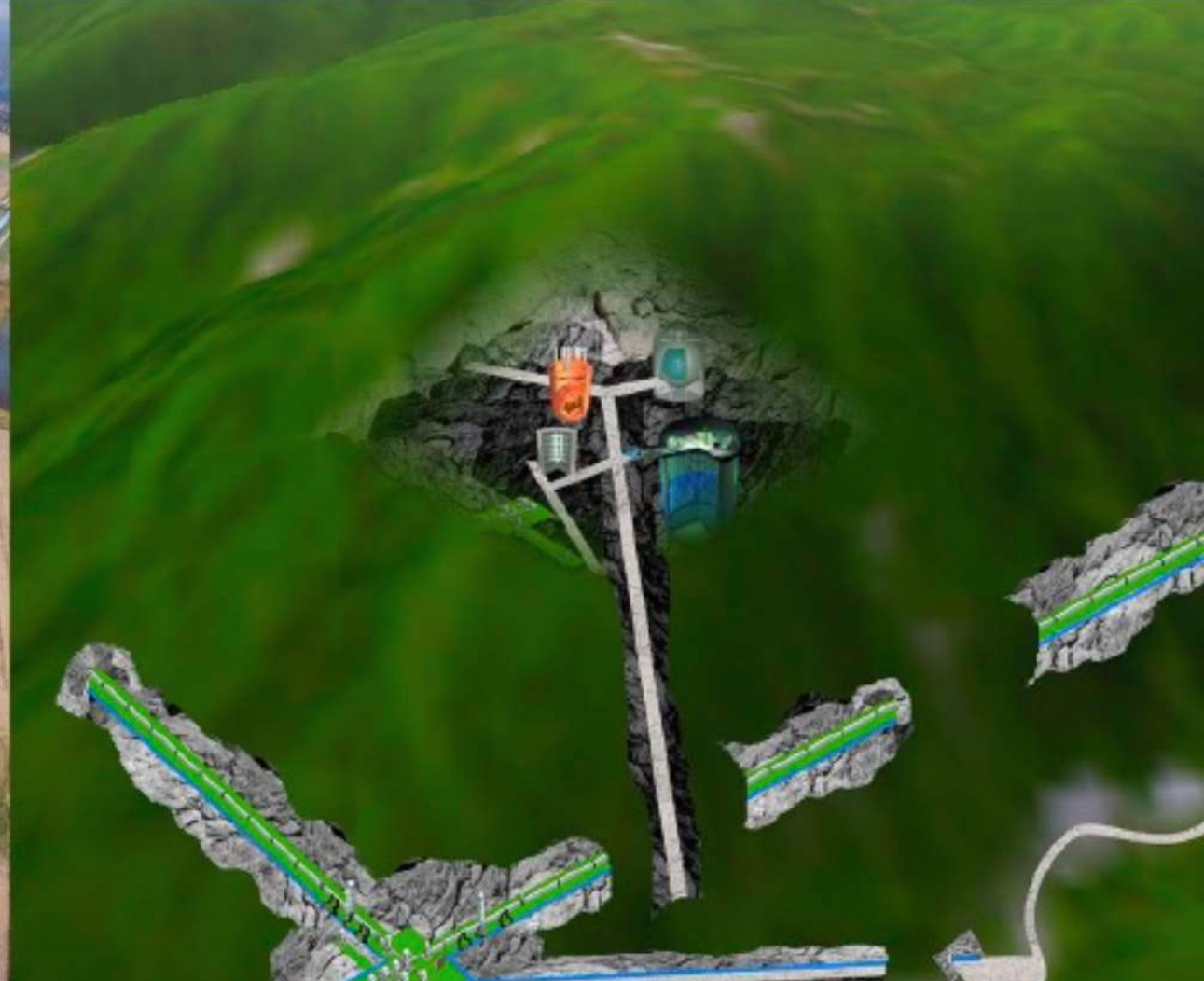
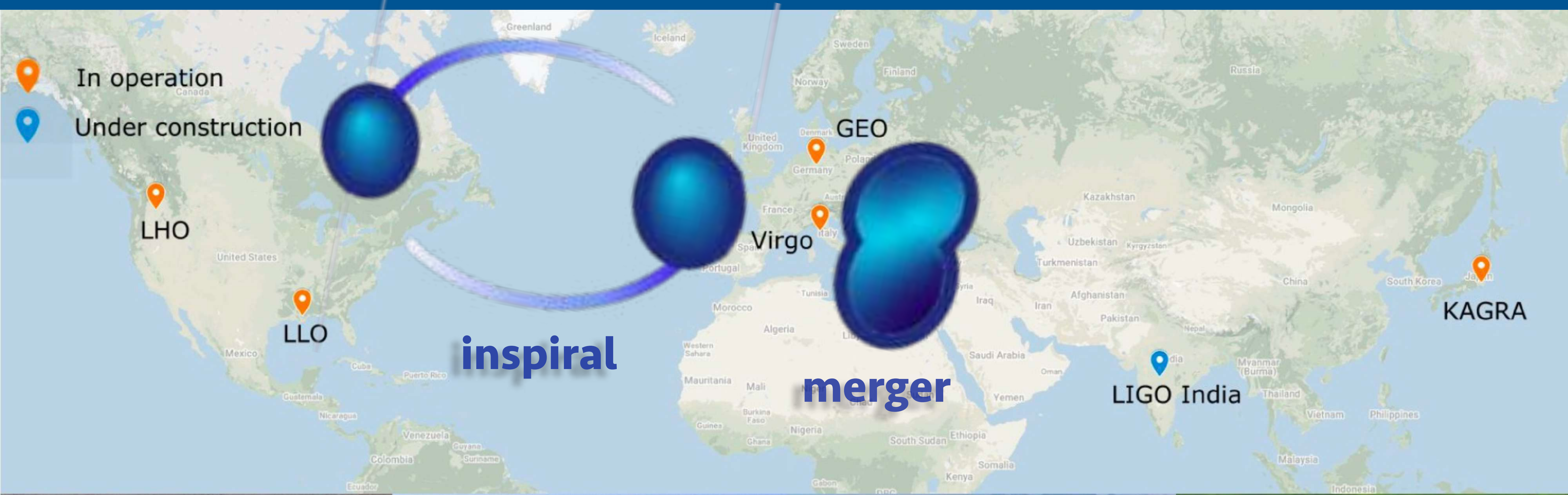
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



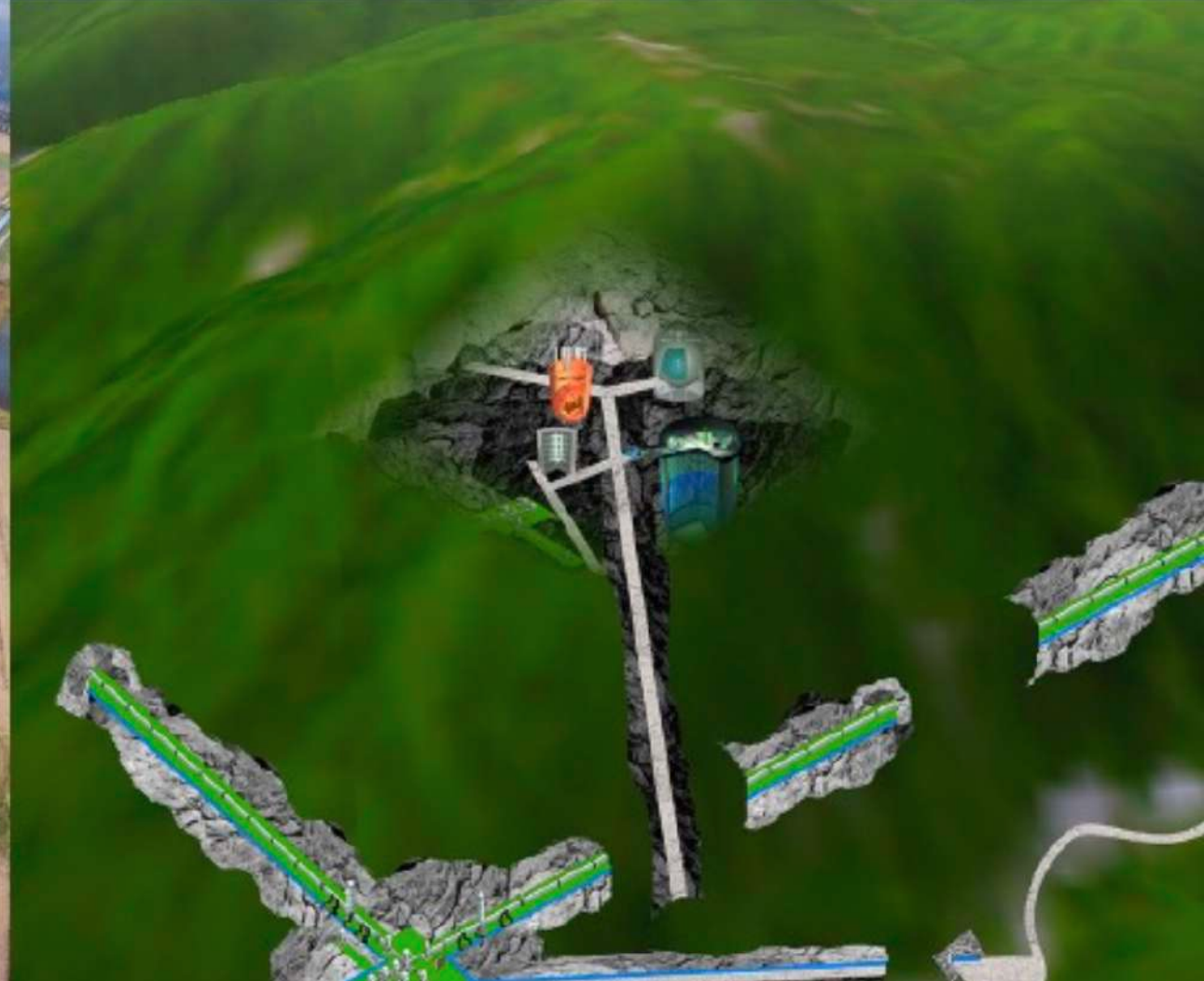
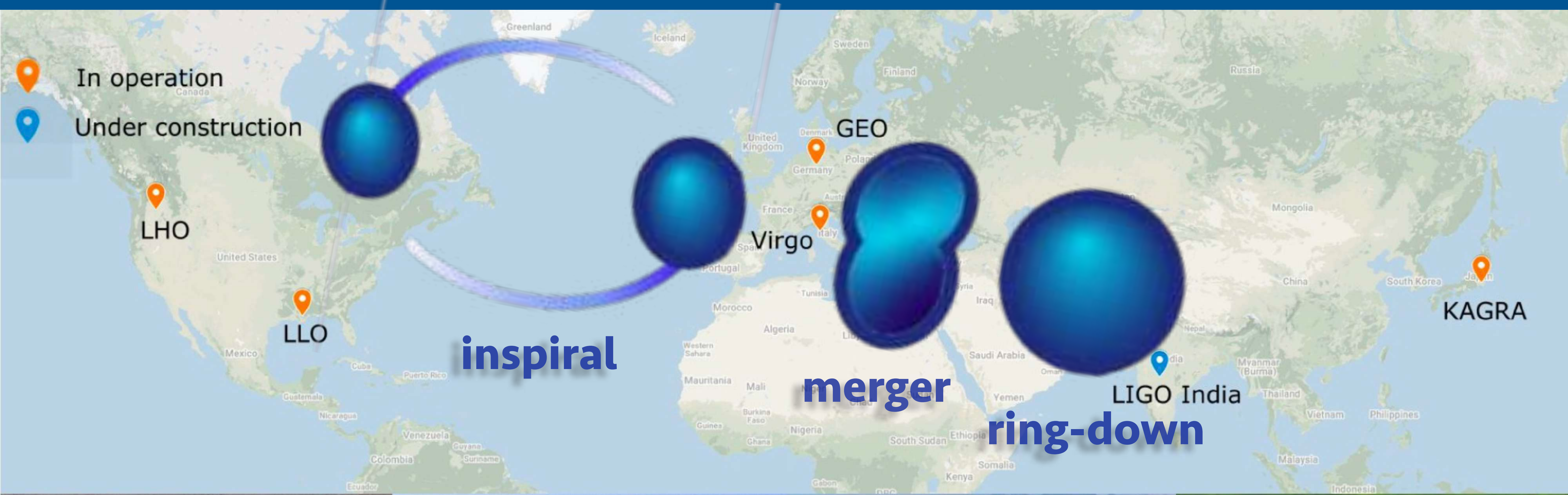
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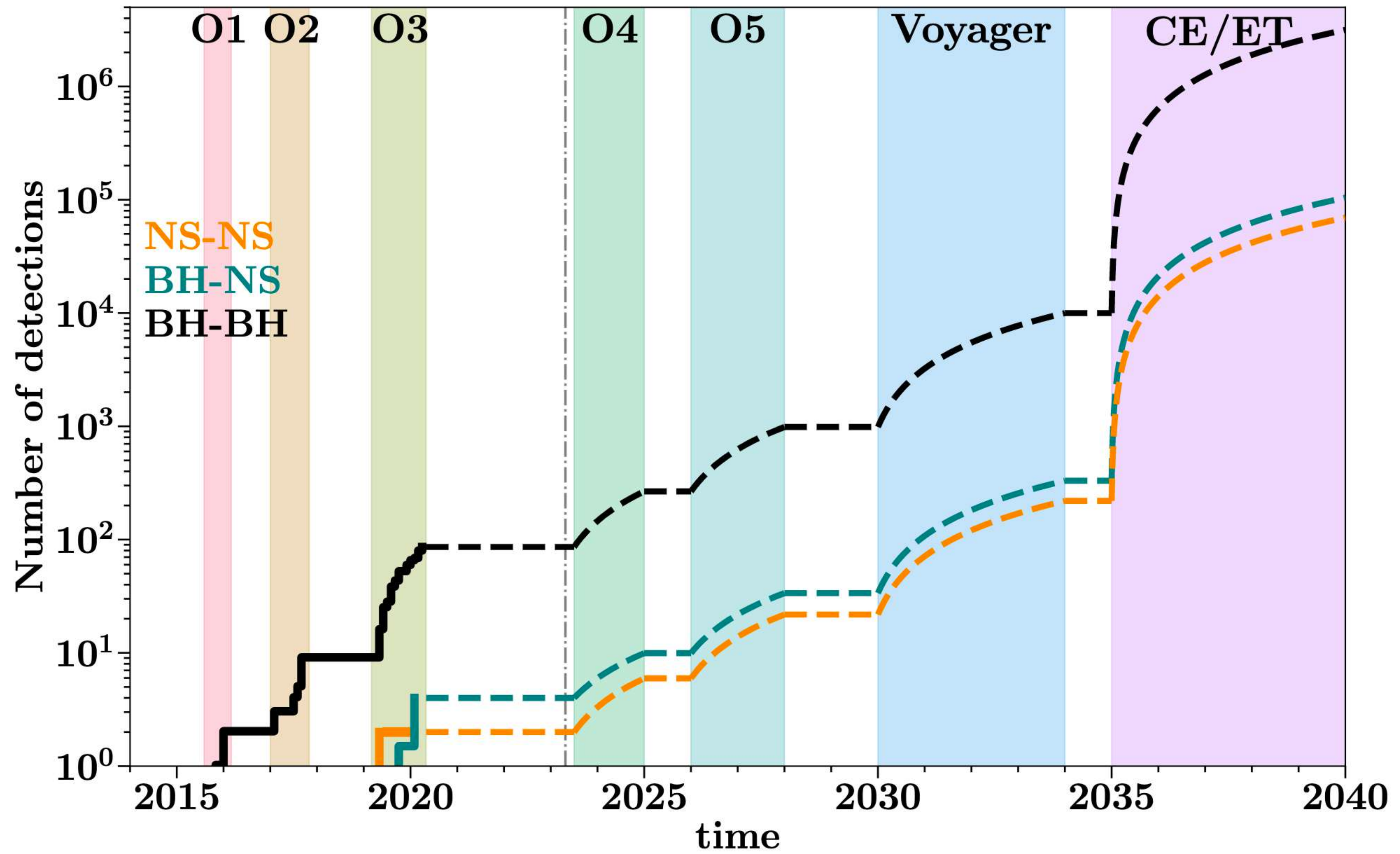
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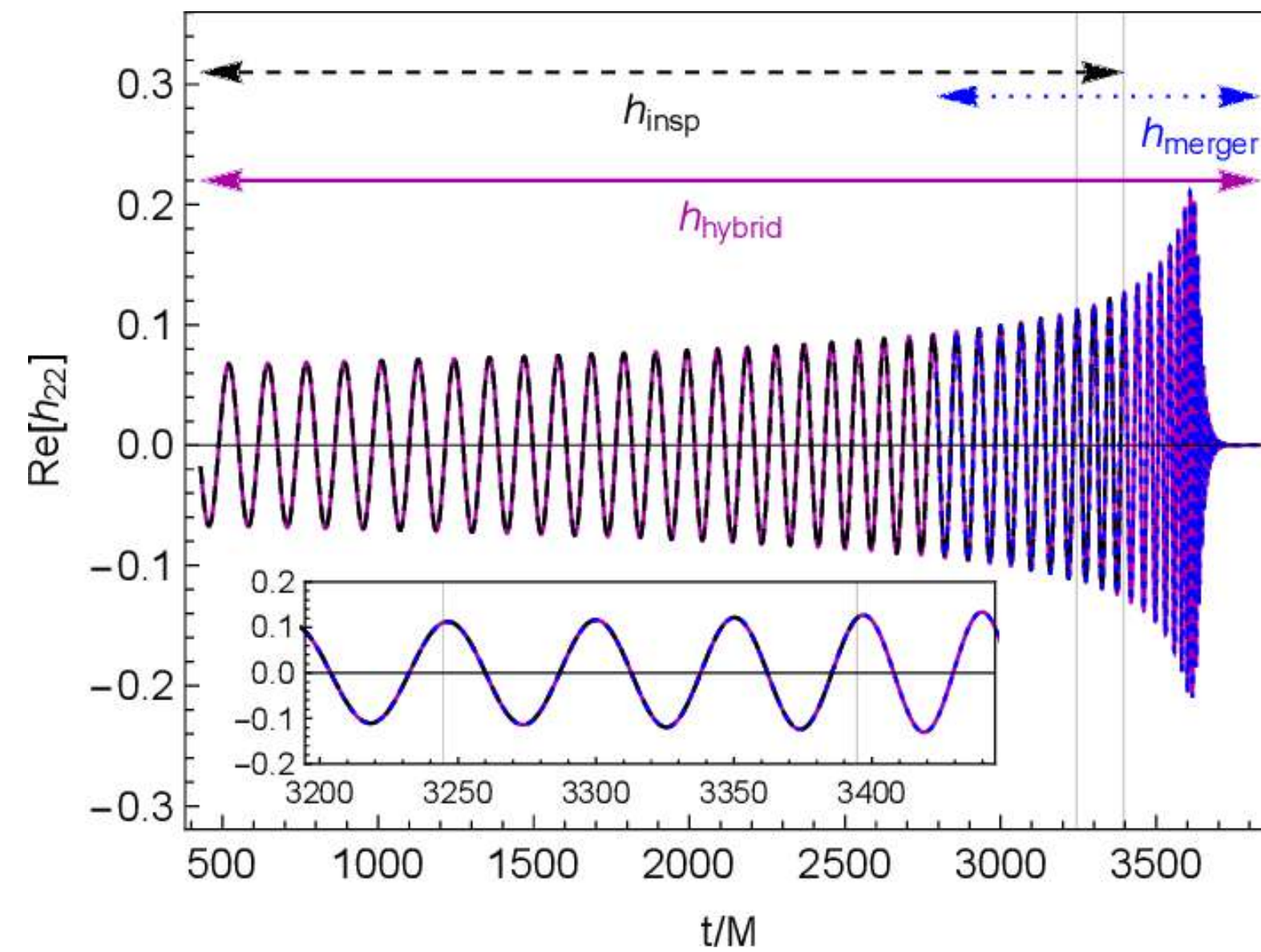


EXPECTED NUMBER OF DETECTIONS

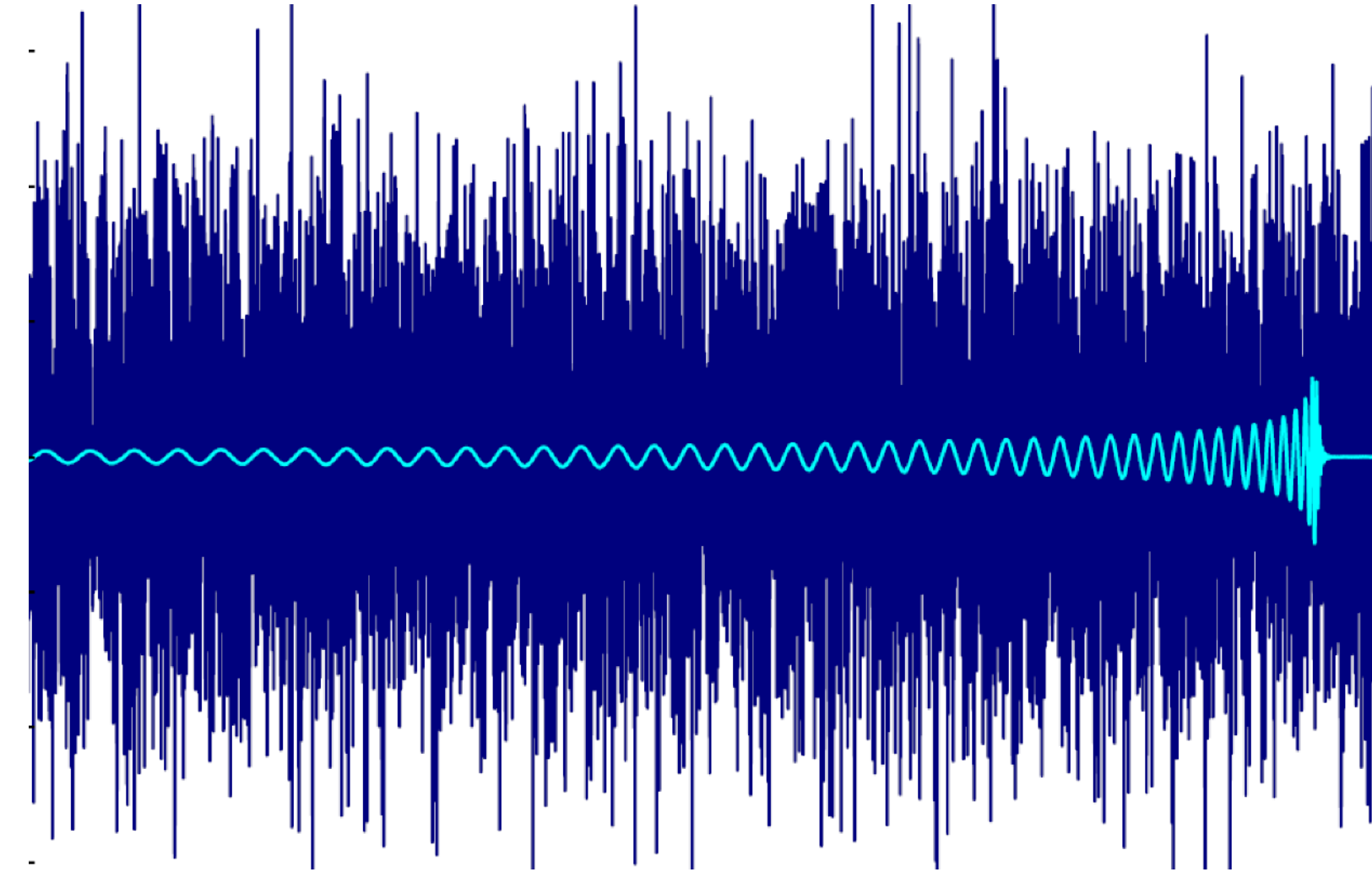


MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

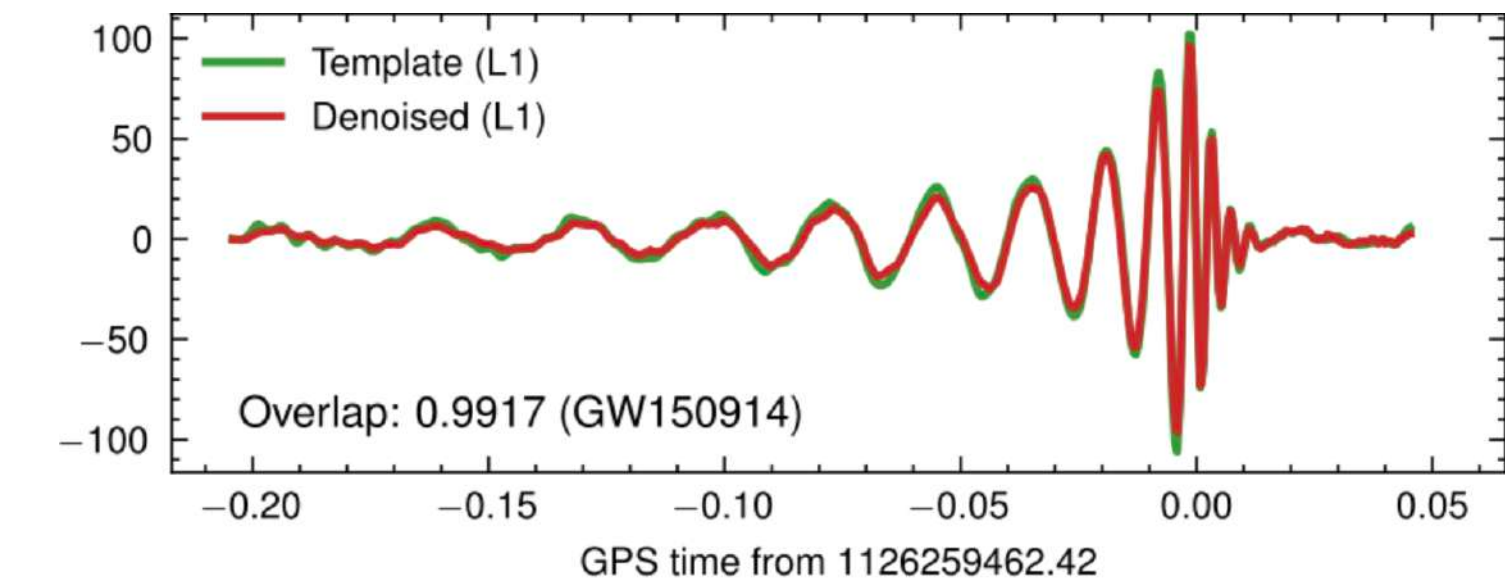
Waveform Modeling



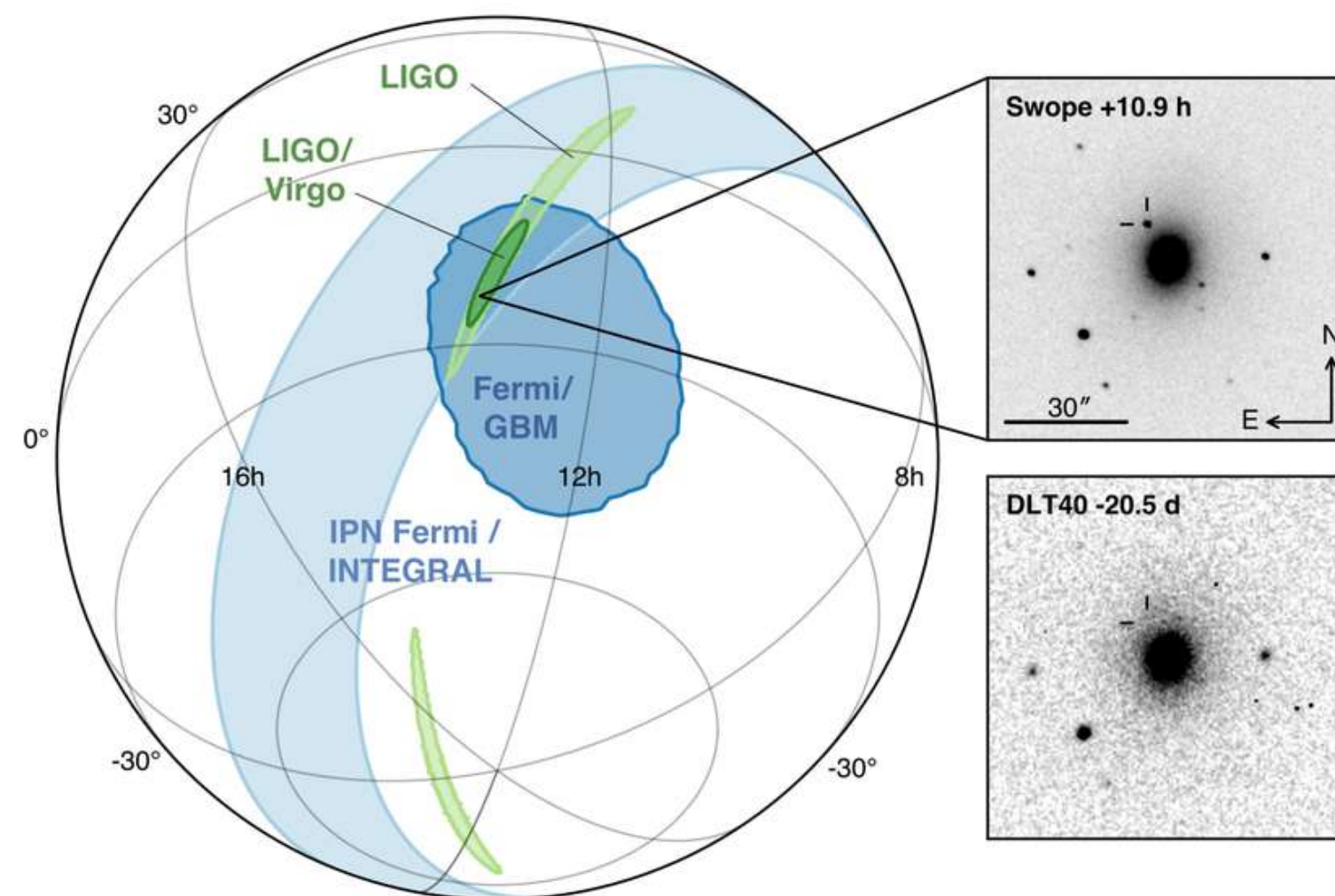
Detection



Denoising

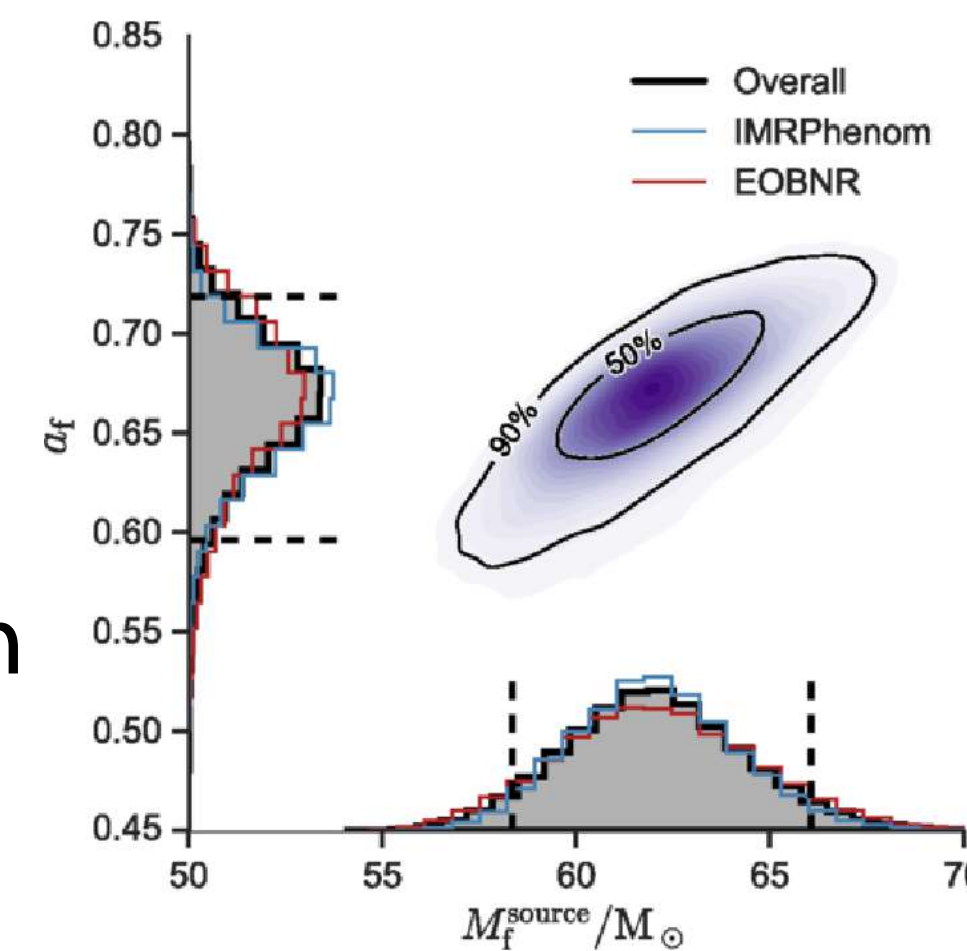


Glitch Classification

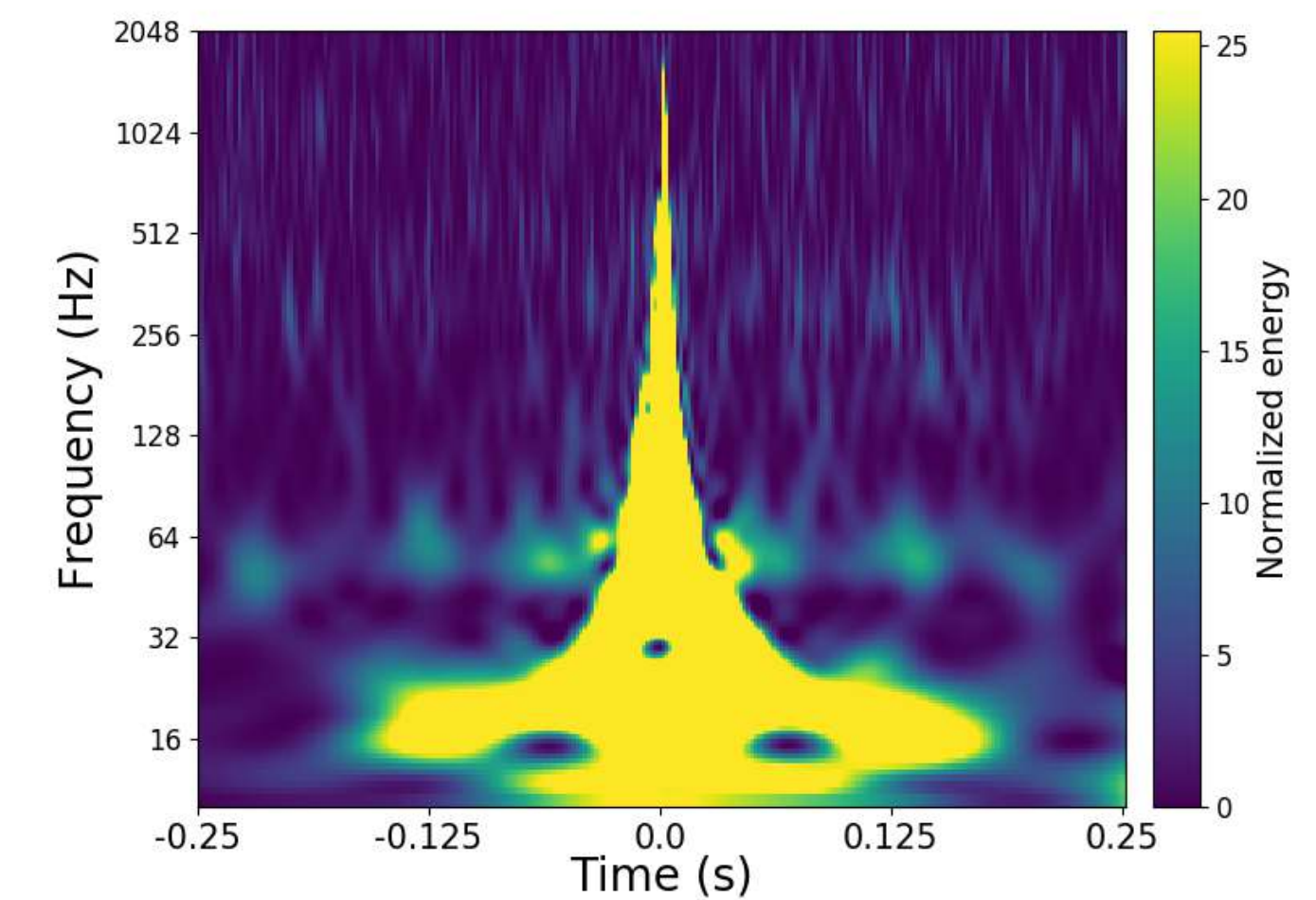


Parameter Estimation

Sky Localization

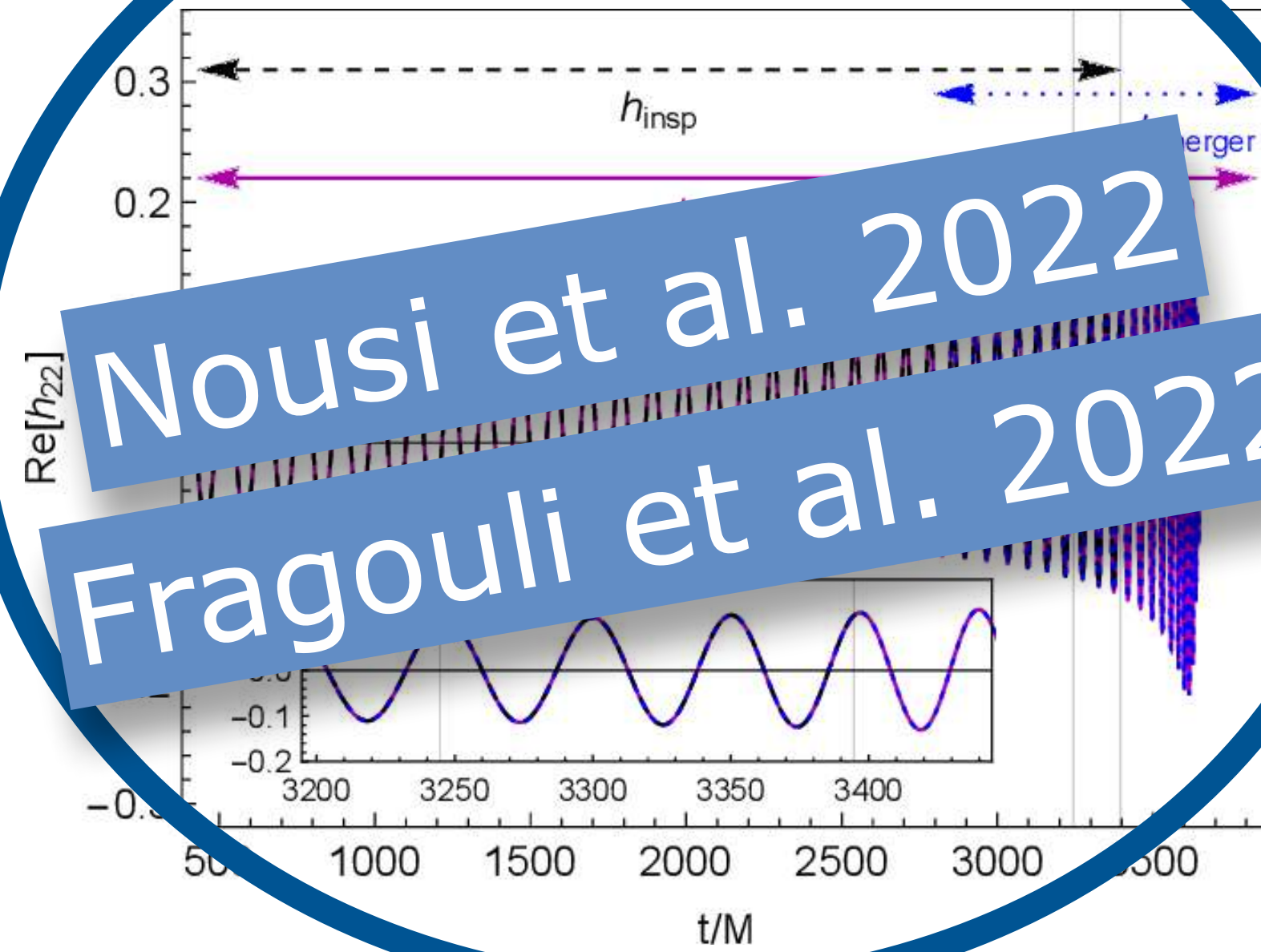


Livingston - O2a

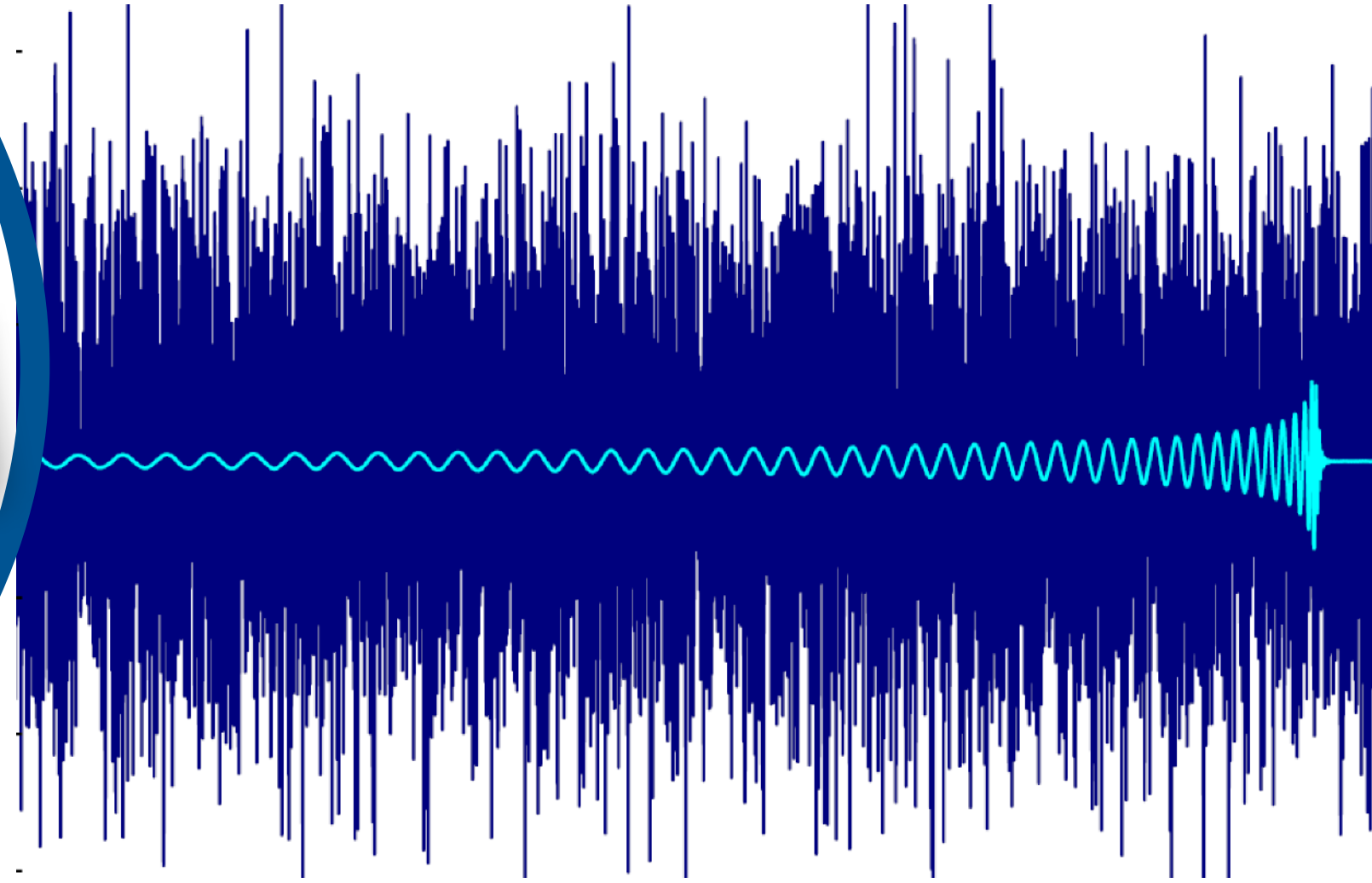


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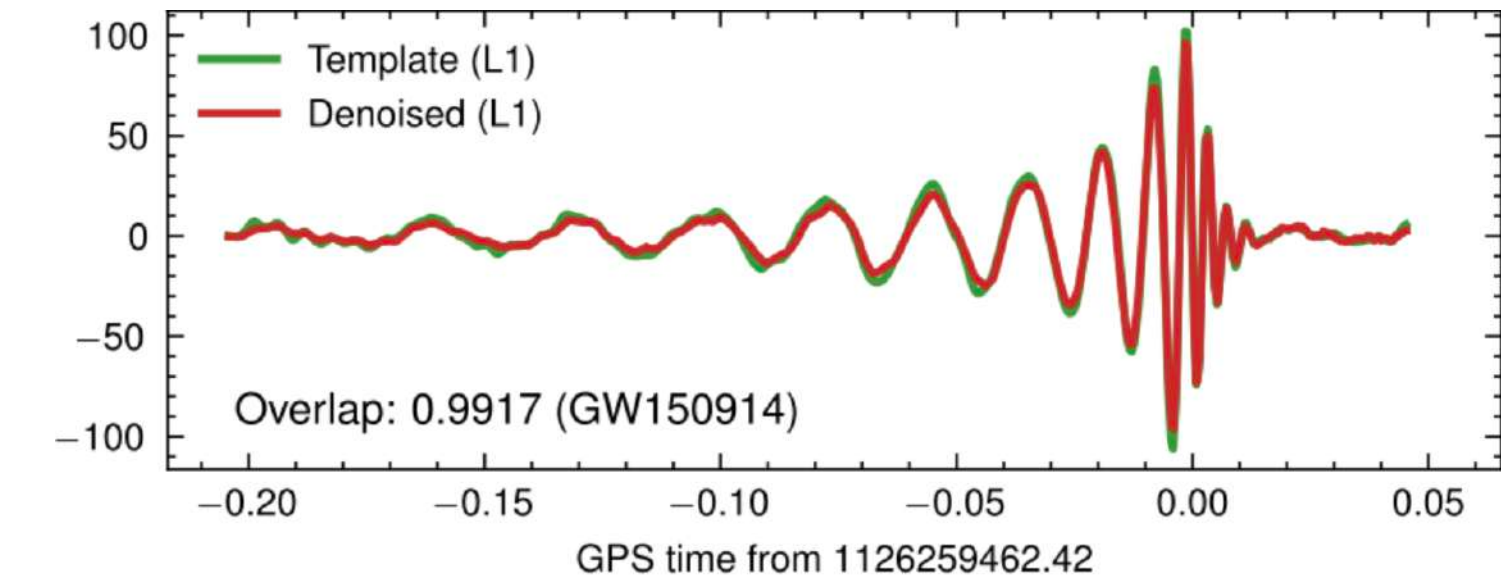
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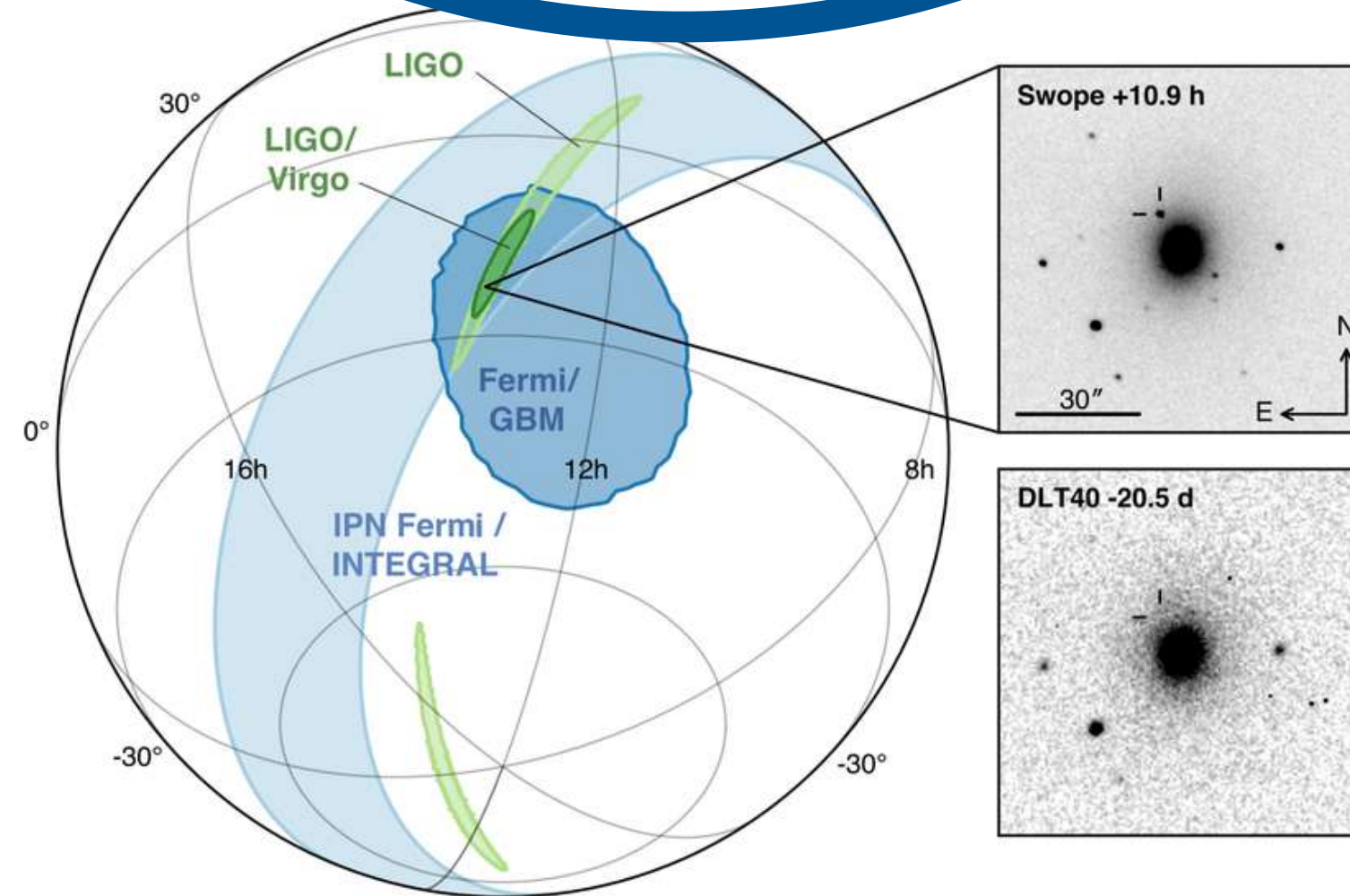
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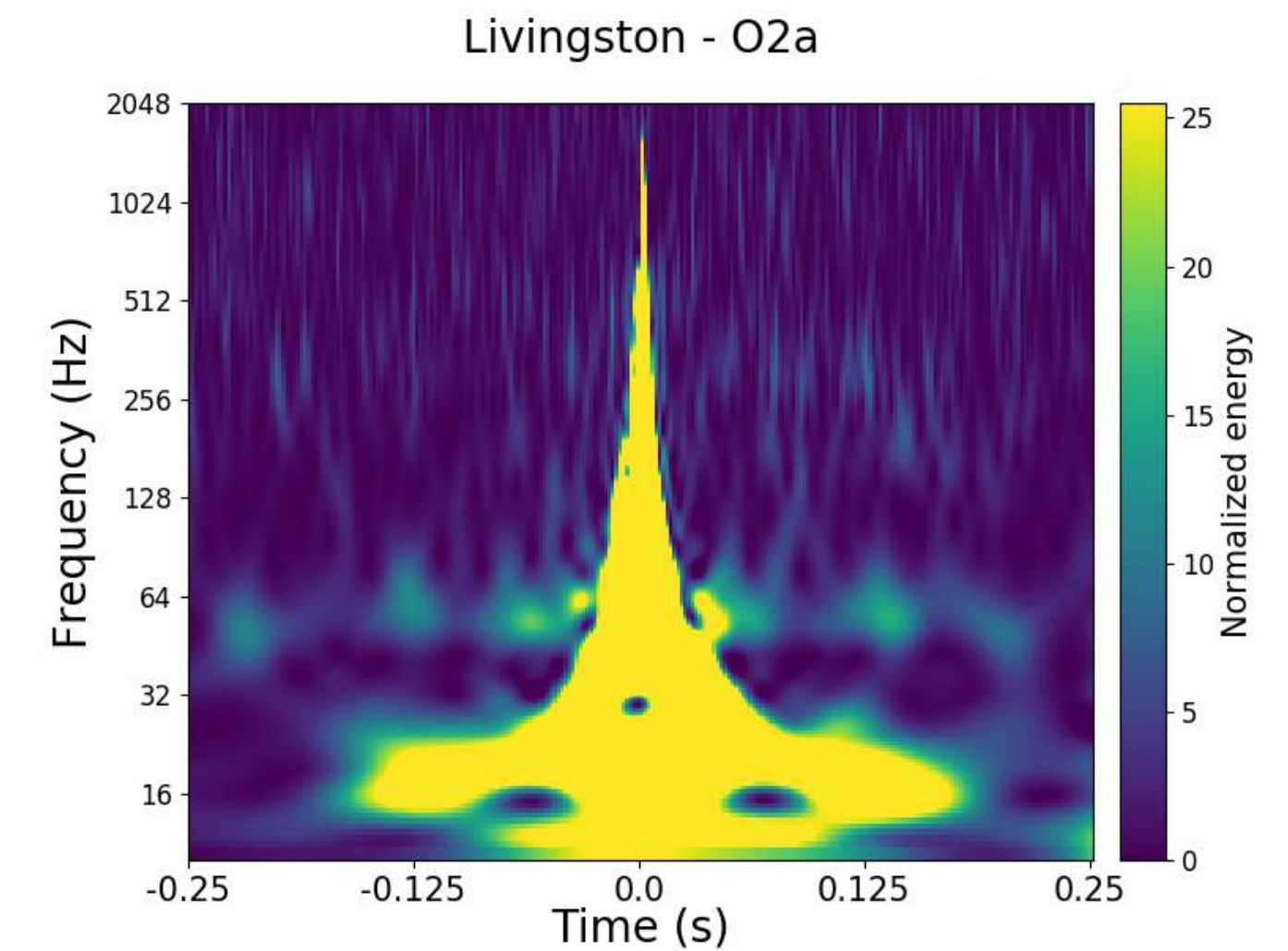
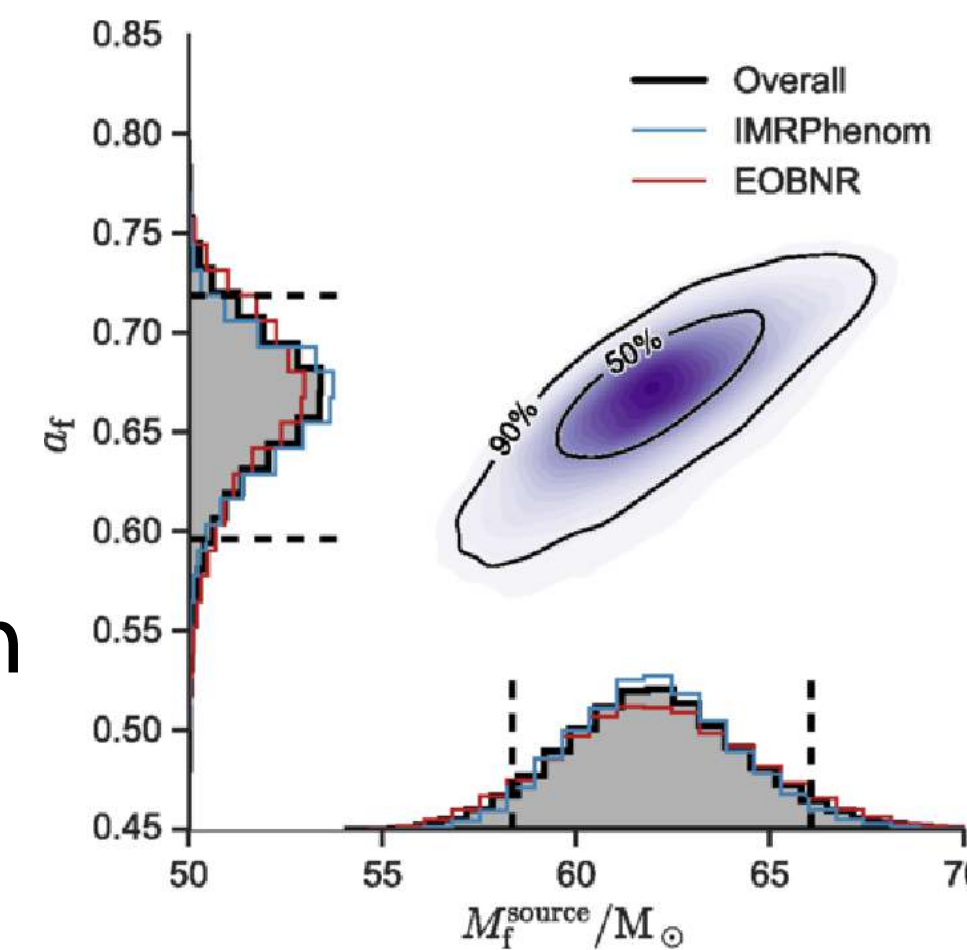


Glitch Classification



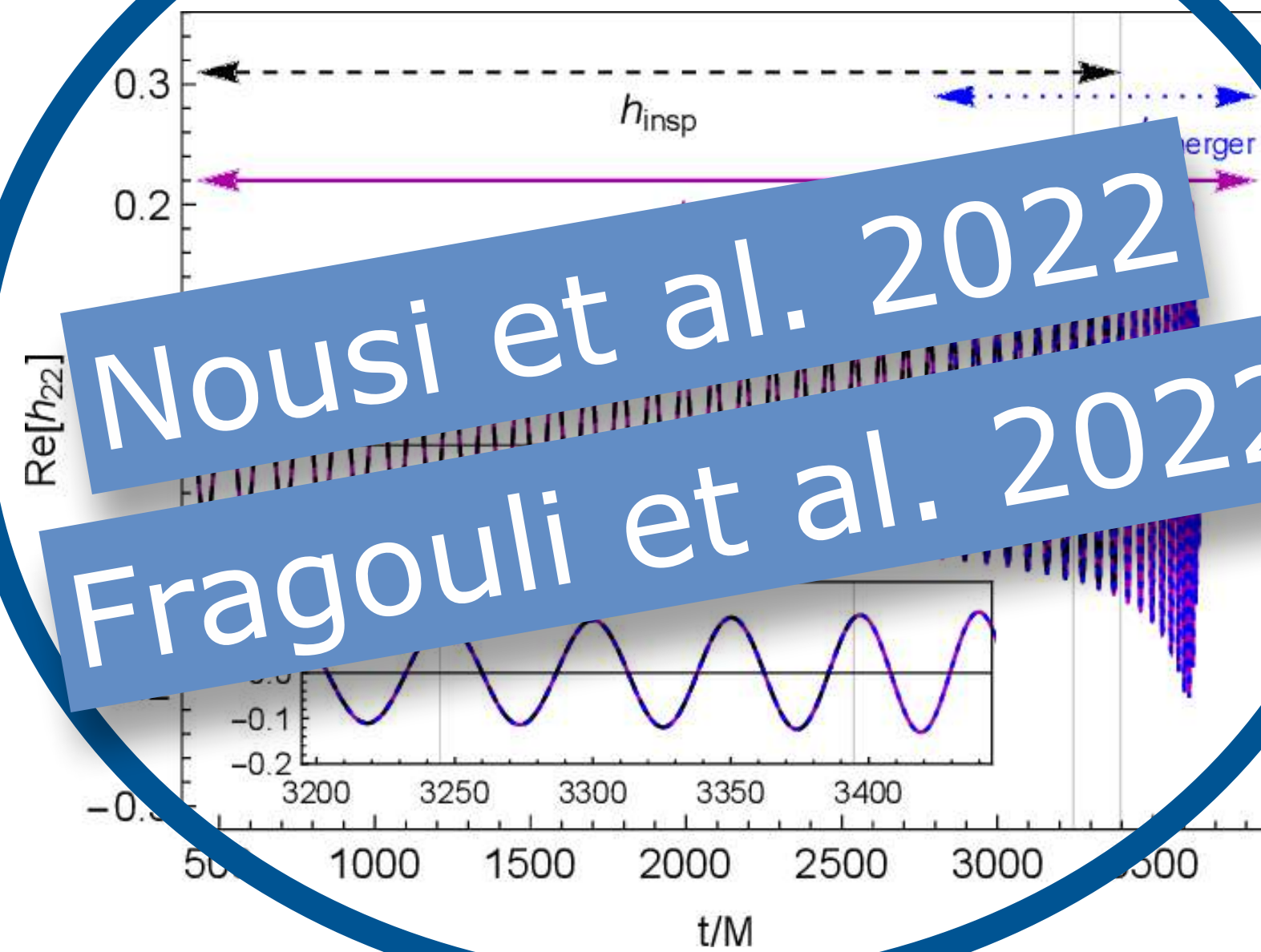
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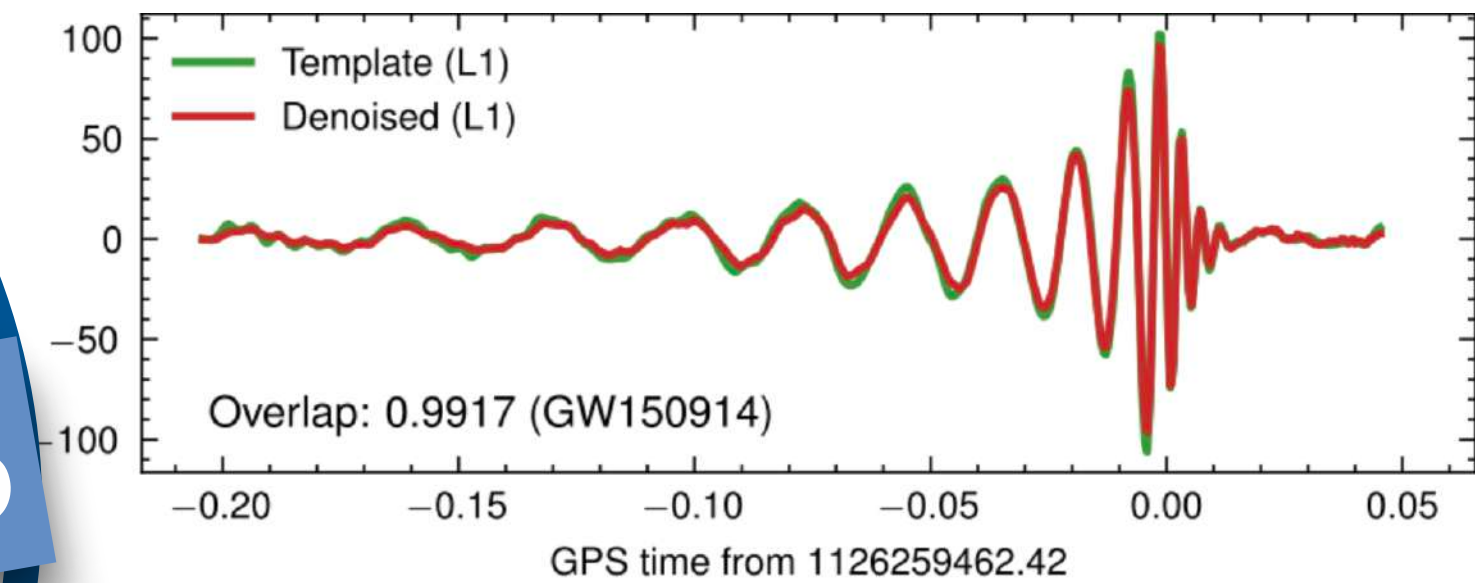
Nousi et al. 2022

Fragouli et al. 2022

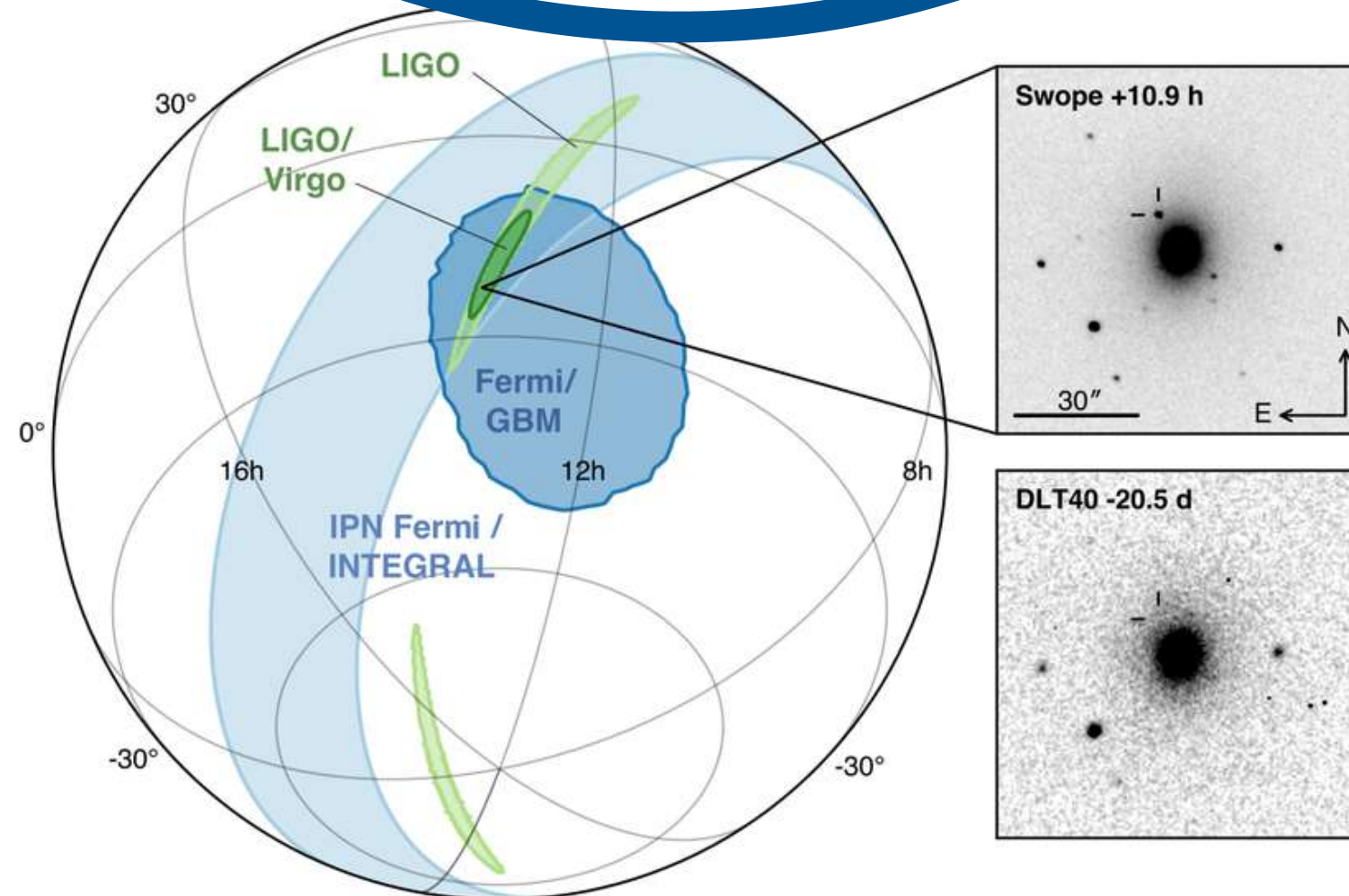
Detection



Denoising

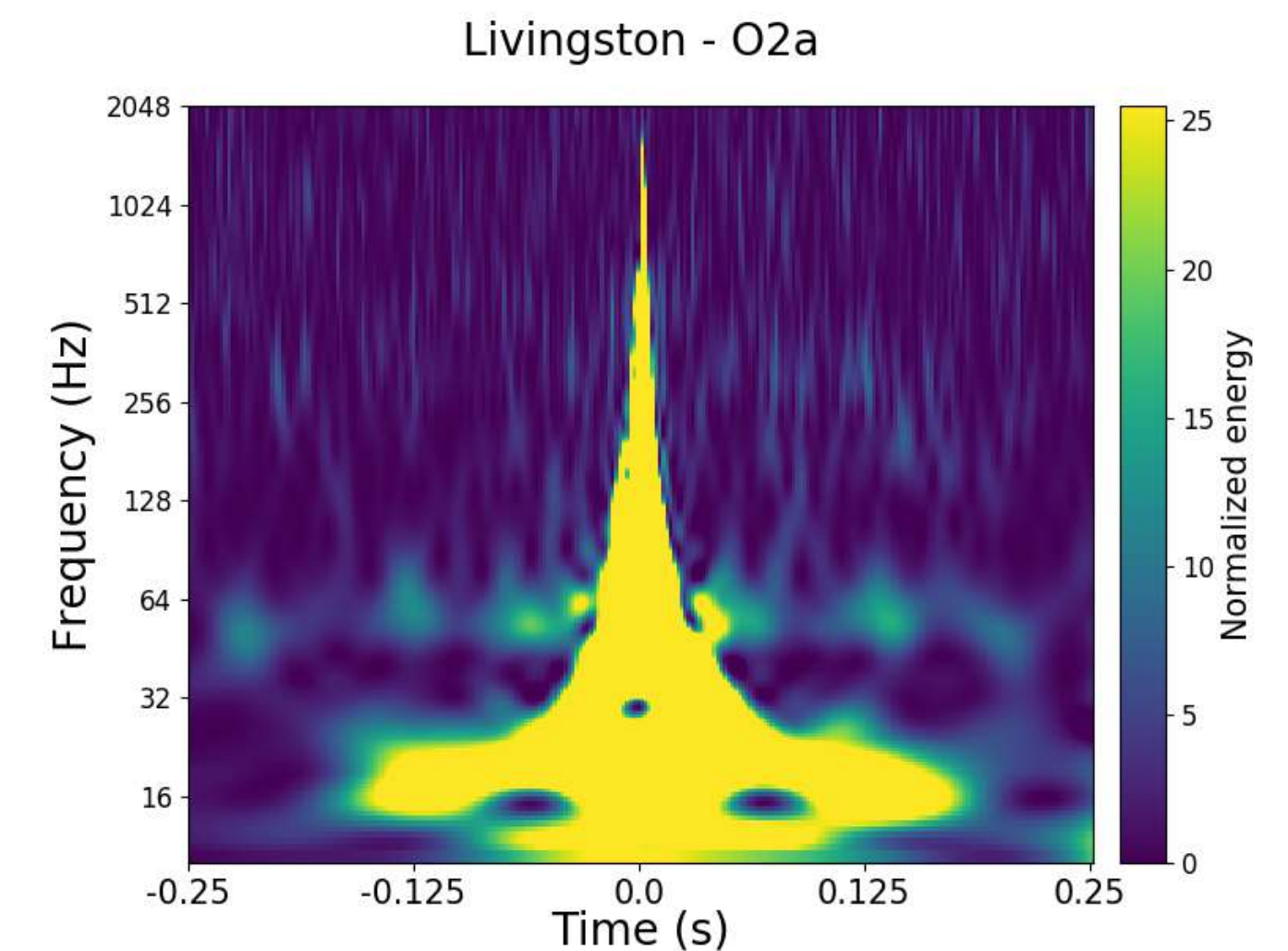
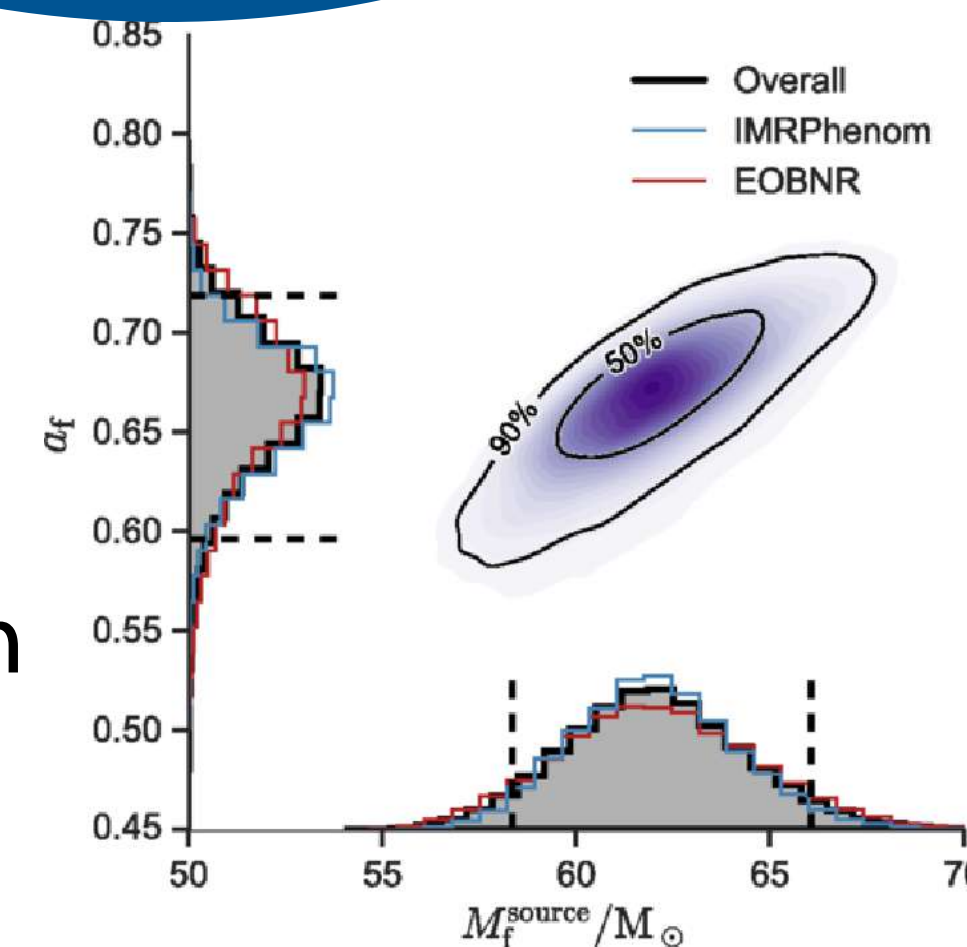


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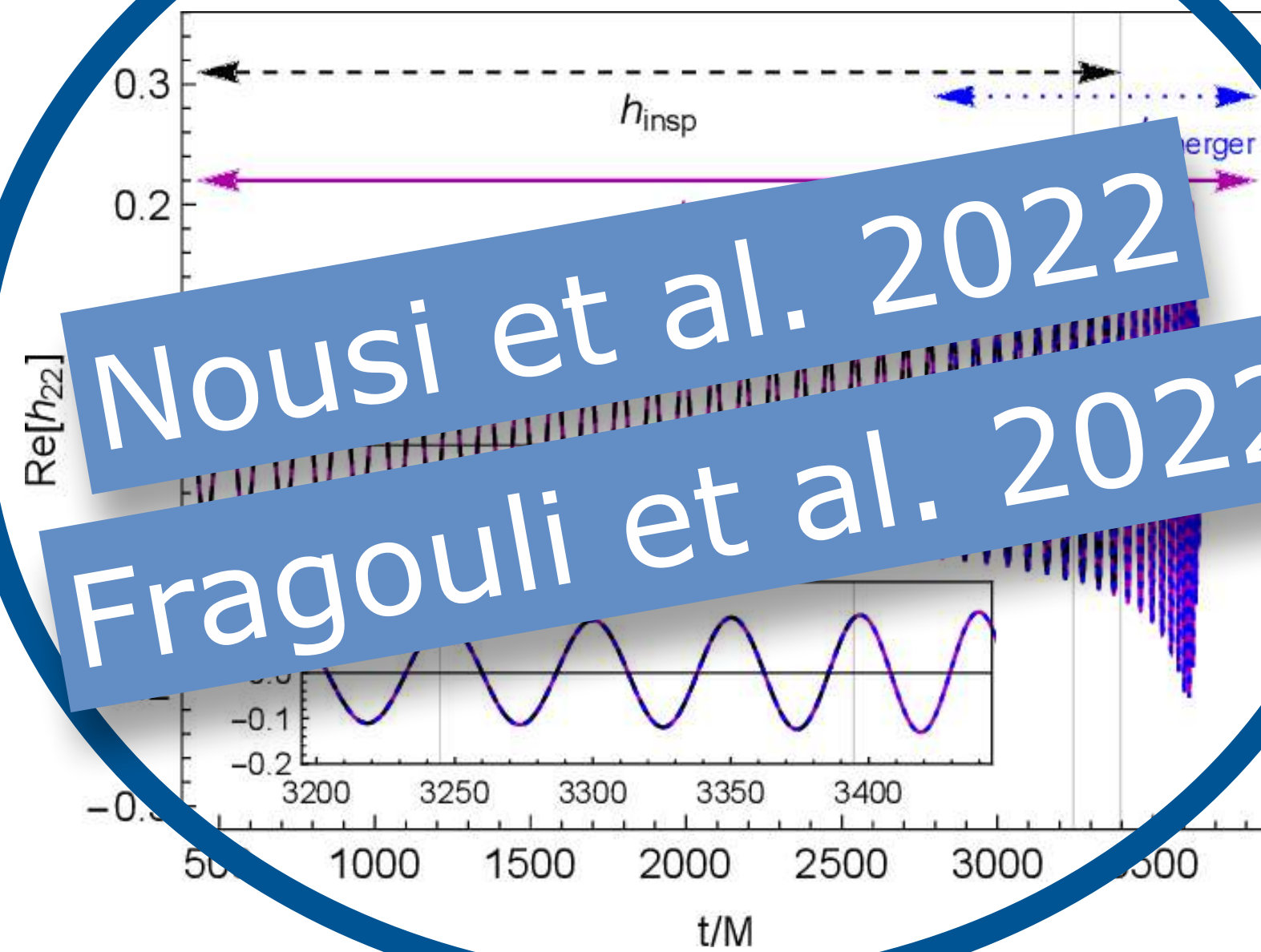
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Waveform Modeling



Nousi et al. 2022

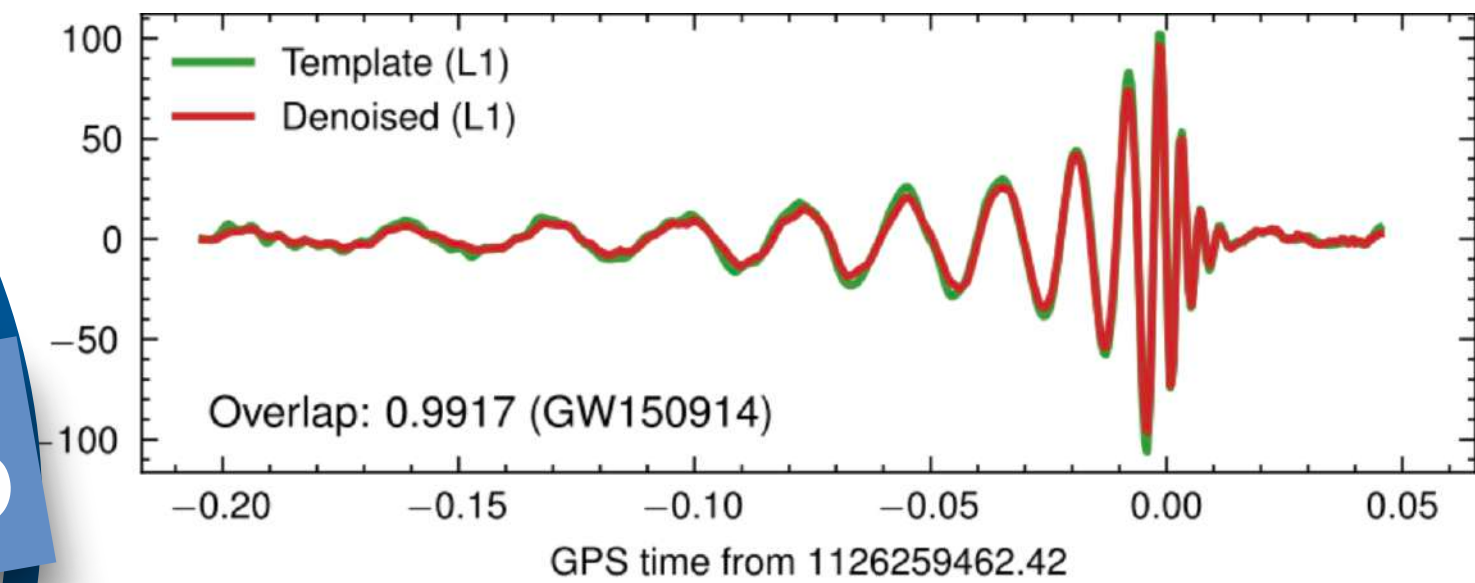
Fragouli et al. 2022

Detection

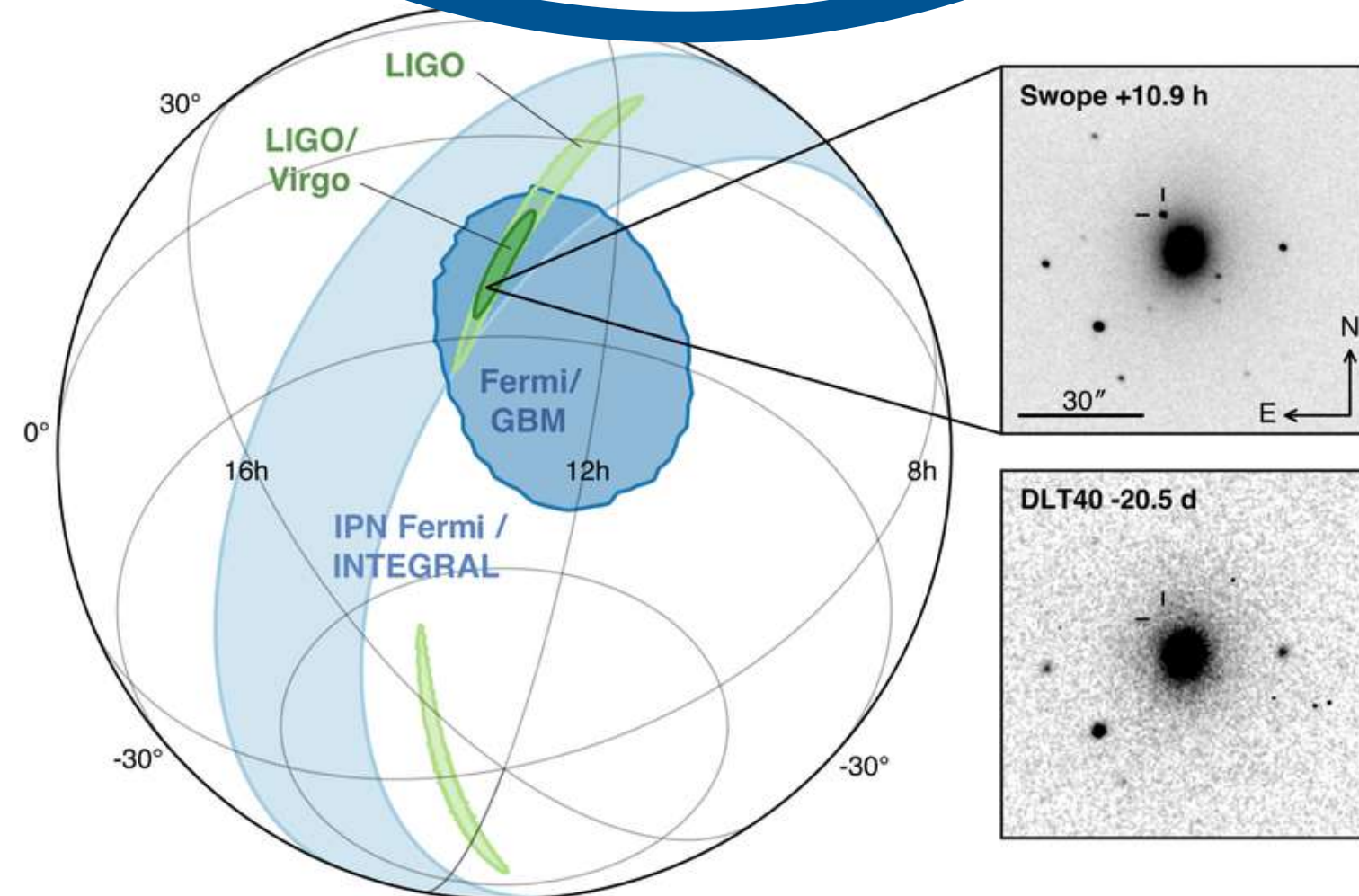


See also A. Koloniari and O. Zelenka talks

Denoising

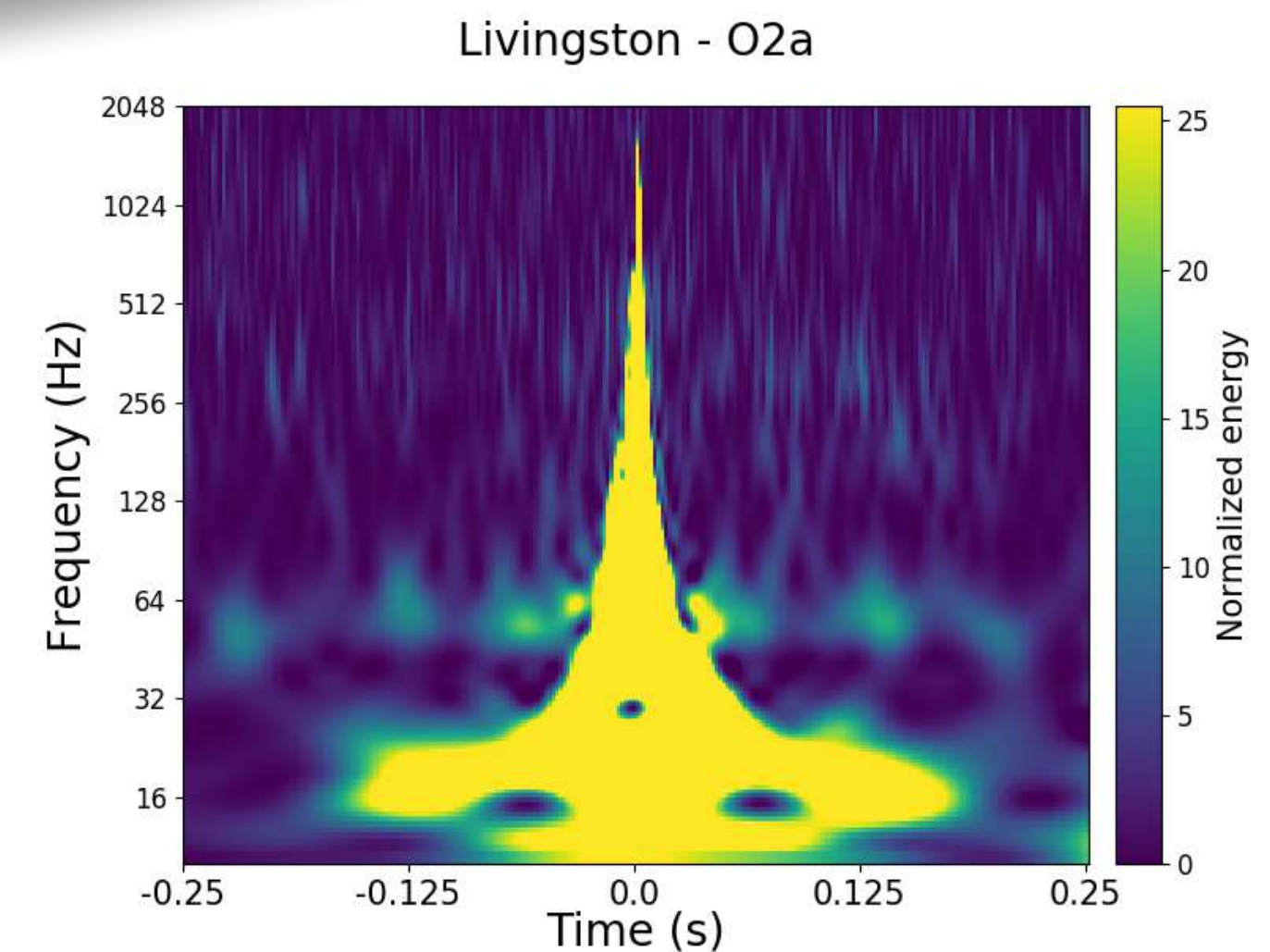
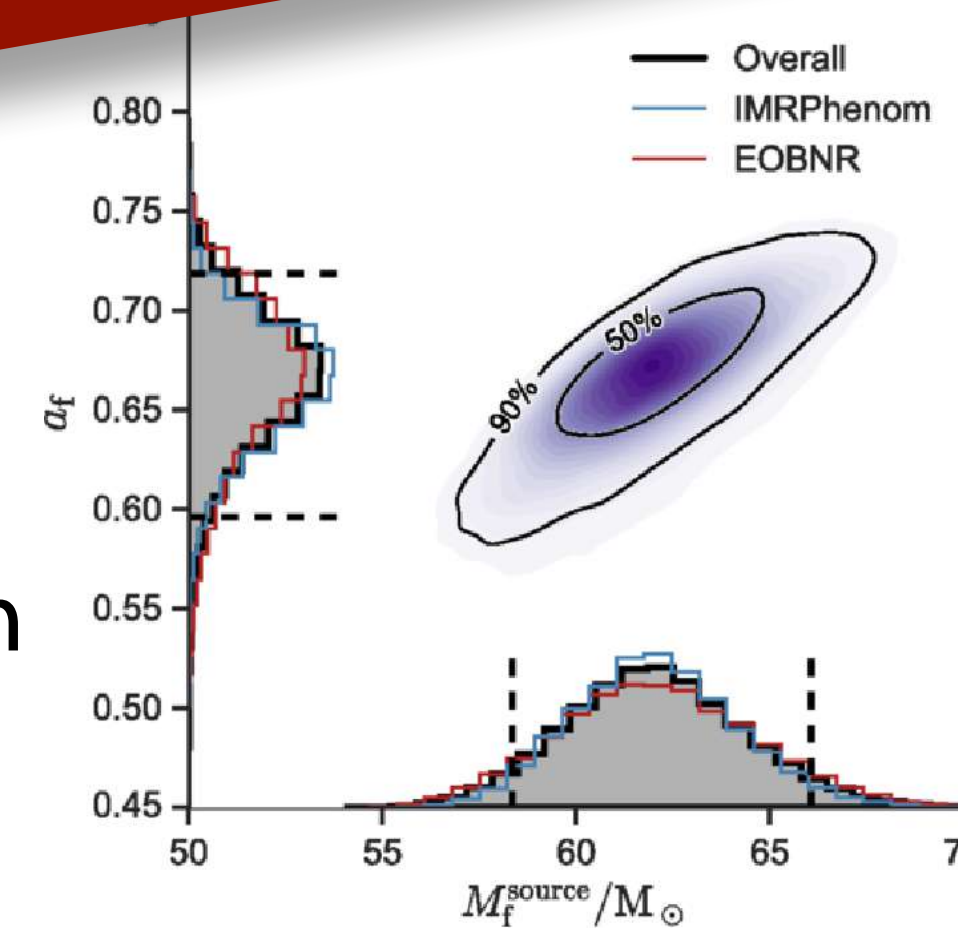


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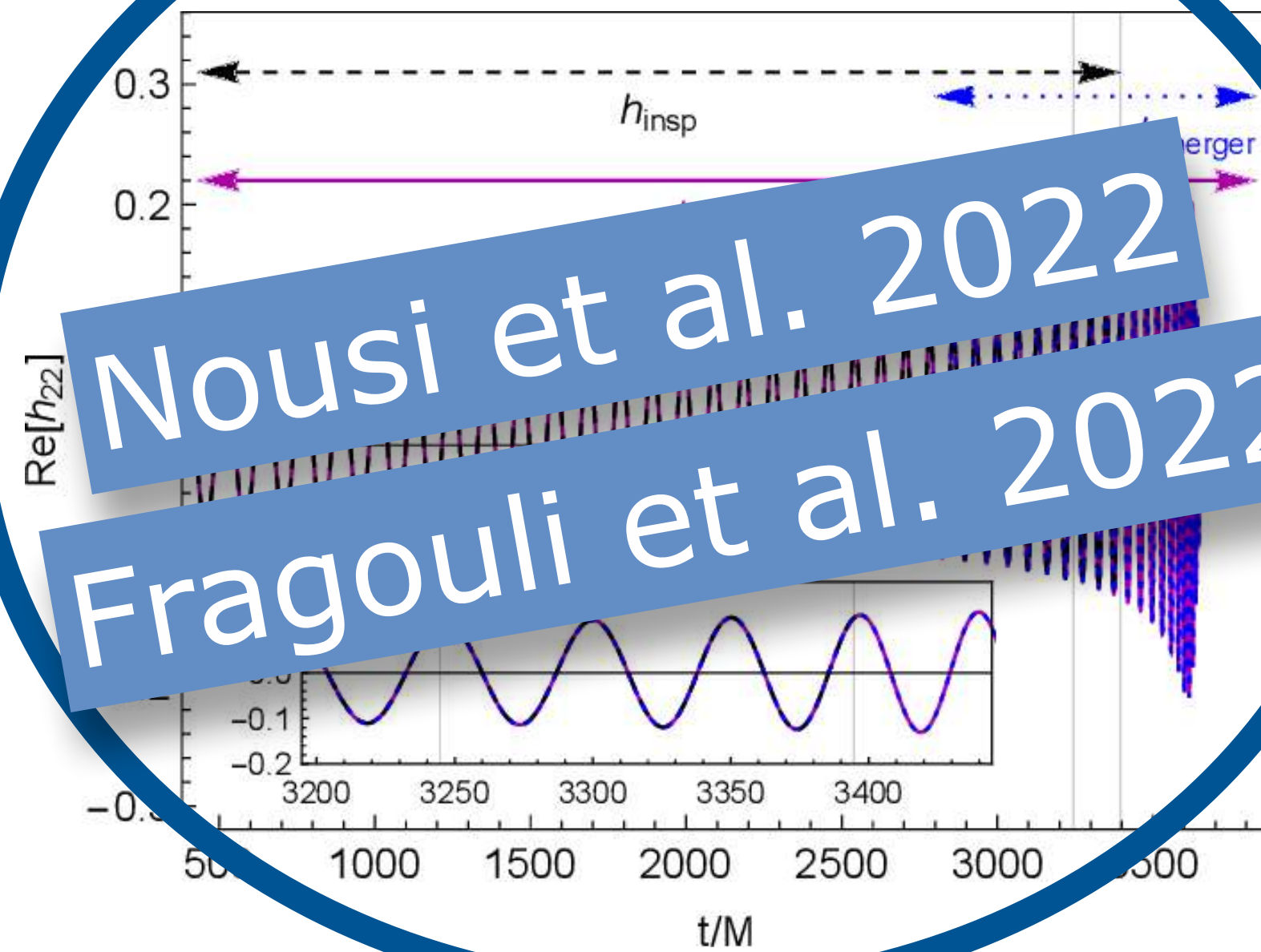
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Nousi et al. 2022

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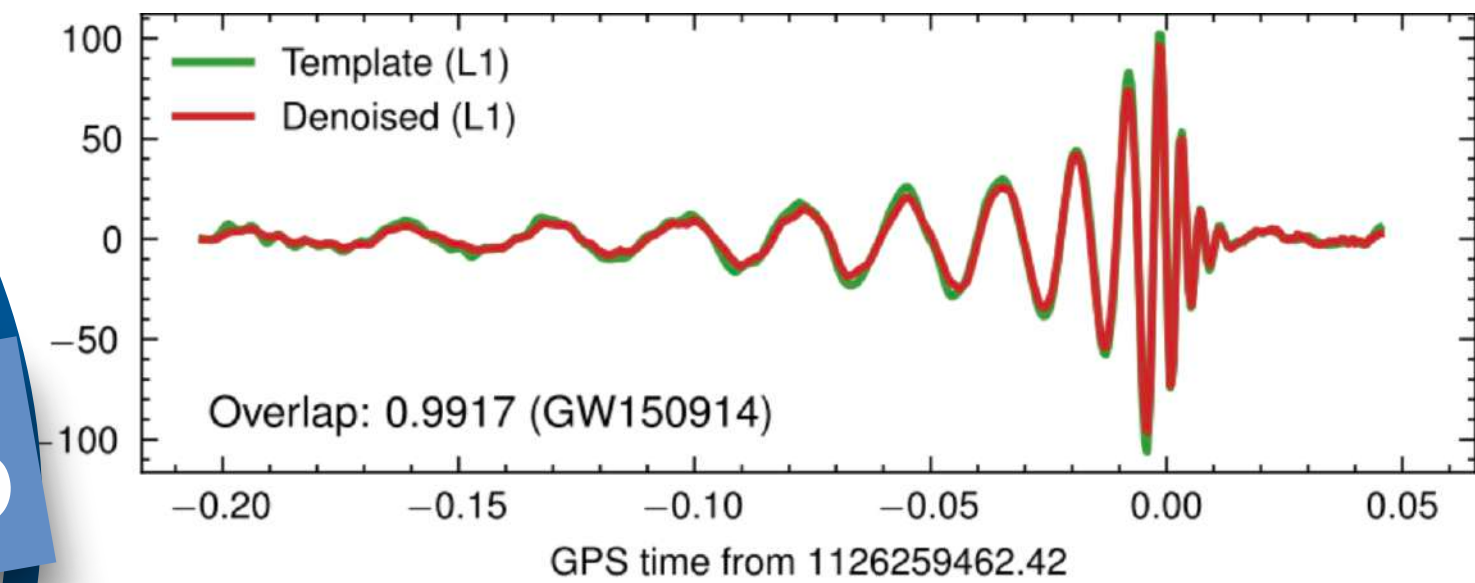
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Nousi et al. 2023

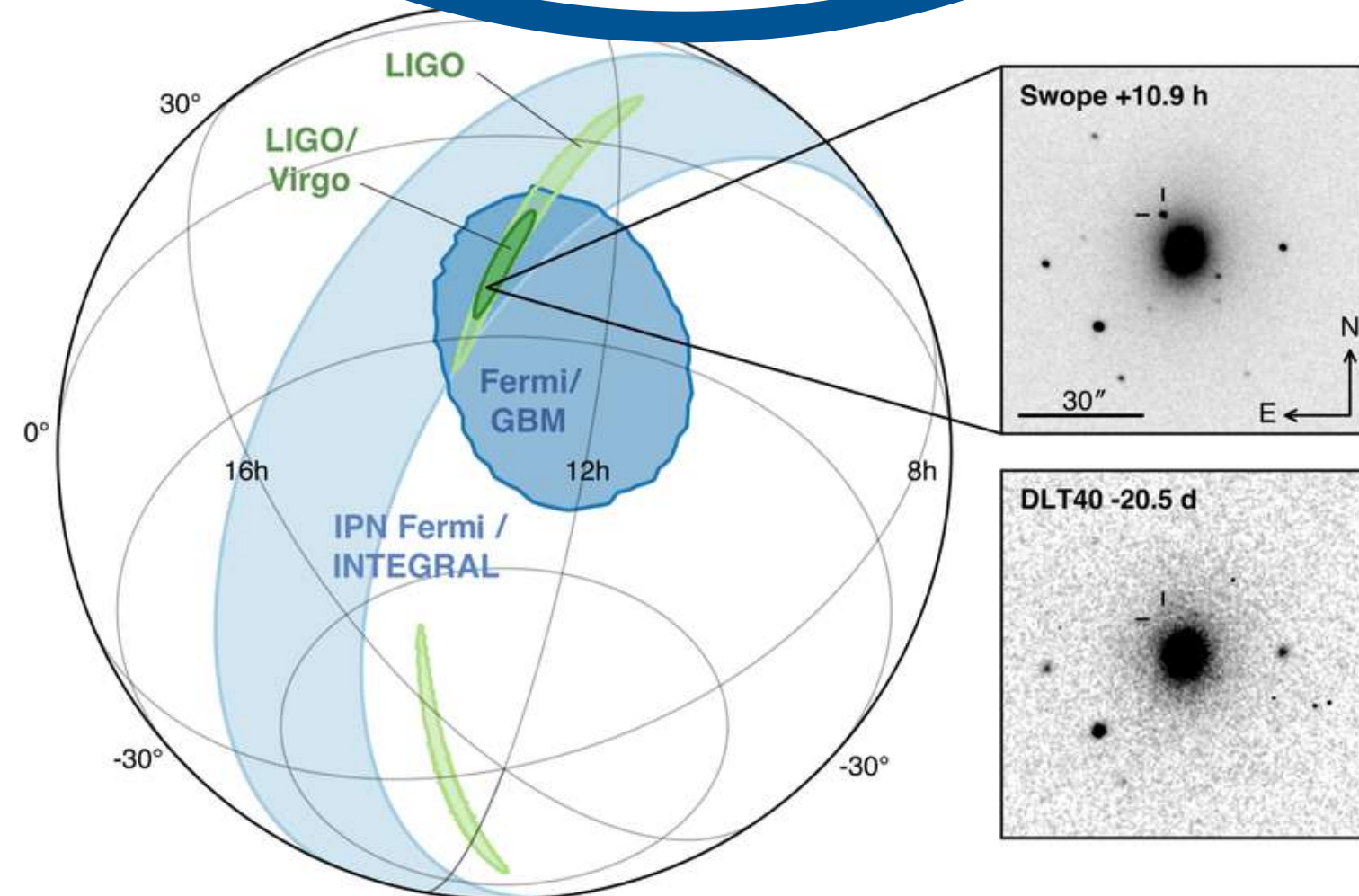
Koloniari et al. 2025

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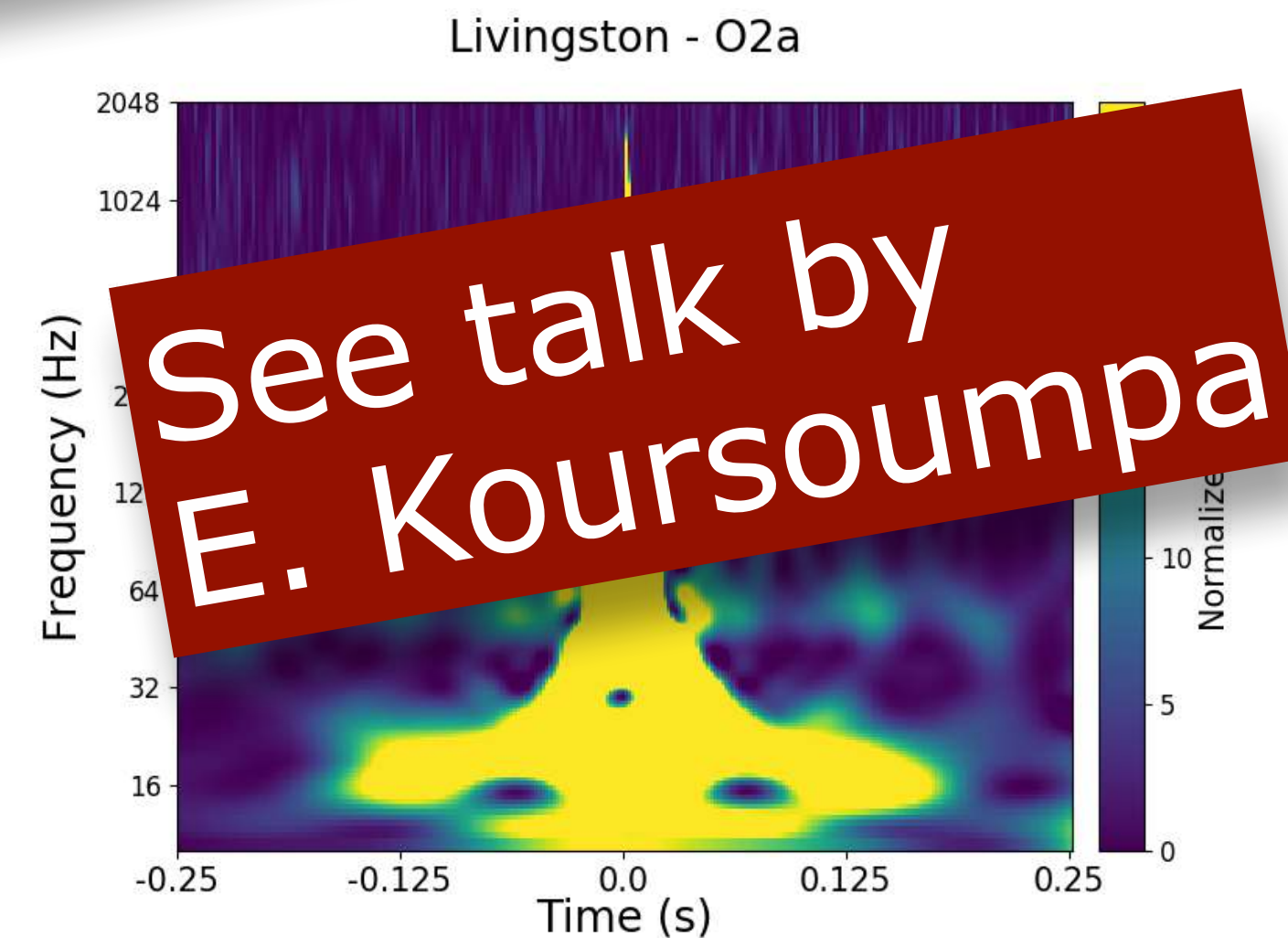
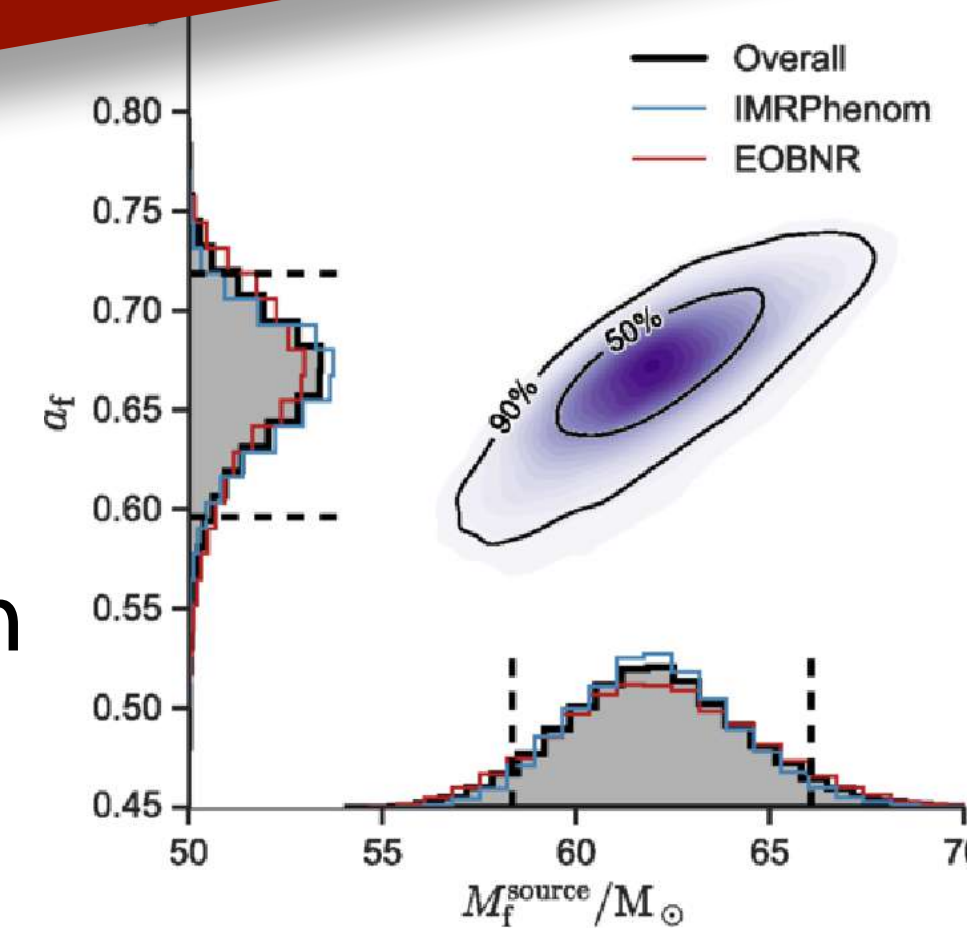


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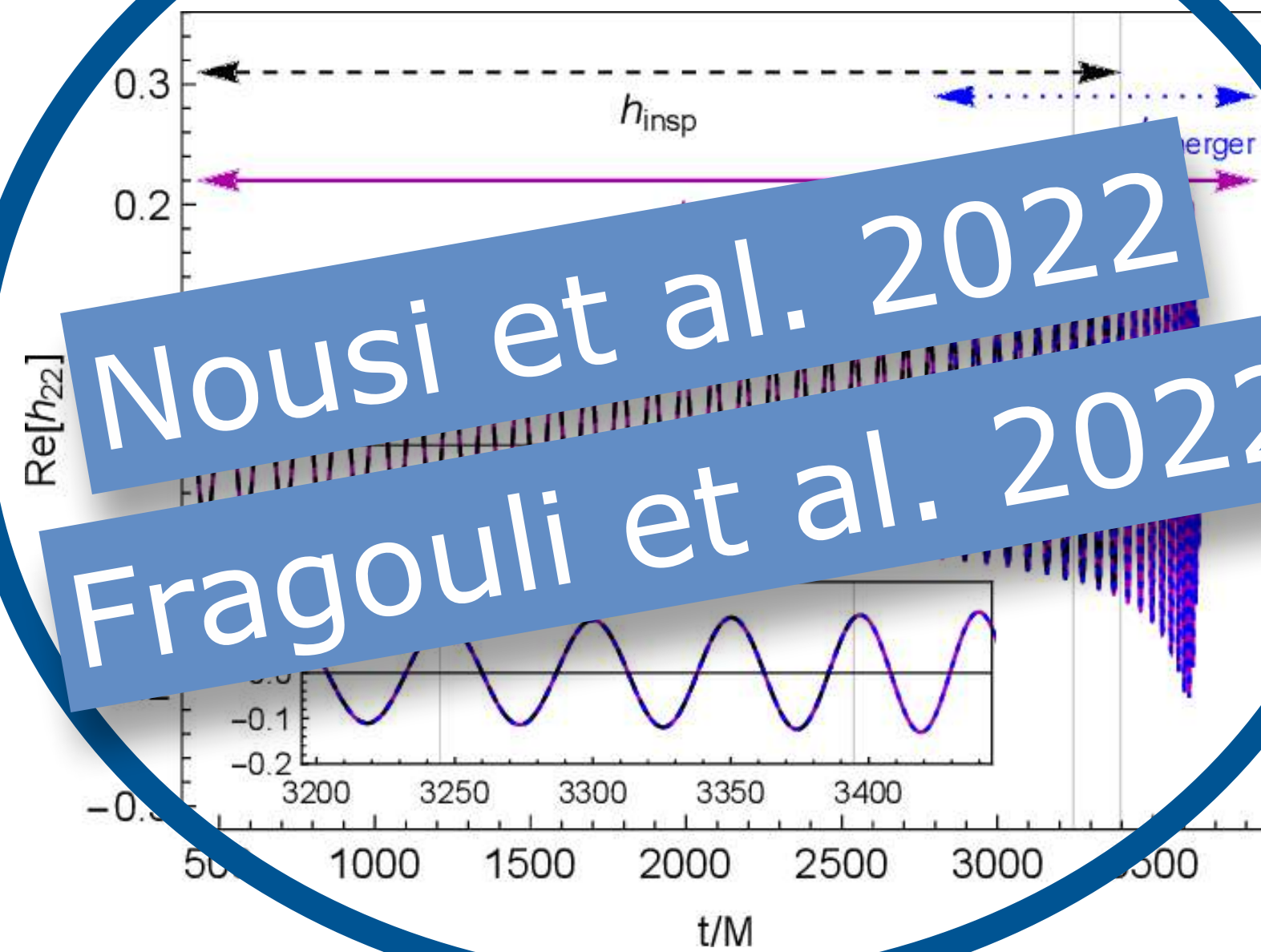
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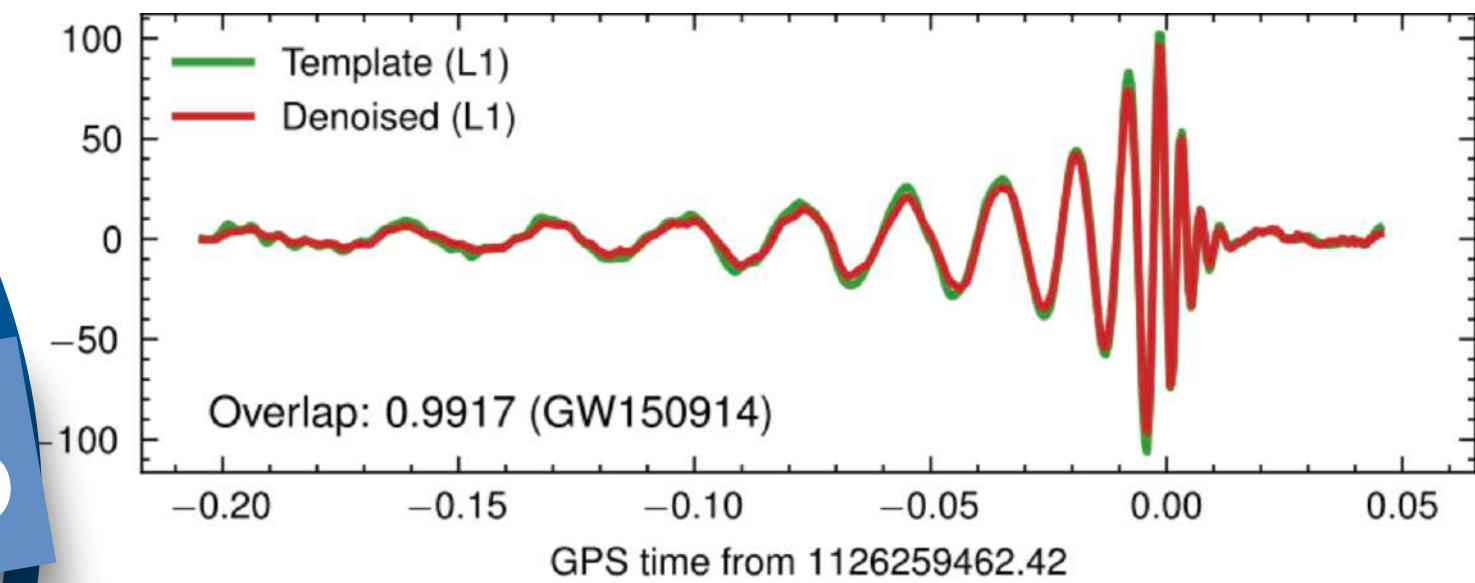
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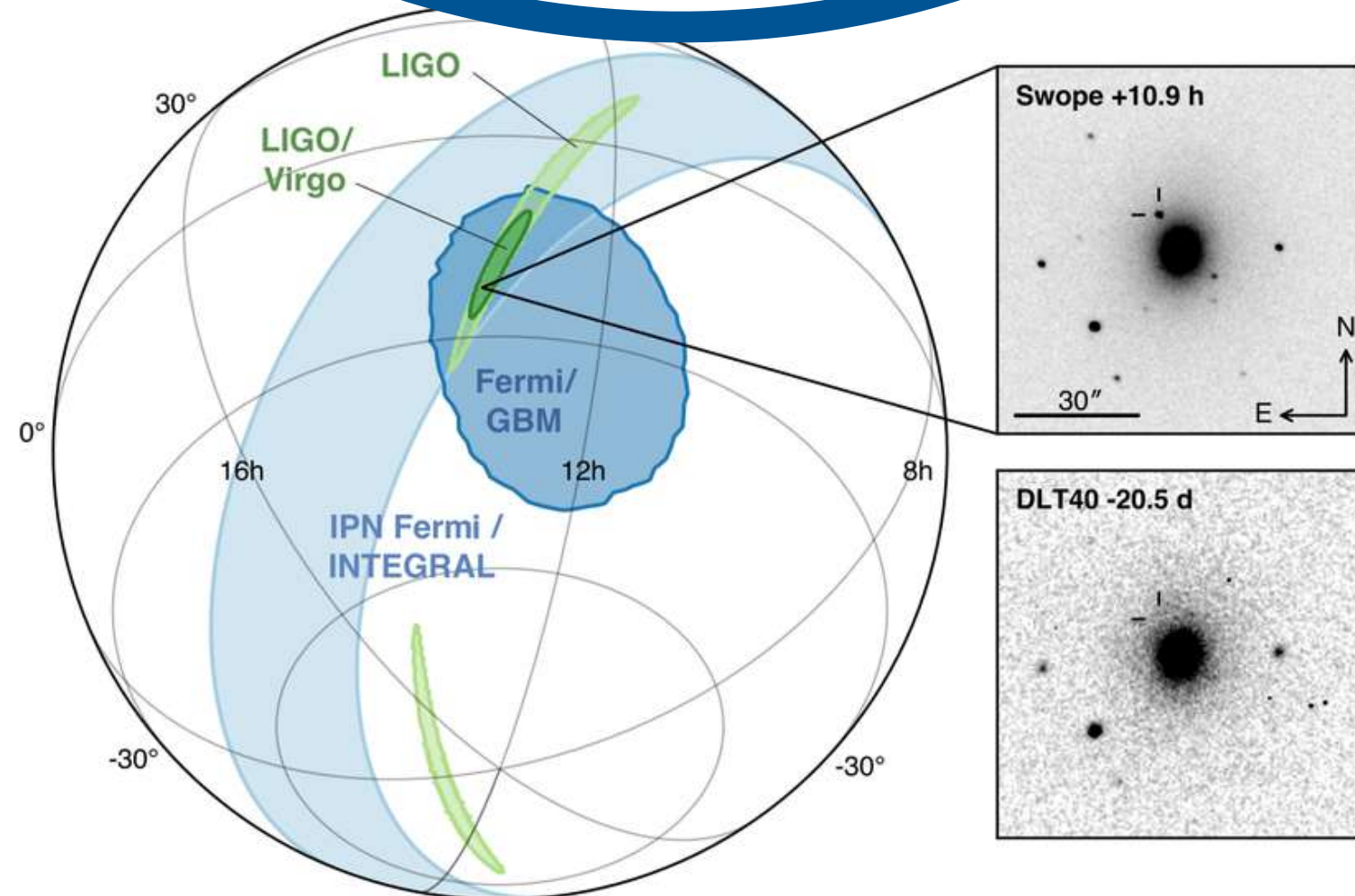
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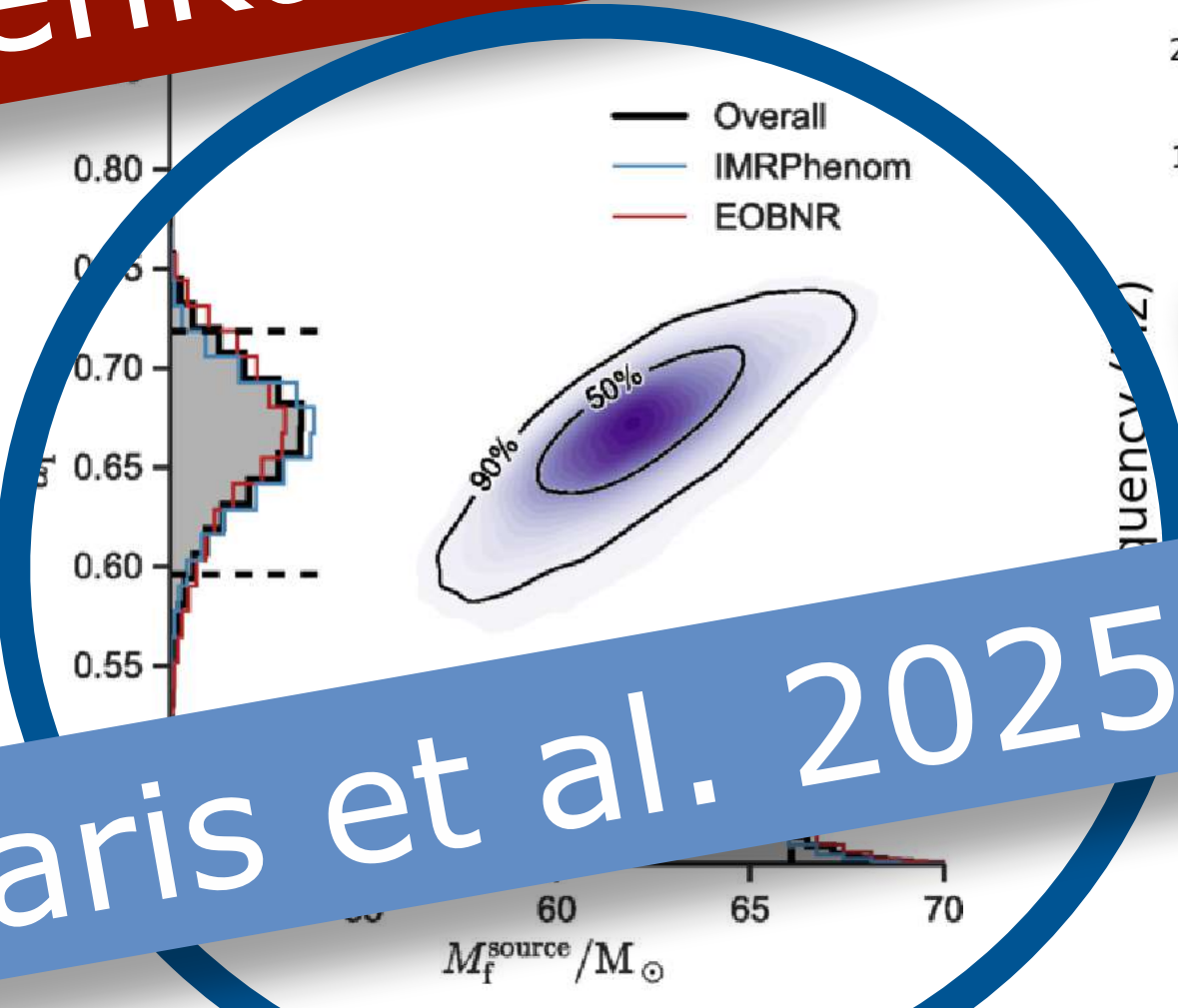
Glitch Classification



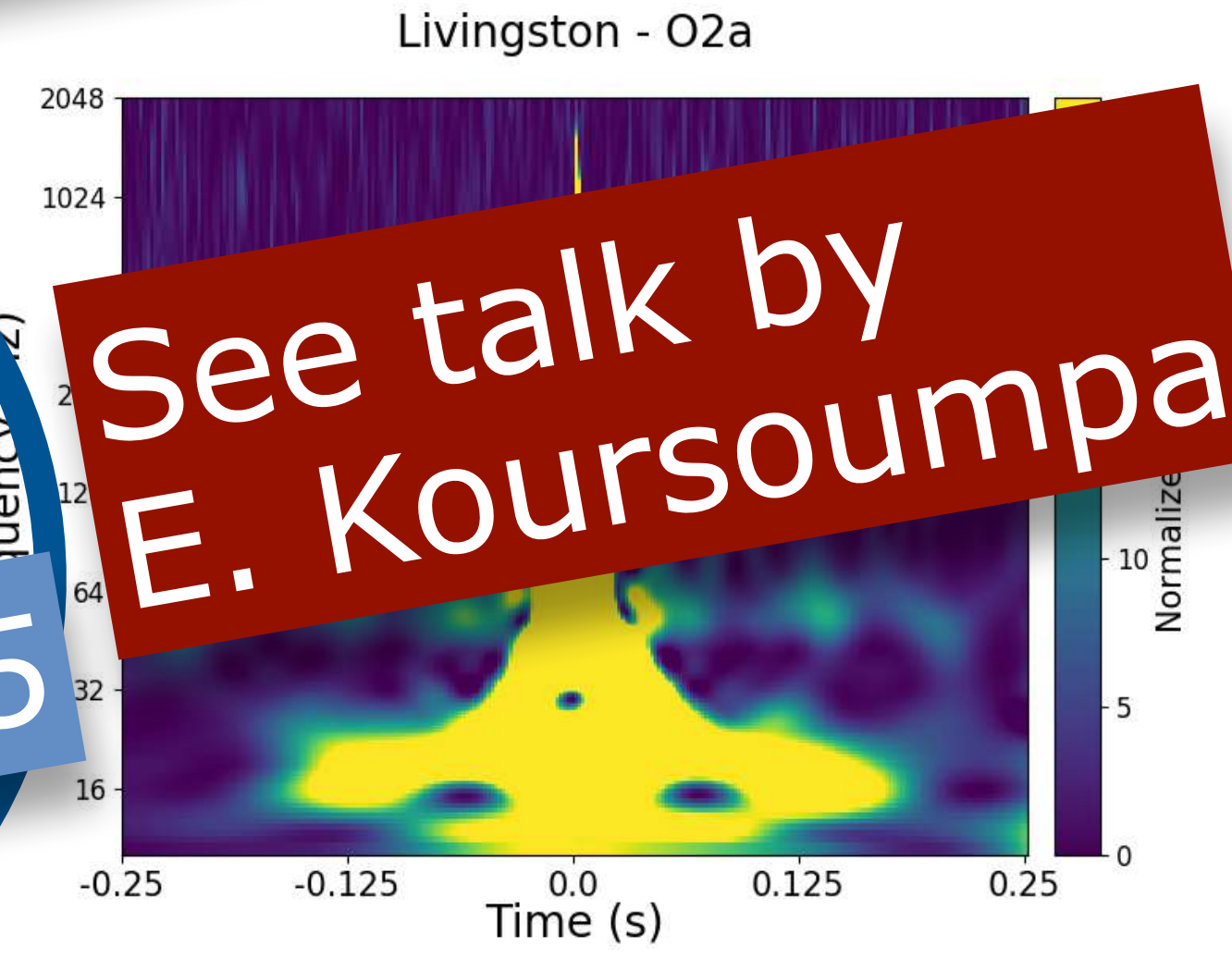
Parameter Estimation

Sky Localization

Vretinakis et al. 2025



See talk by E. Koursoumpa



PHYSICAL REVIEW D **108**, 024022 (2023)

Deep residual networks for gravitational wave detection

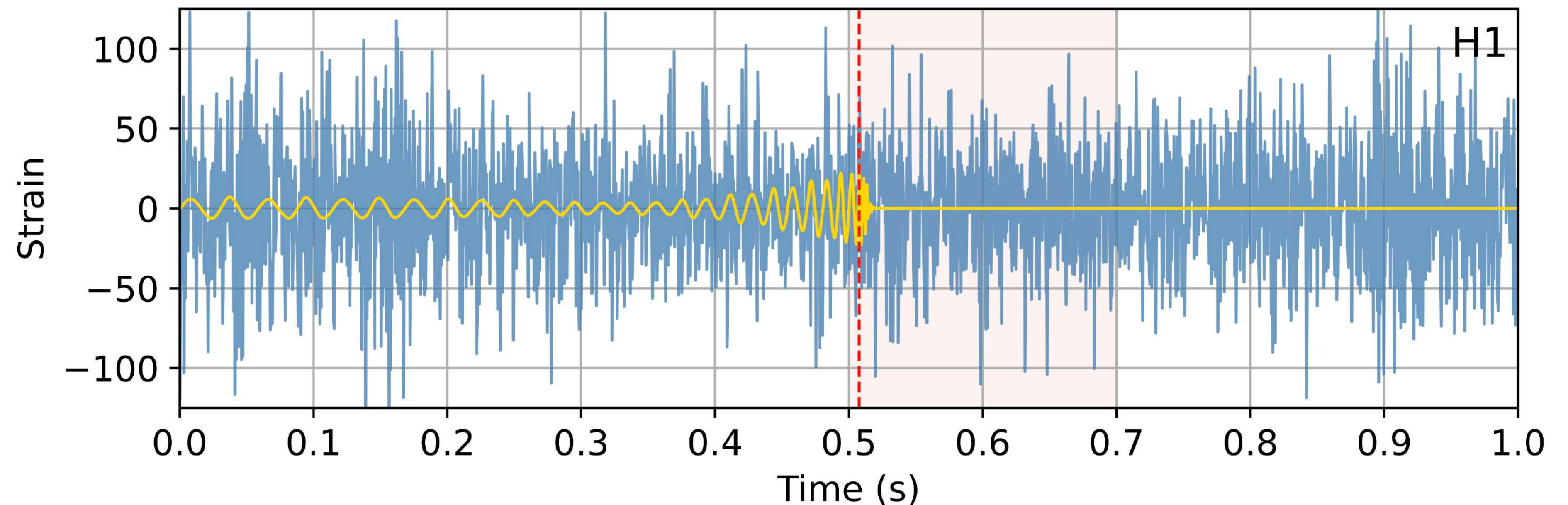
Paraskevi Nousi¹, Alexandra E. Koloniari², Nikolaos Passalis¹, Panagiotis Iosif²,
Nikolaos Stergioulas² and Anastasios Tefas¹

¹*Department of Informatics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece*

²*Department of Physics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece*



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Architecture:

- 54-layer Resnet-1D
- Deep Adaptive Input Normalization
- SNR-based Curriculum Learning
- 30x faster than PyCBC (using a single GPU card)



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Training: 1-second segments @2kHz of BBH injections with [IMRPhenomXPHM](#)
in real O3 noise from L1 and H1

Mass range: $7M_{\odot} \leq M \leq 50M_{\odot}$

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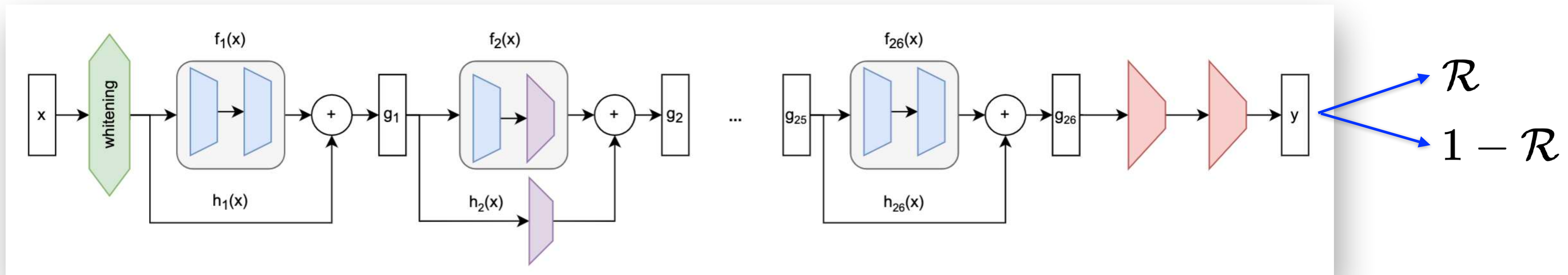
Mass range: $7M_{\odot} \leq M \leq 50M_{\odot}$

Leading algorithm (Virgo-AUTH) in the **1st ML GW search challenge** in the most demanding dataset.

<https://github.com/gwastro/ml-mock-data-challenge-1>

NETWORK ARCHITECTURE OF ARES-GW

1-D ResNet-54 (27 residual blocks with 2 convolutional layers each and skip connections)!

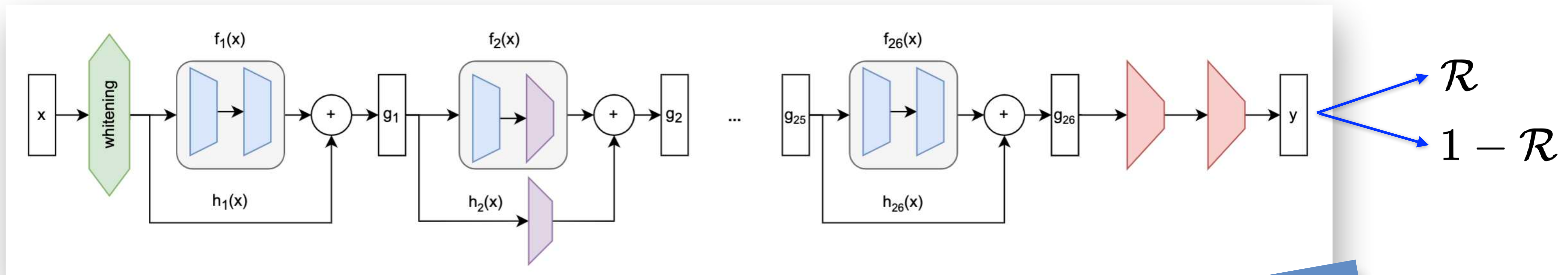


- Residual blocks with skip connections: $g(\mathbf{x}) = f(\mathbf{x}) + h(\mathbf{x})$
- $h(\mathbf{x}) = \mathbf{x}$ or a strided convolutional layer
- After each convolutional layer: batch normalization + ReLU activation
- Mini-batch size of 400 segments
- Adam optimizer for back propagation
- Objective function = regularized binary cross entropy

Residual blocks	Filters	Strided	Input D
4	8		2×2048
1	16	✓	8×2048
2	16		16×1024
1	32	✓	16×1024
2	32		32×512
1	64	✓	32×512
2	64		64×256
1	64	✓	64×256
2	64		64×128
1	64	✓	64×128
2	64		64×64
5	32		64×64
3	16		32×64

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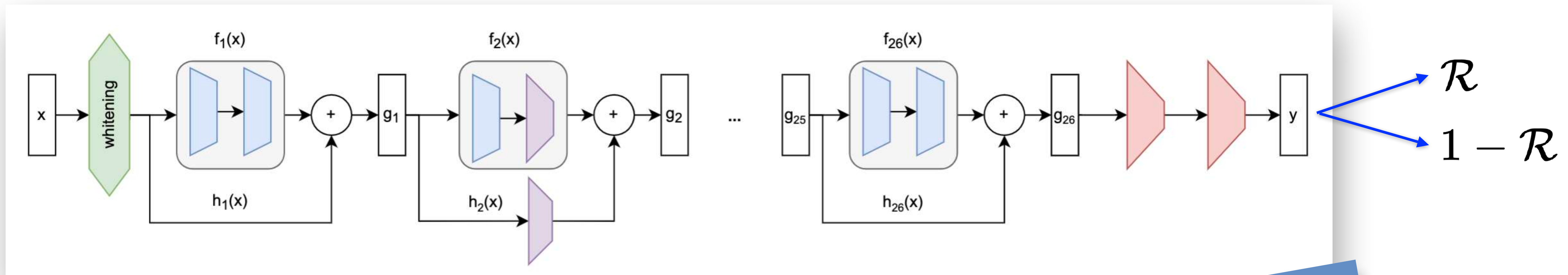
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Gradient problem solved!
-> much deeper networks

			Input D
			2×2048
		✓	8×2048
	16		16×1024
	32	✓	16×1024
1	32		32×512
2	32		32×512
1	64	✓	64×256
2	64		64×256
1	64	✓	64×128
2	64		64×128
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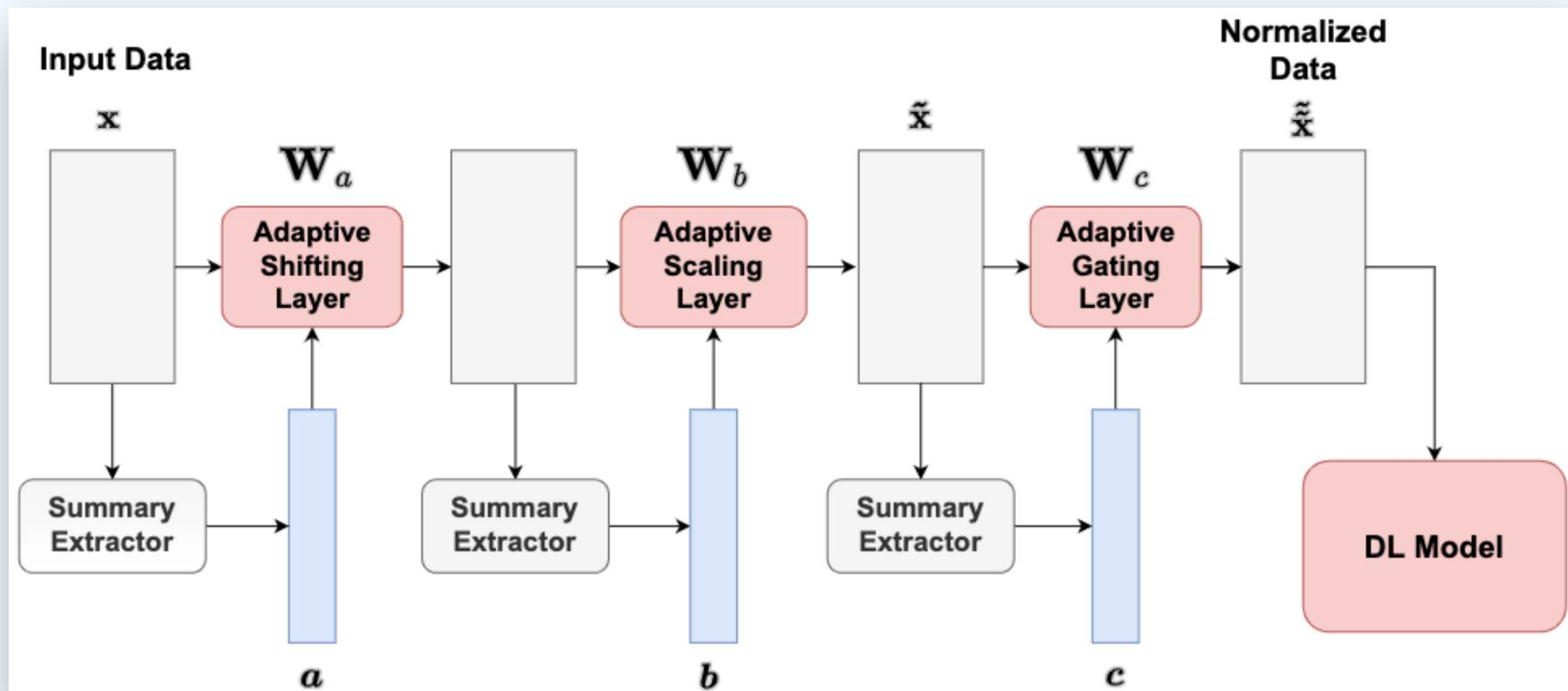
1-D ResNet-54 now used by most
ML GW detection codes

		Input D
		2×2048
		8×2048
1	16	✓
2	32	
3	64	
4	64	✓
5	32	
6	16	
		64×256
		64×128
		64×128
		64×64
		64×64
		32×64

ADAPTIVE INPUT NORMALIZATION

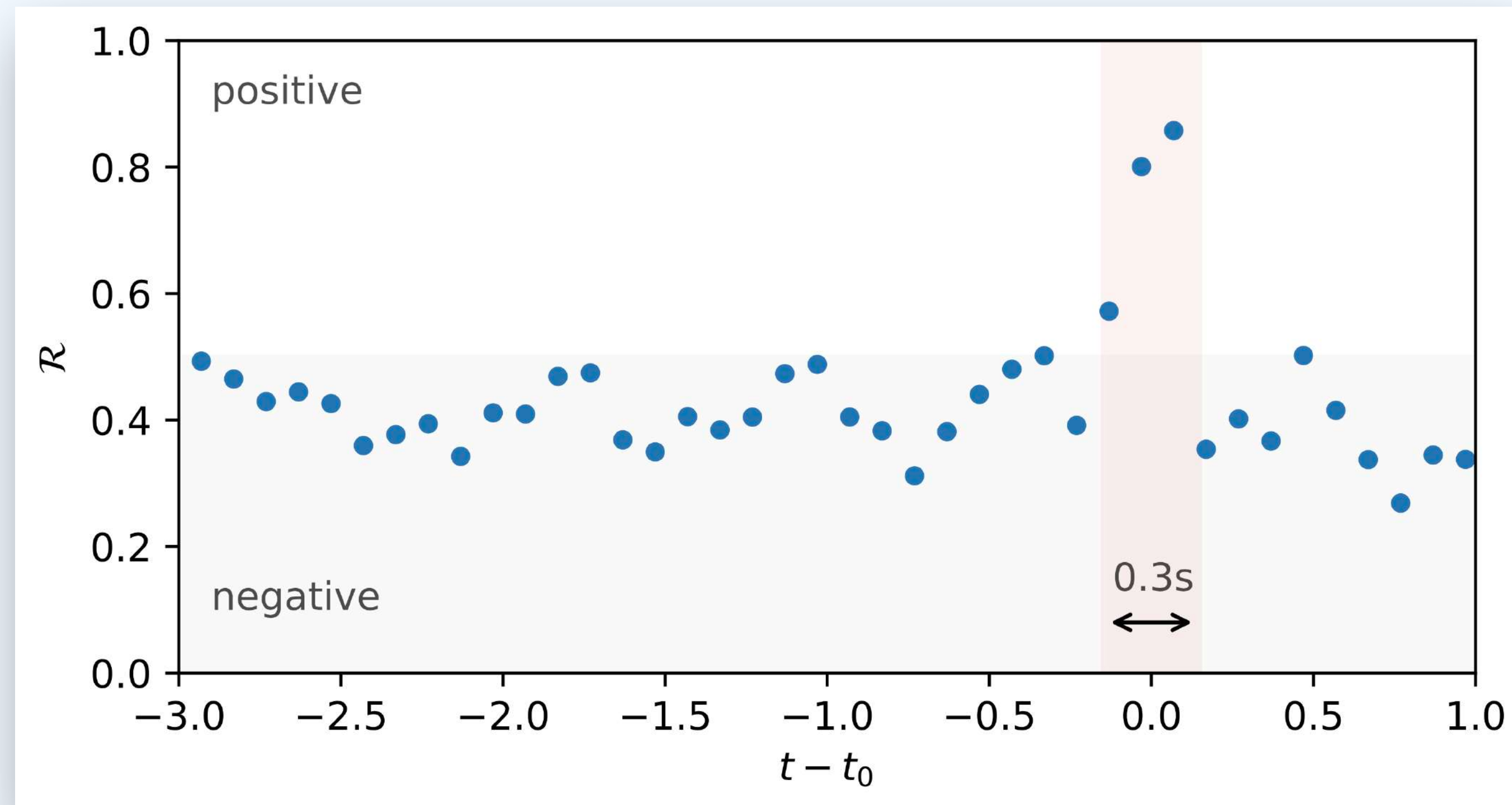
Deep Adaptive Input Normalization (DAIN) (Passalis et al. 2019)

Is applied during training - weights $\mathbf{W}_a$, $\mathbf{W}_b$, $\mathbf{W}_c$ are learnable and adapt to input data!



RANKING STATISTIC

Neural Network Ranking Statistic $\mathcal{R}$ is reported every 0.1 s of input data



Logarithmic Ranking Statistic

$$\mathcal{R}_s = -\log_{10}(1 - \mathcal{R} + 10^{-16})$$

ARESGW ON GITHUB

<https://github.com/vivinousi/gw-detection-deep-learning>

The screenshot displays the GitHub repository page for `vivinousi/gw-detection-deep-learning`. The repository is public and has 22 stars and 2 forks. The main content area shows the repository structure with a table of files and folders, their commit history, and the README content.

File/Folder	Commit Message	Commit Date
doc	readme update	2 years ago
modules	training code initial commit	2 years ago
trained_models	training code initial commit	2 years ago
utils	training code initial commit	2 years ago
LICENSE	Initial commit	2 years ago
README.md	readme update	2 years ago
run_on_test.sh	training code initial commit	2 years ago
test.py	training code initial commit	2 years ago
test_challenge_model.py	training code initial commit	2 years ago
train.py	readme update	2 years ago

The README content is as follows:

AResGW: Augmentation and RESidual networks for Gravitational Wave detection

Gravitational wave detection in real noise timeseries using deep residual neural networks.

This repository contains the method submitted by our team, Virgo-AUTH, to the [MLGWSC](#) competition. Our method contains the following components:



PAPER

New gravitational wave discoveries enabled by machine learning

OPEN ACCESS

Alexandra E Koloniari^{1,*} , Evdokia C Koursoumpa¹ , Paraskevi Nousi² , Paraskevas Lampropoulos¹ , Nikolaos Passalis³ , Anastasios Tefas⁴  and Nikolaos Stergioulas¹ 

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¹ Department of Physics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece

² Swiss Data Science Center, ETH, Zürich, Switzerland

³ Department of Chemical Engineering, Faculty of Engineering, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece

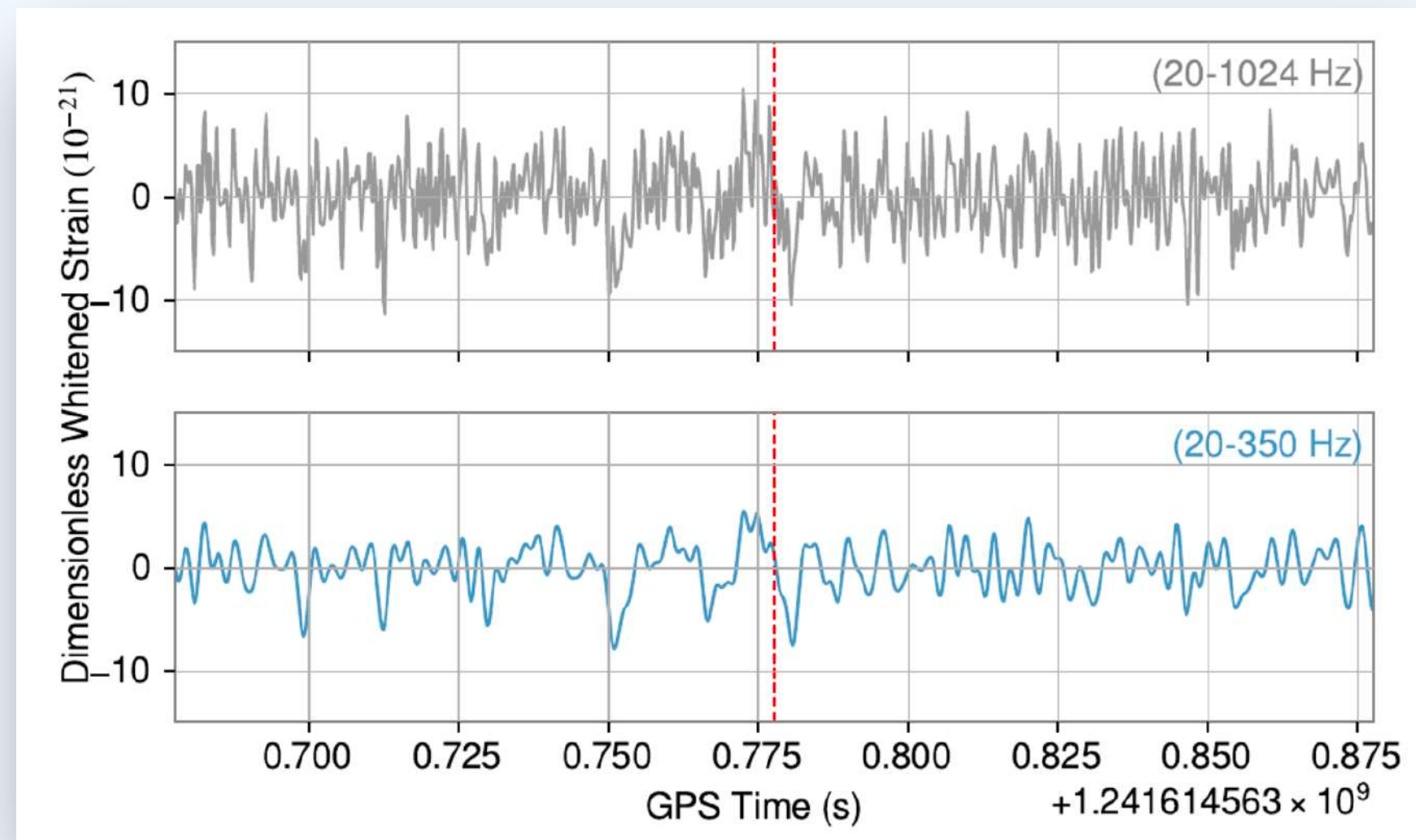
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* Author to whom any correspondence should be addressed.

E-mail: akolonia@auth.gr

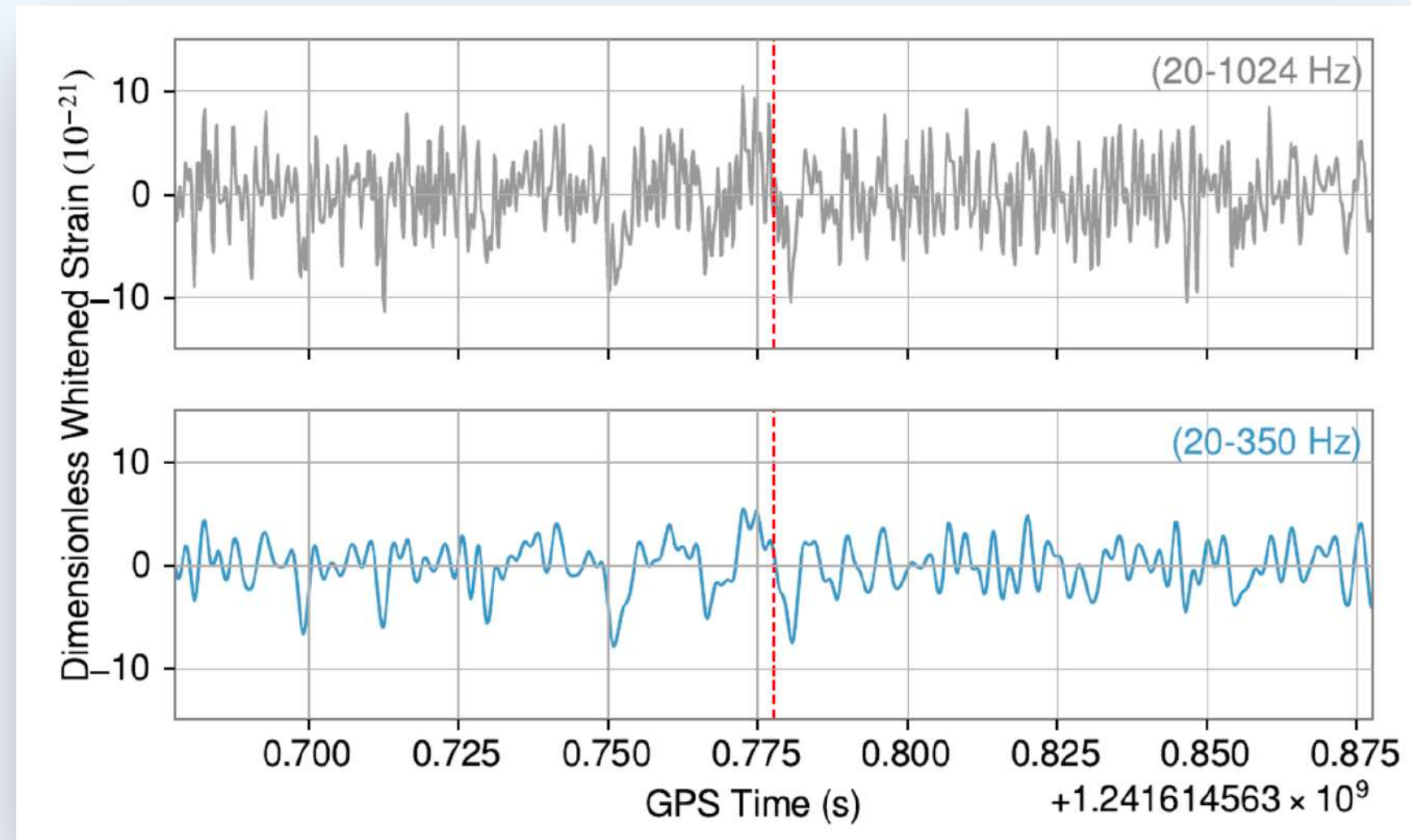
MAIN ENHANCEMENTS:

1) Training on low-pass filtered data

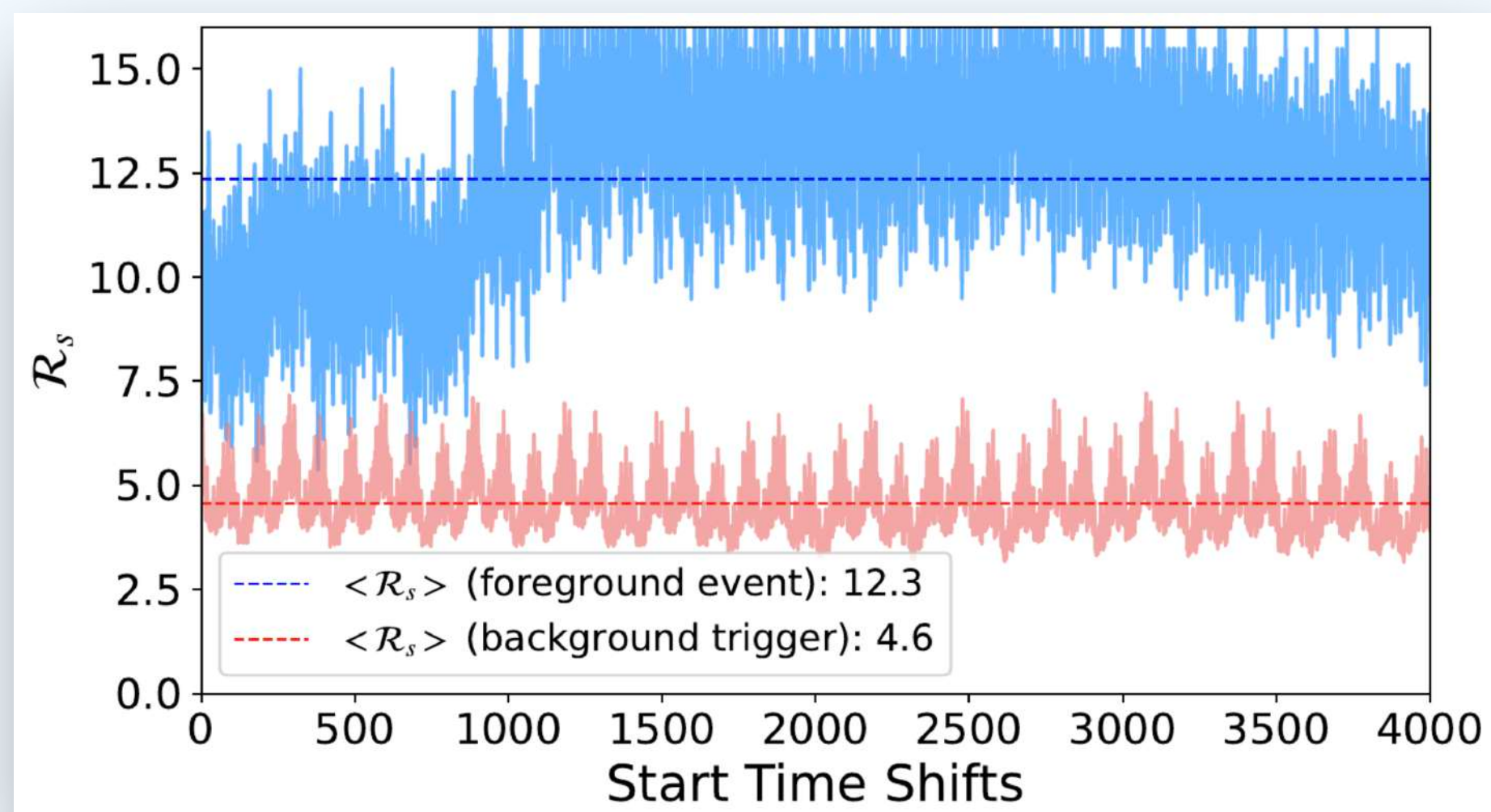


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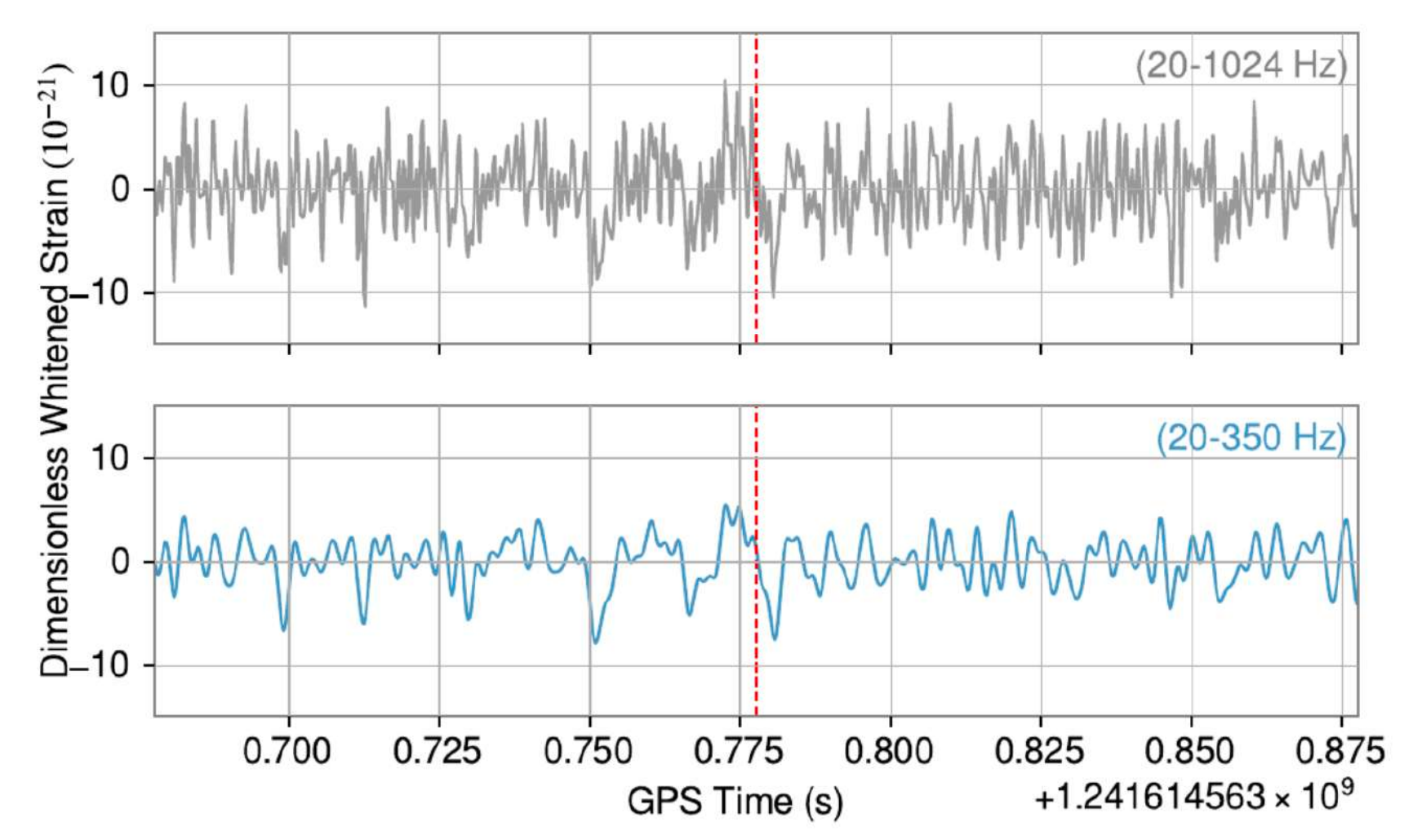


2) Ensemble-averaged ranking statistic

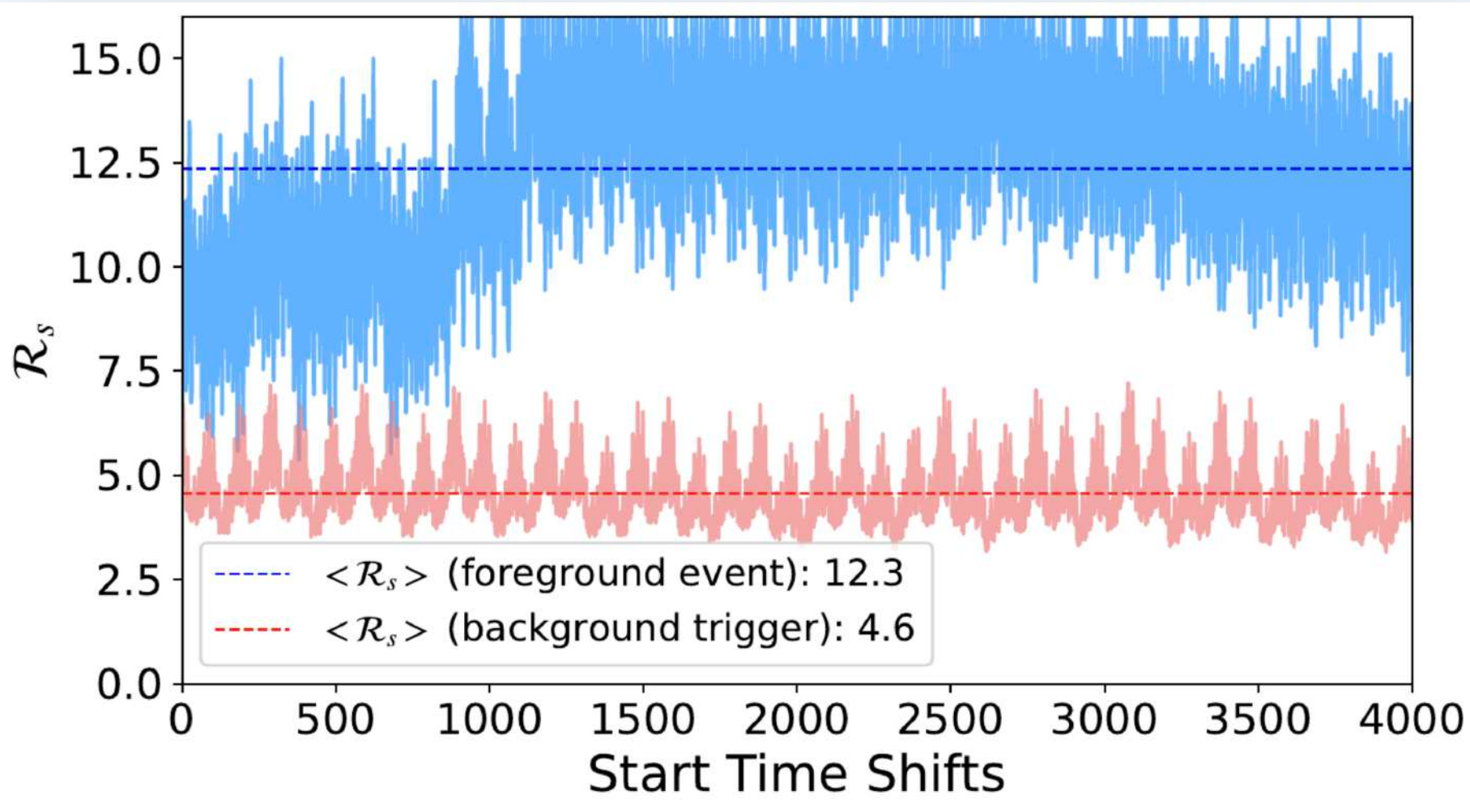


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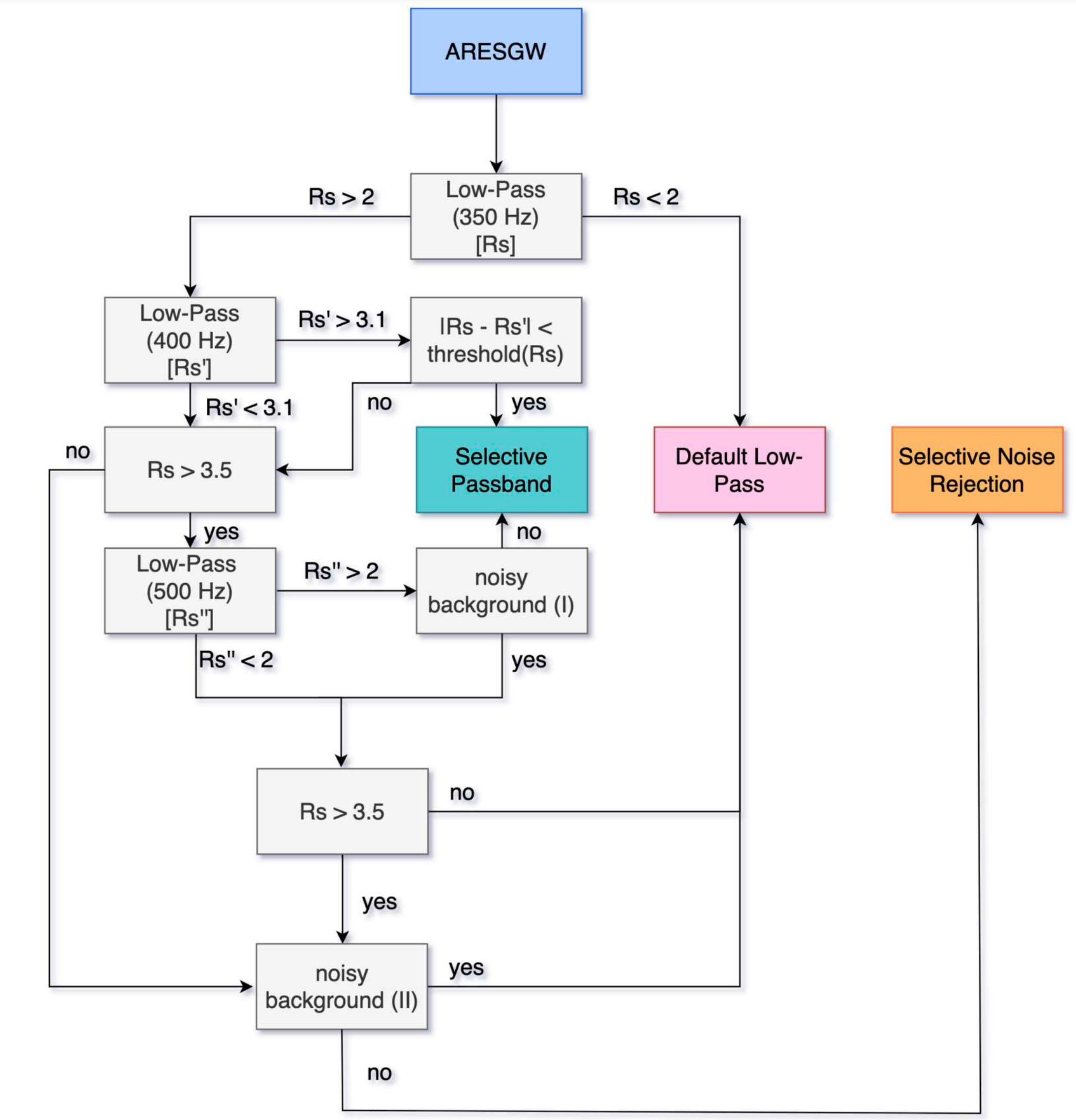
1) Training on low-pass filtered data



2) Ensemble-averaged ranking statistic



3) Application of noise filters to reduce background FAR.



ASTROPHYSICAL PROBABILITY

p_astro is calculated as

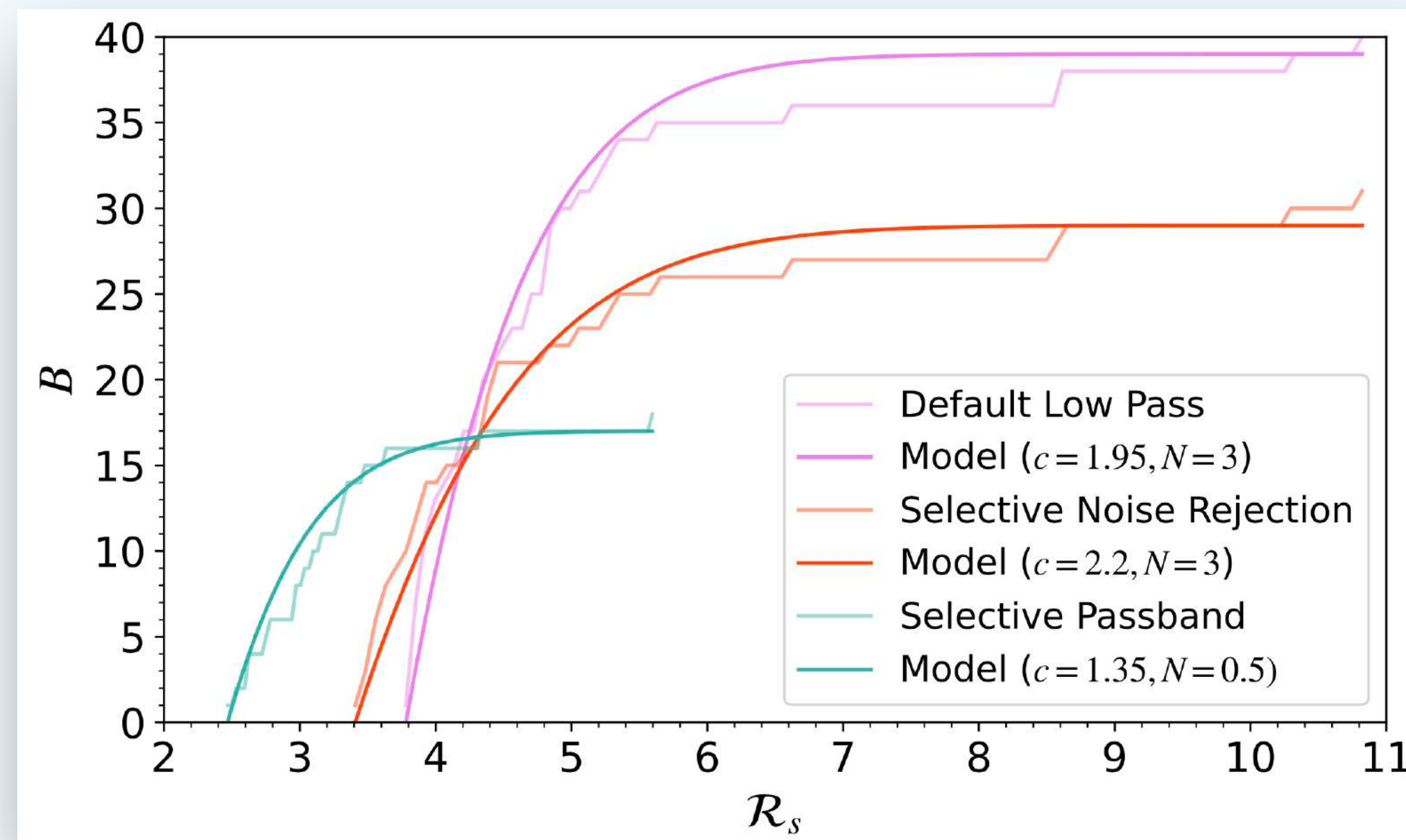
$$p_{\text{astro}} = \frac{f(\mathcal{R}_s)}{b(\mathcal{R}_s) + f(\mathcal{R}_s)}$$

where the **background** and **foreground differential rates** are

$$b(\mathcal{R}_s) = \frac{dB}{d\mathcal{R}_s} \quad f(\mathcal{R}_s) = \frac{dF}{d\mathcal{R}_s}$$

The cumulative distribution of the **O3 background** is modeled **analytically** as

$$\hat{B}(x) = \frac{\left(1 + \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right)\right)^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}{2^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}$$

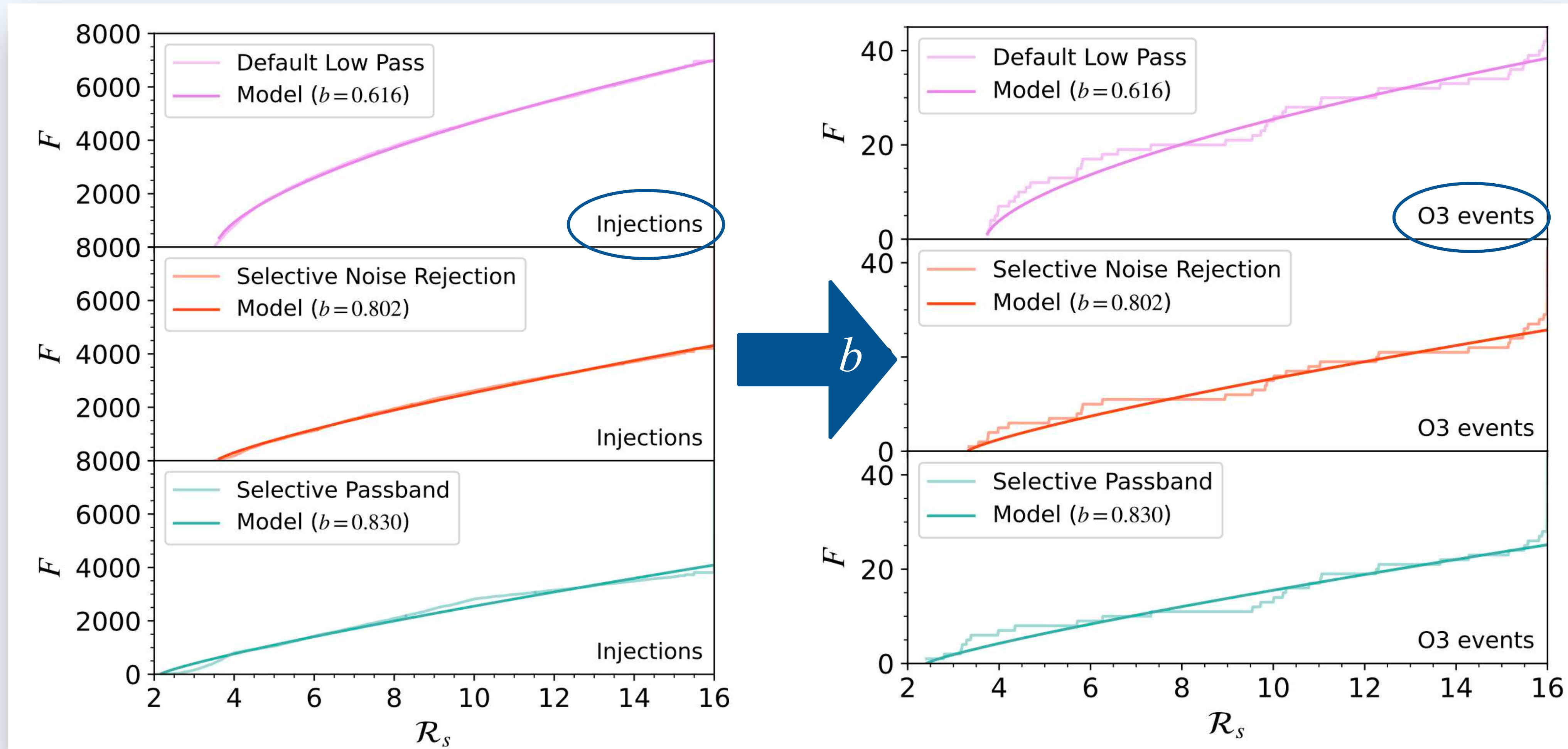


ASTROPHYSICAL PROBABILITY

Analytic model of **cumulative foreground** distribution:

$$F(x) = a(x - x_{\min})^b$$

Coefficient **b** determined through **injections** in O3 noise:



NEW GW DETECTIONS WITH AresGW IN O3 DATA

AresGW detects **42 out of 51** known O3 events (*most sensitive pipeline in this mass range*)

We found **8 new gravitational wave candidates** with $p_{\text{astro}} > 50\%$ (3 $p_{\text{astro}} > 99\%$).

TABLE VII: New candidate events identified by AresGW.

#	Event Name	GPS Time (s)	p_{astro}	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay (s)	χ_L^2	χ_H^2	Class
1	GW190511_125545	1241614563.77	1.00	0.27	9.54	0.0027	1.16	1.46	Selective Passband
2	GW190614_134749	1244555287.93	0.99	4.6	5.80	0.0012	0.65	0.80	Selective Passband
3	GW190607_083827	1243931925.99	0.99	6.5	8.95	0.0056	0.90	0.48	Selective Noise Rejection
4	GW190904_104631	1251629209.01	0.72	14	4.35	0.0002	0.38	0.71	Selective Passband
5	GW190523_085933	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
6	GW200208_211609	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

NEW GW DETECTIONS WITH AresGW IN O3 DATA

AresGW detects **42 out of 51** known O3 events (*most sensitive pipeline in this mass range*)

We found **8 new gravitational wave candidates** with $p_{\text{astro}} > 50\%$ (3 $p_{\text{astro}} > 99\%$).

TABLE VII: New candidate events identified by AresGW.

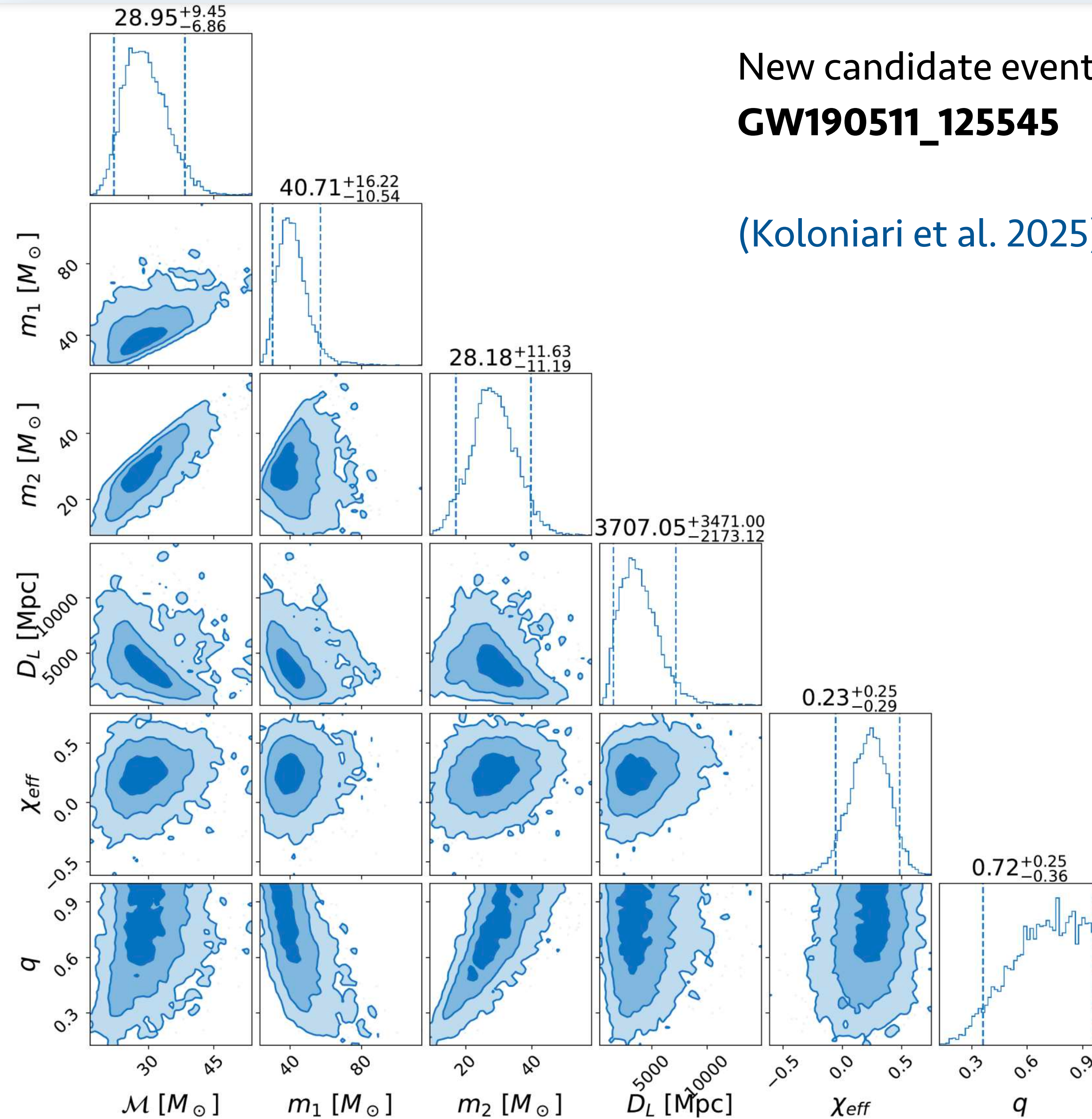
#	Event Name	GPS Time (s)	p_{astro}	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay	χ^2	ρ	Class
1	GW190511_125545	1241614563.77	1.00	1	3.95	0.00001	0.90	0.80	Selective Passband
2	GW190614_134740	1242637191.44	0.99	1	3.95	0.00001	0.90	0.80	Selective Passband
3	GW190607_083053	1242637191.44	0.72	14	4.35	0.0002	0.38	0.71	Selective Noise Rejection
4	GW190904_104351	1265231787.68	0.68	20	6.60	0.0054	0.75	1.39	Selective Passband
5	GW190523_085353	1242637191.44	0.55	18	4.0	0.0063	0.69	0.98	Selective Noise Rejection
6	GW200208_211609	1265231787.68	0.51	49	5.82	0.0103	1.05	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

First GW events identified
using a machine-learning algorithm

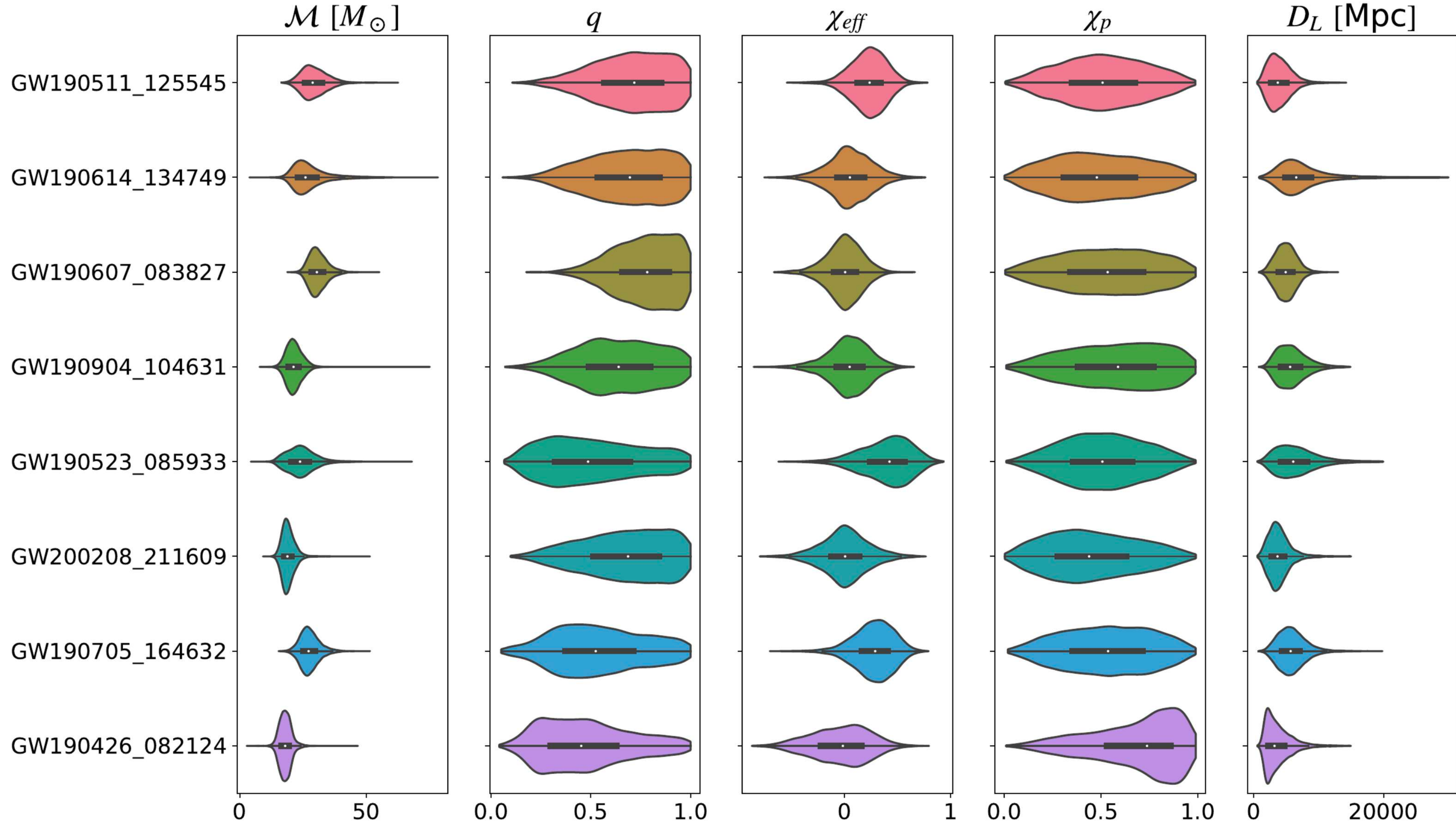
PARAMETER ESTIMATION USING BILBY

New candidate event
GW190511_125545

(Koloniari et al. 2025)



PARAMETER ESTIMATION USING BILBY



RECONSTRUCTED WAVEFORMS FOR NEW EVENTS

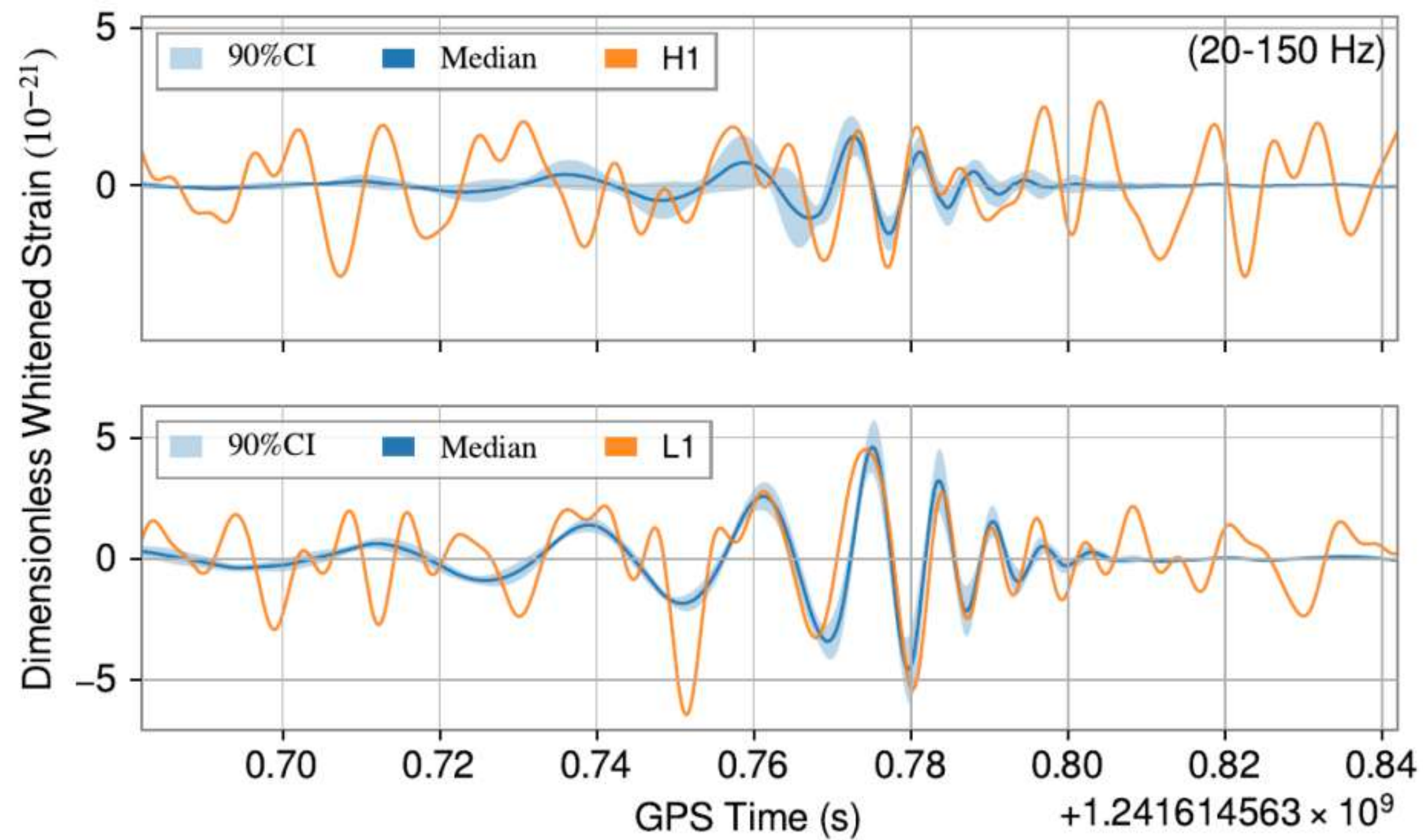


FIG. 35: Whitened, bandpassed strain data and reconstructed waveform for the new event GW190511_125545 identified by AresGW.

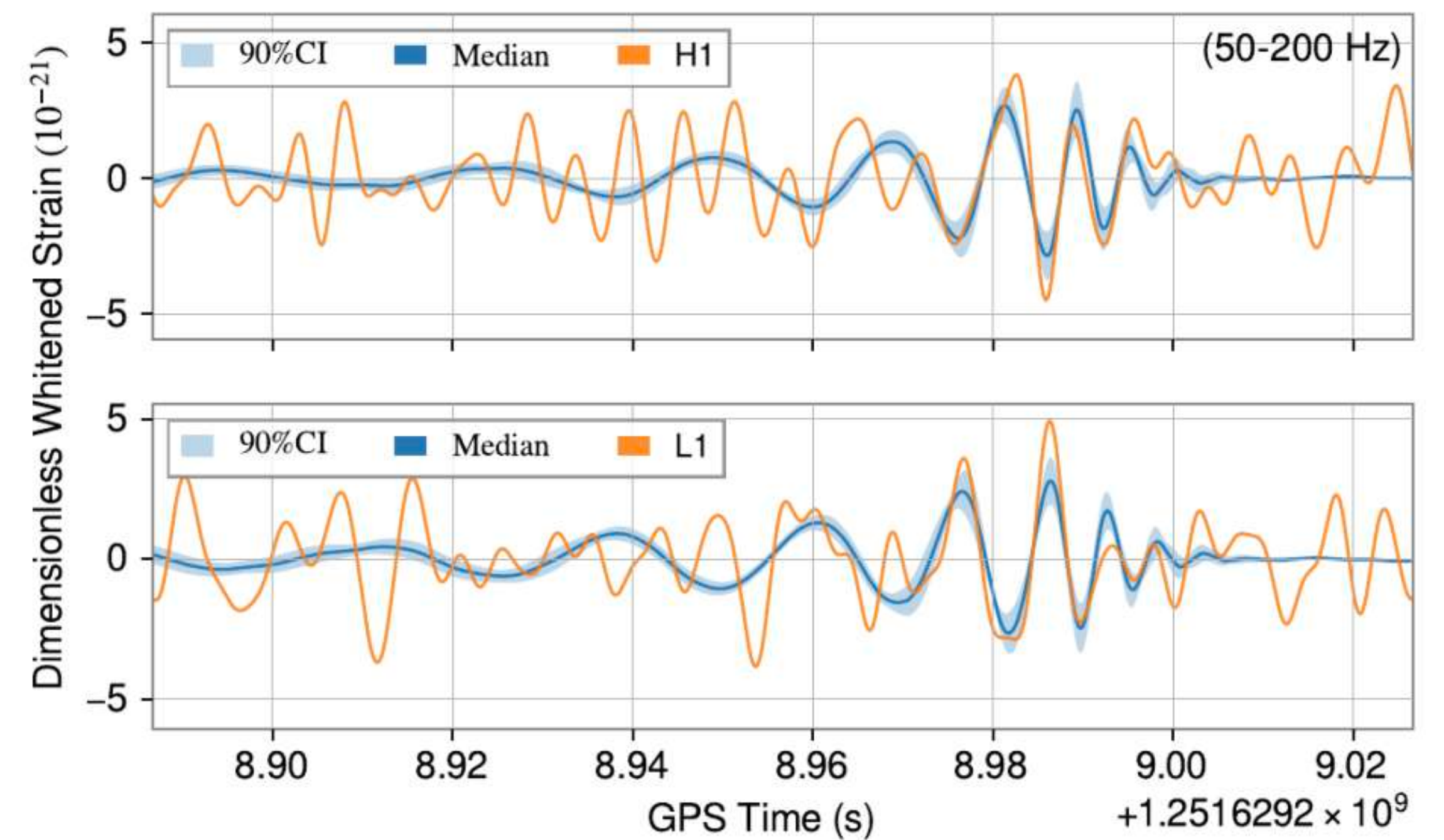
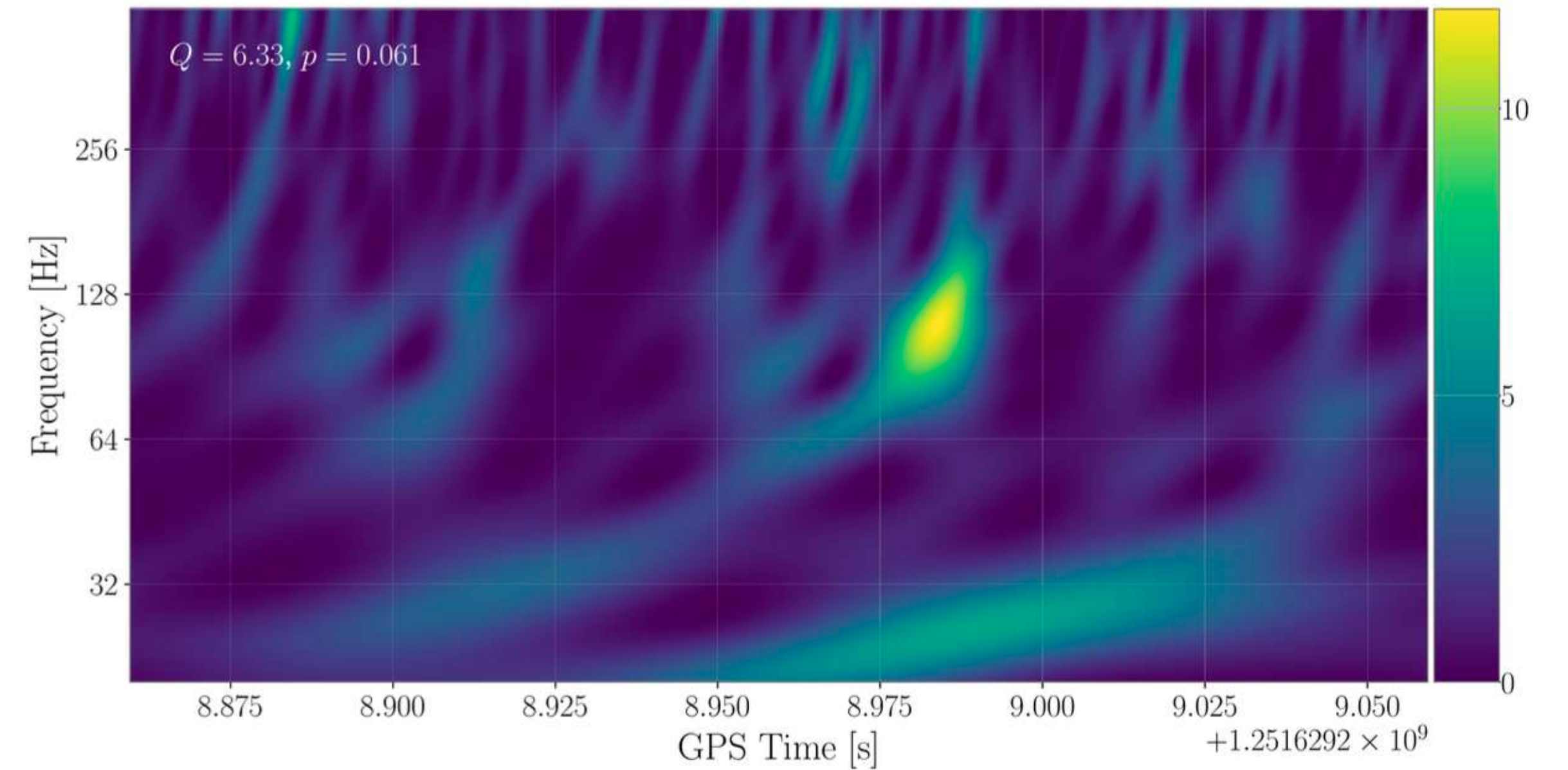
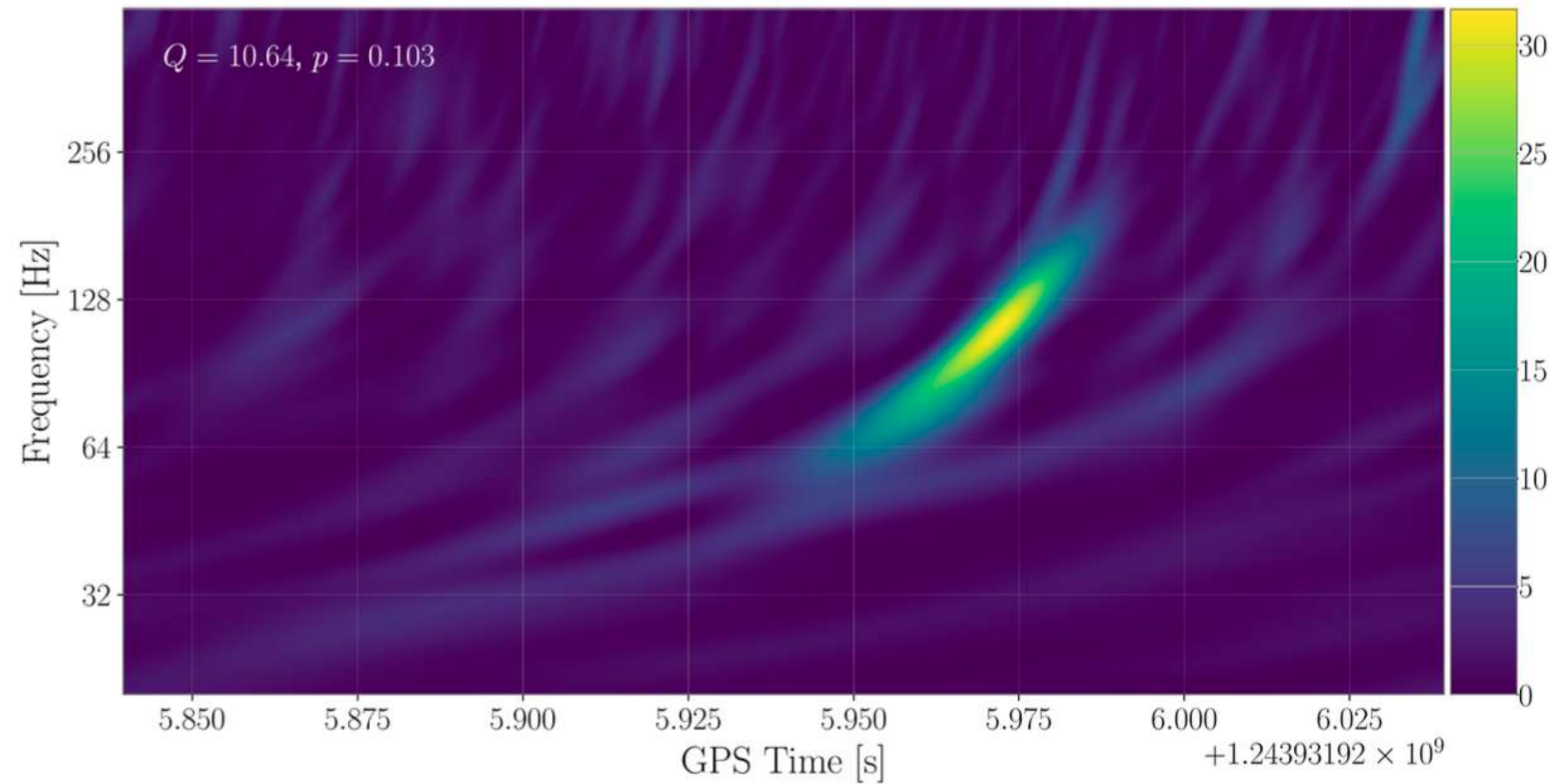
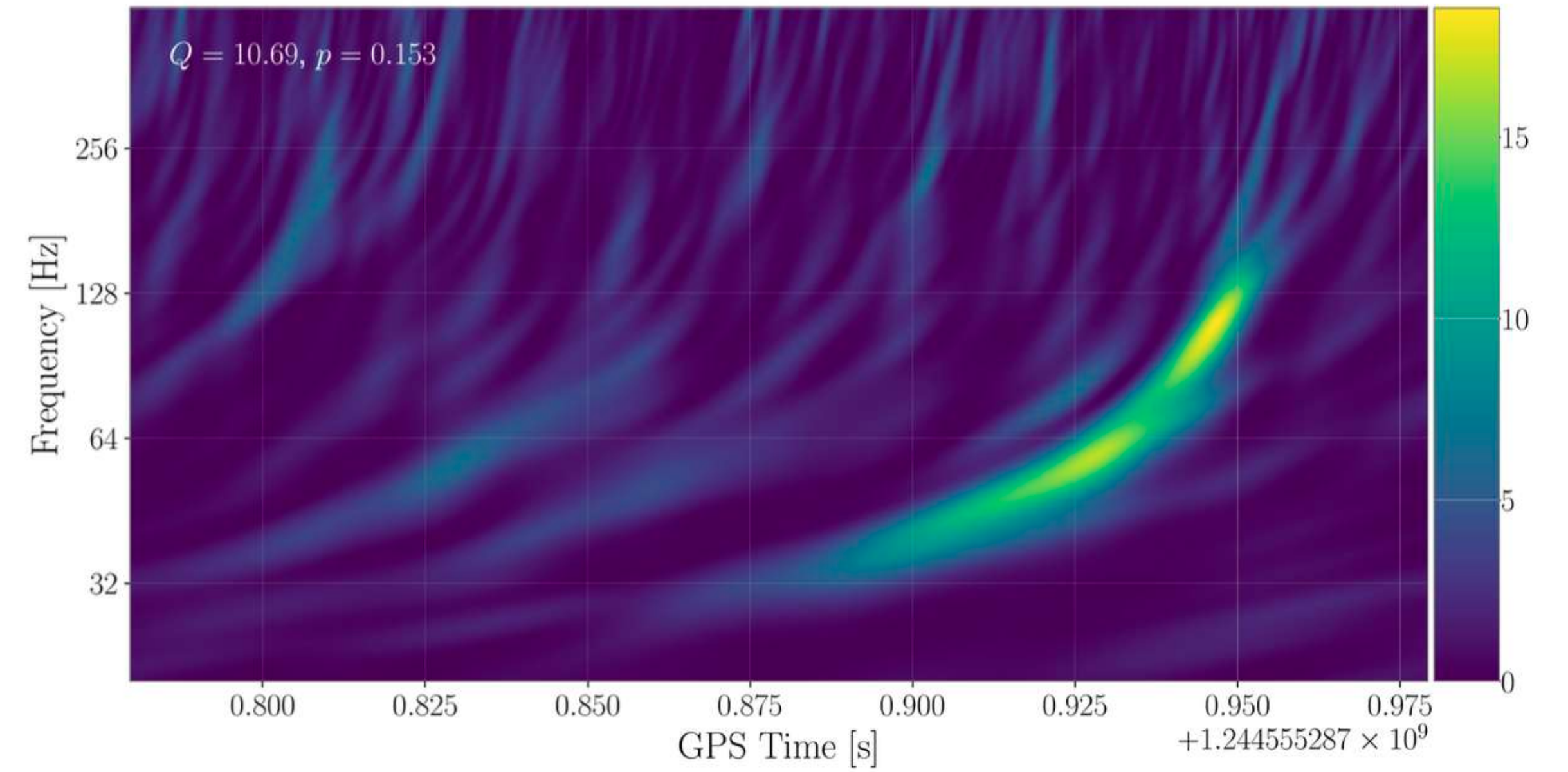
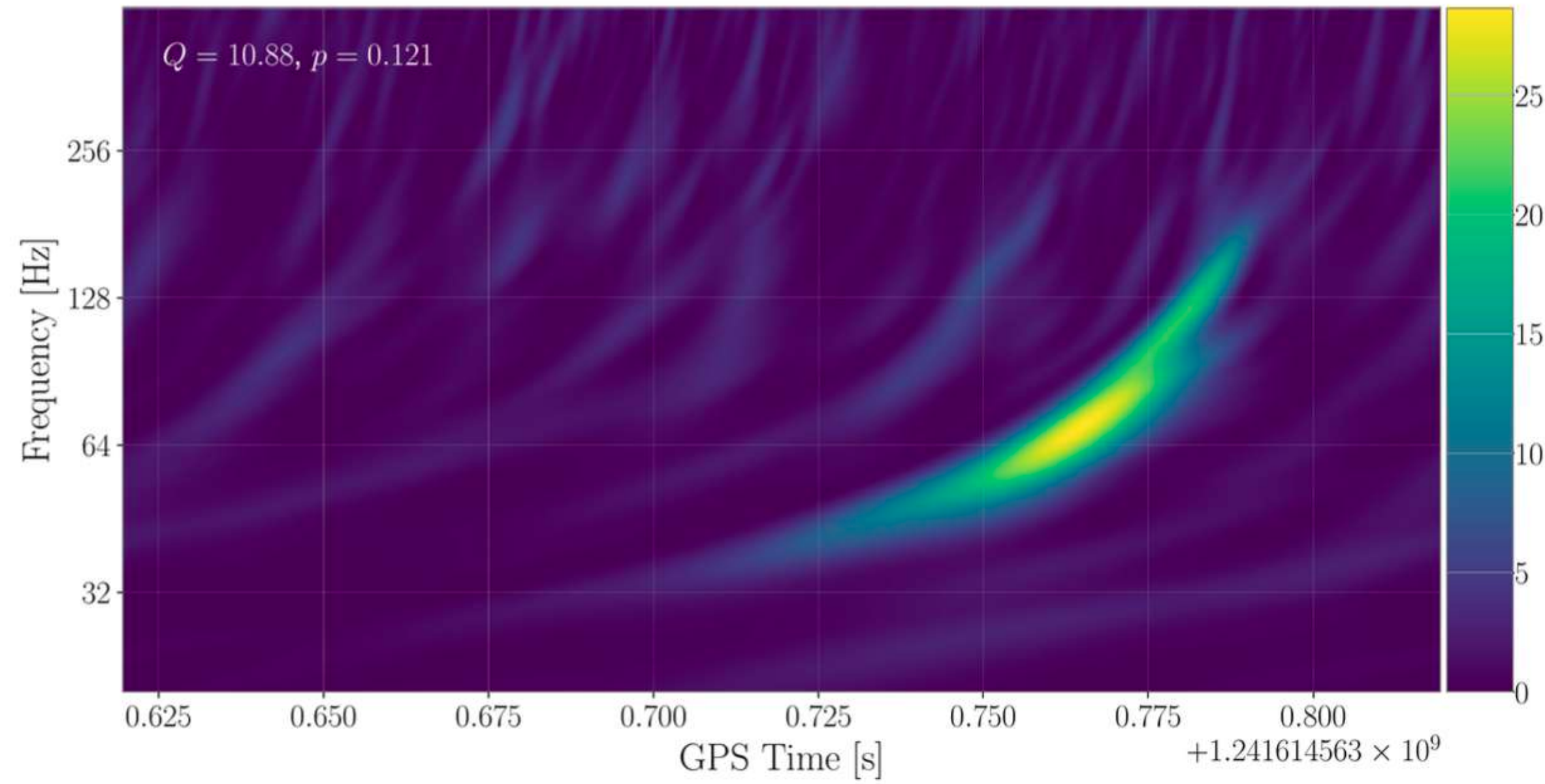


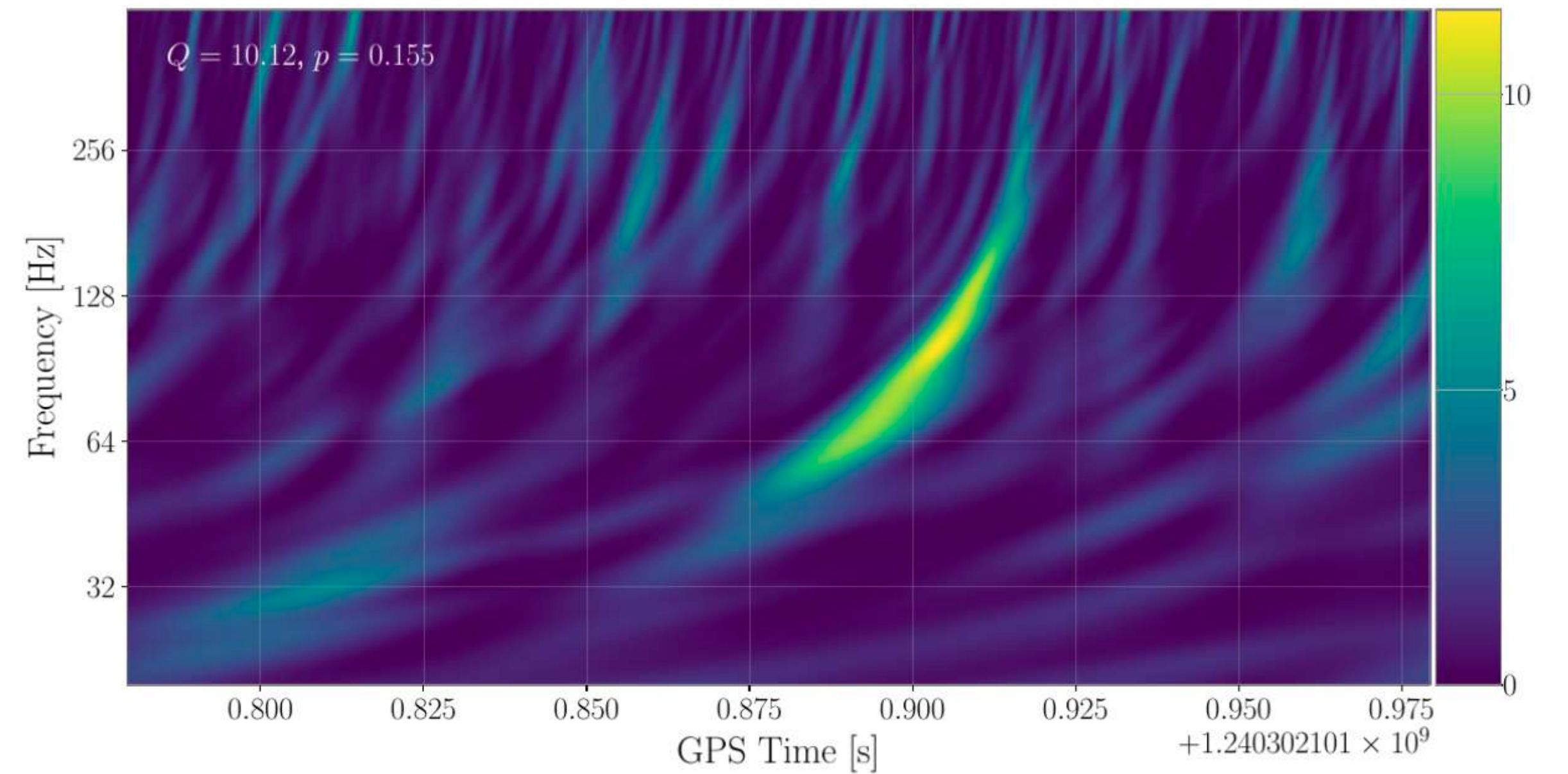
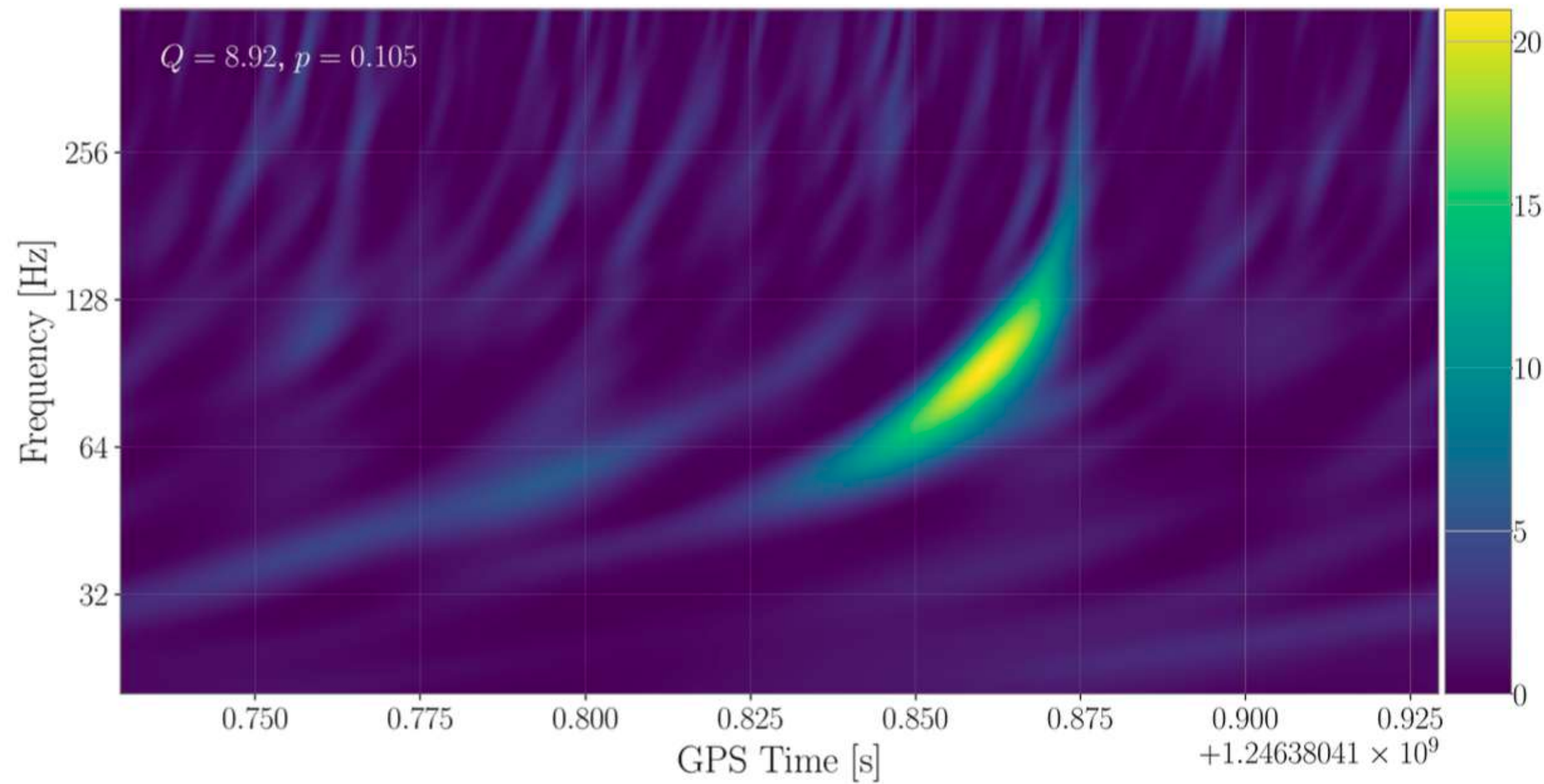
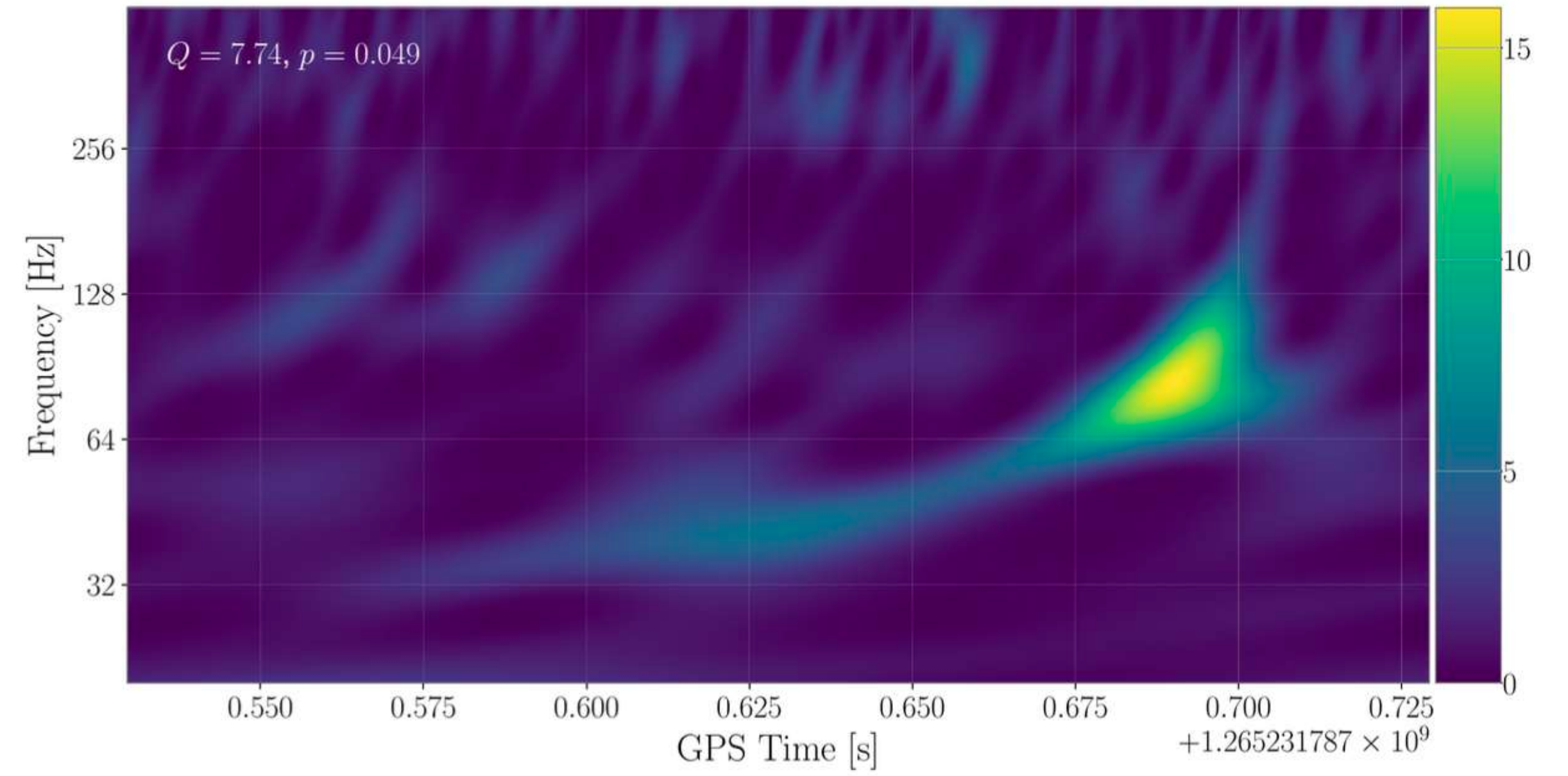
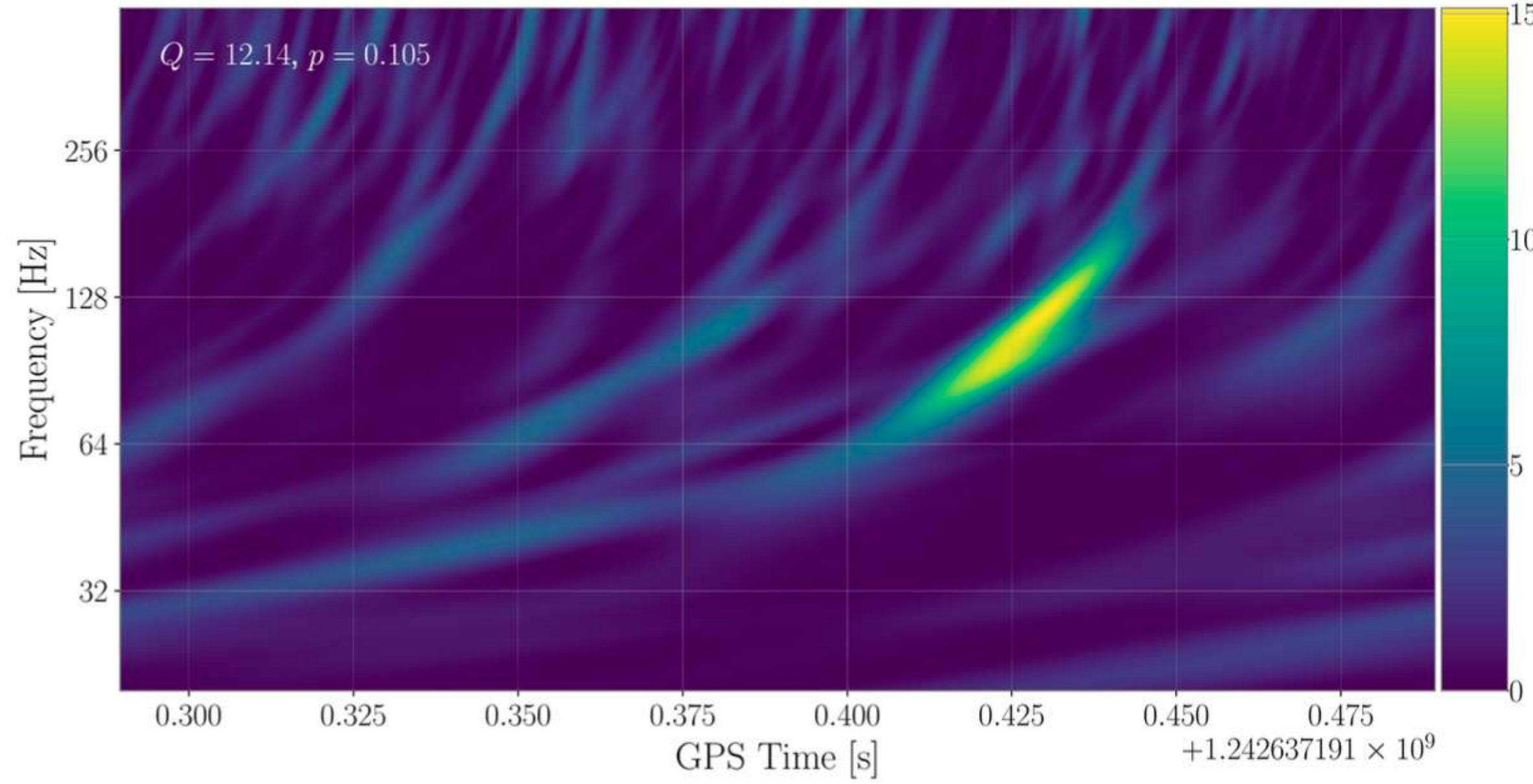
FIG. 38: Same as Fig. 35, but for the new event GW190904_104631.

Koloniari, Koursoumpa, Nousi, Lampropoulos, Passalis, Tefas, Stergioulas (2025)

ARESGW NEW CANDIDATE EVENTS



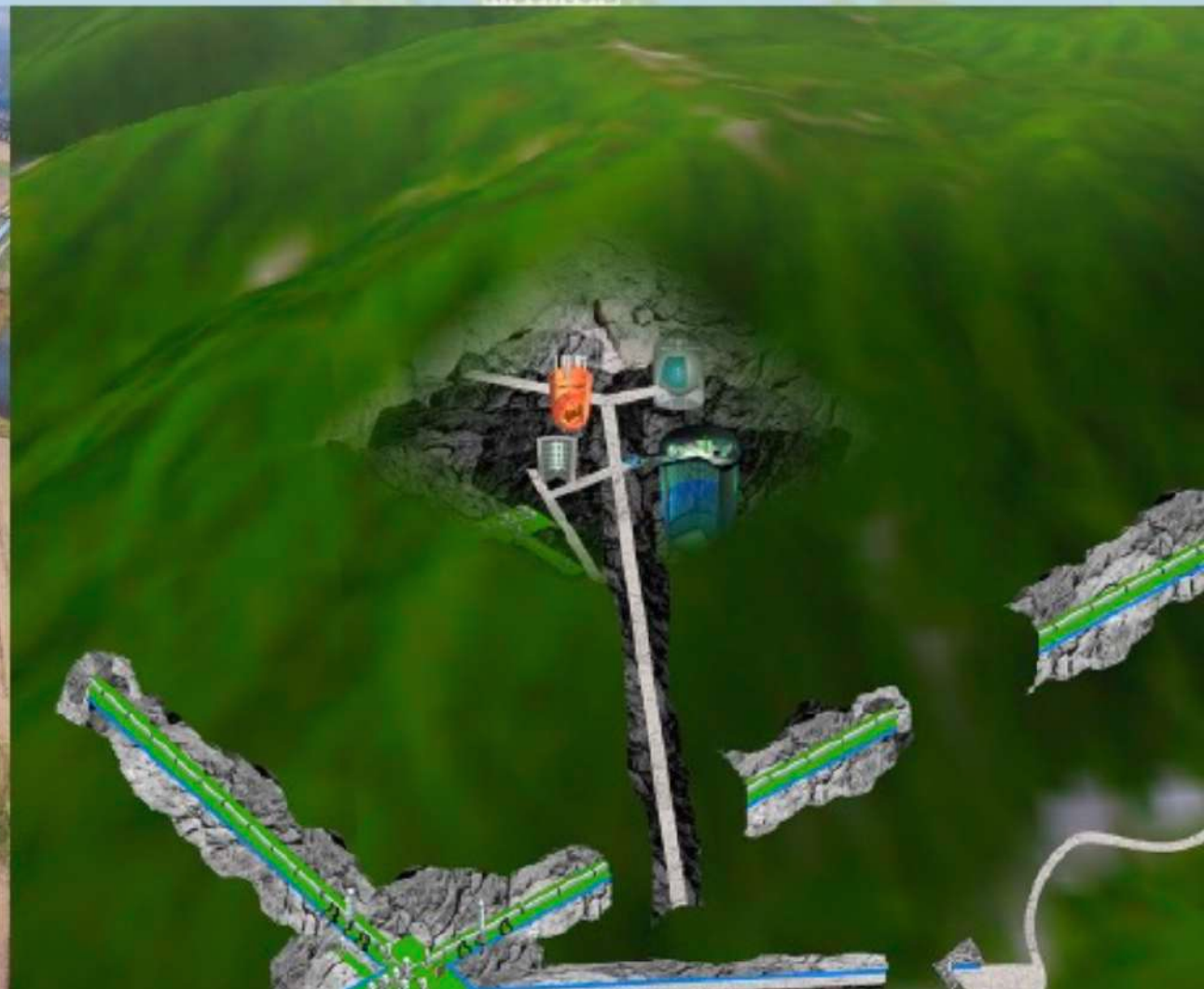
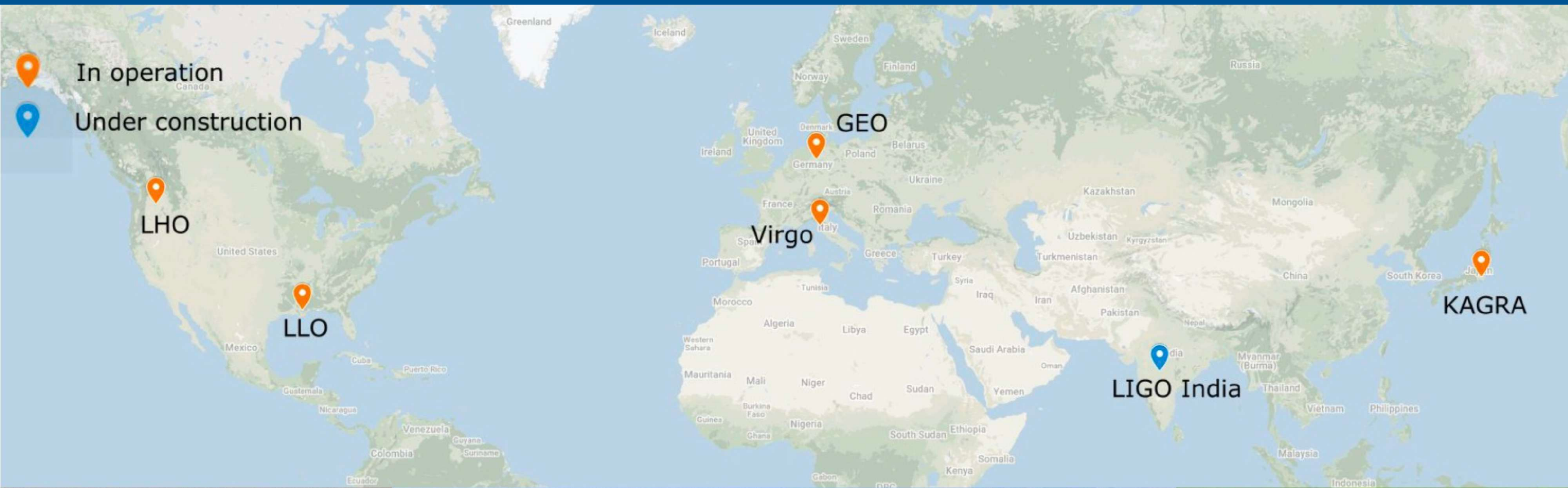
ARESGW NEW CANDIDATE EVENTS



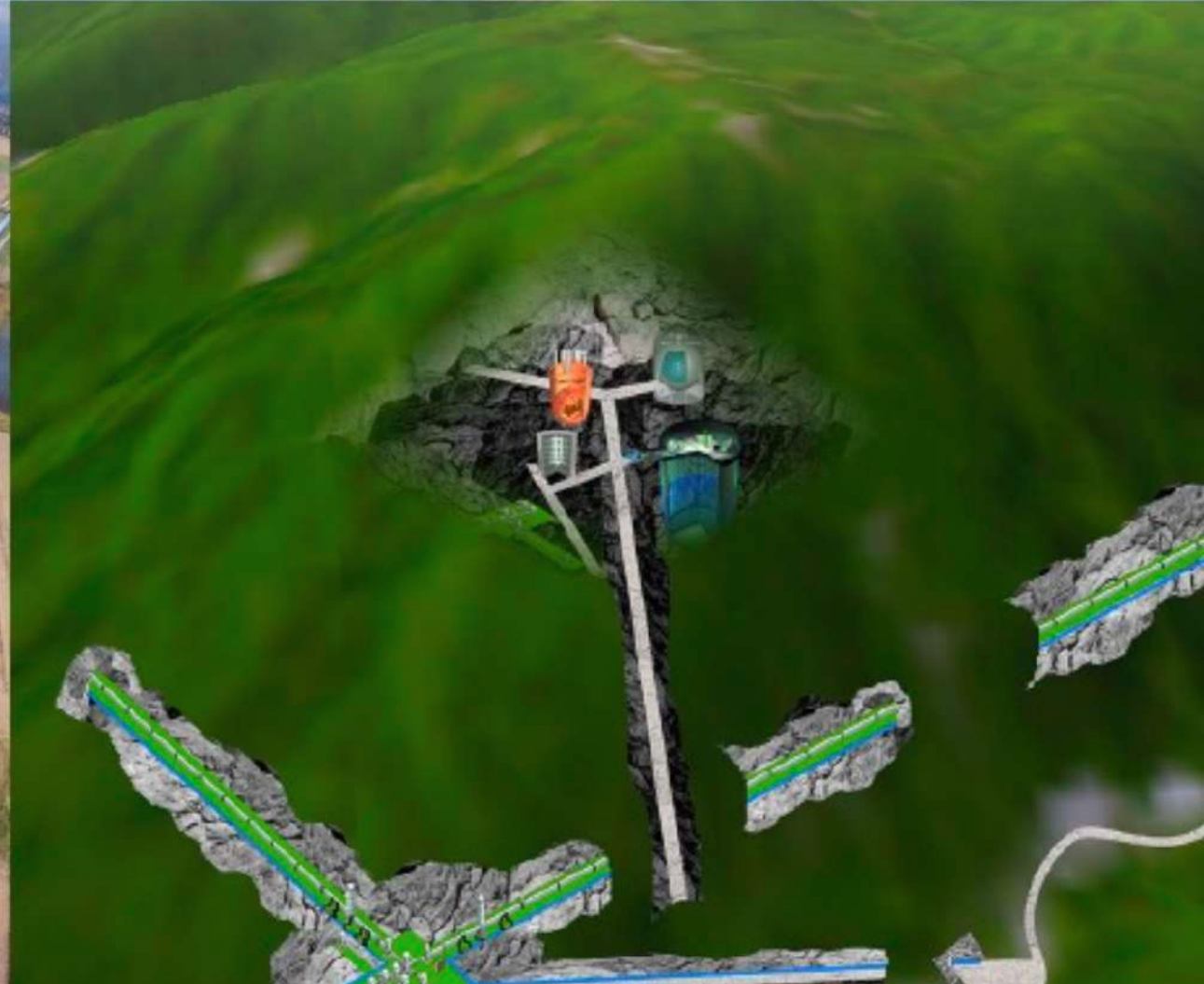
PART B.

BINARY NEUTRON STAR POST-MERGER PHASE

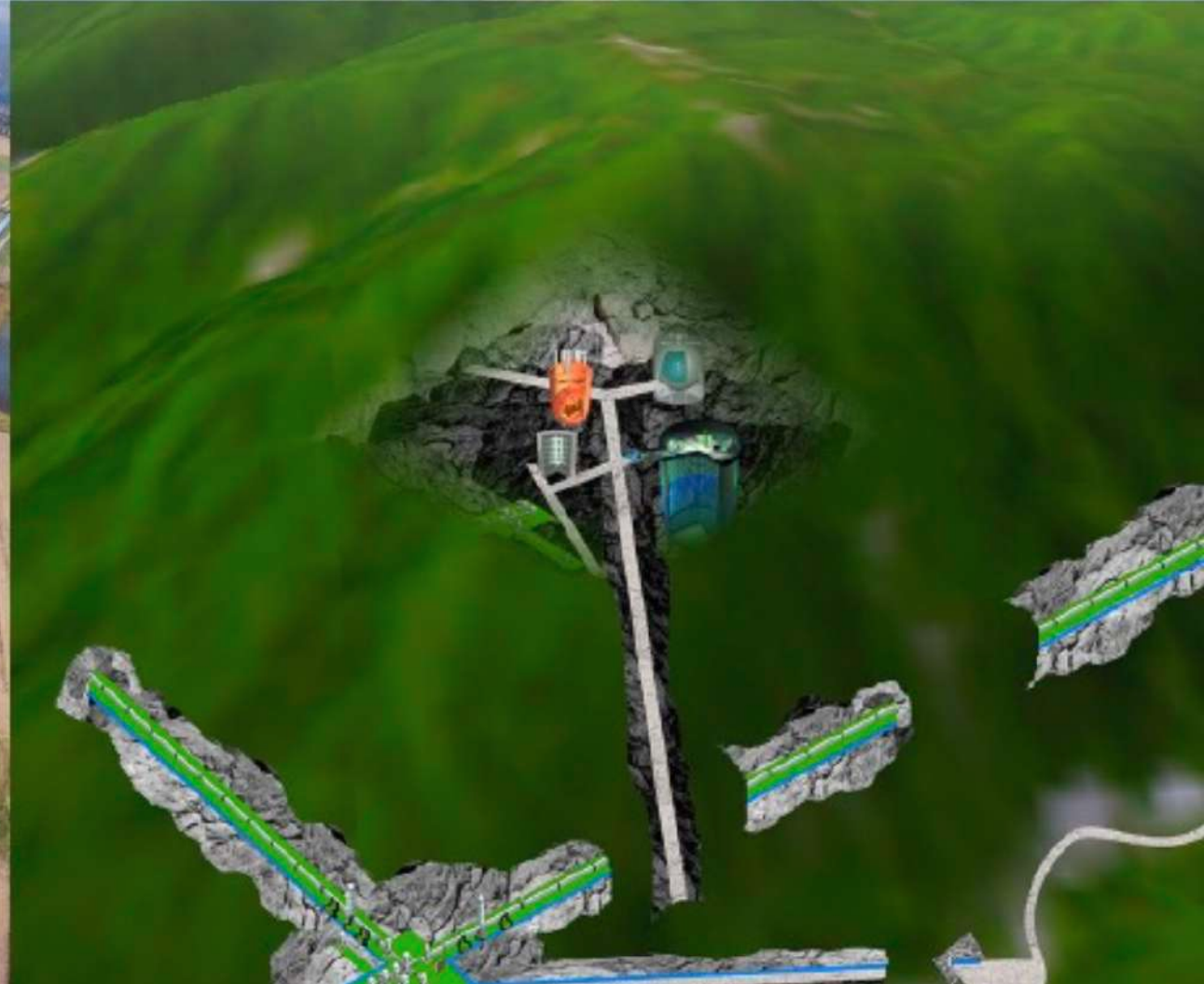
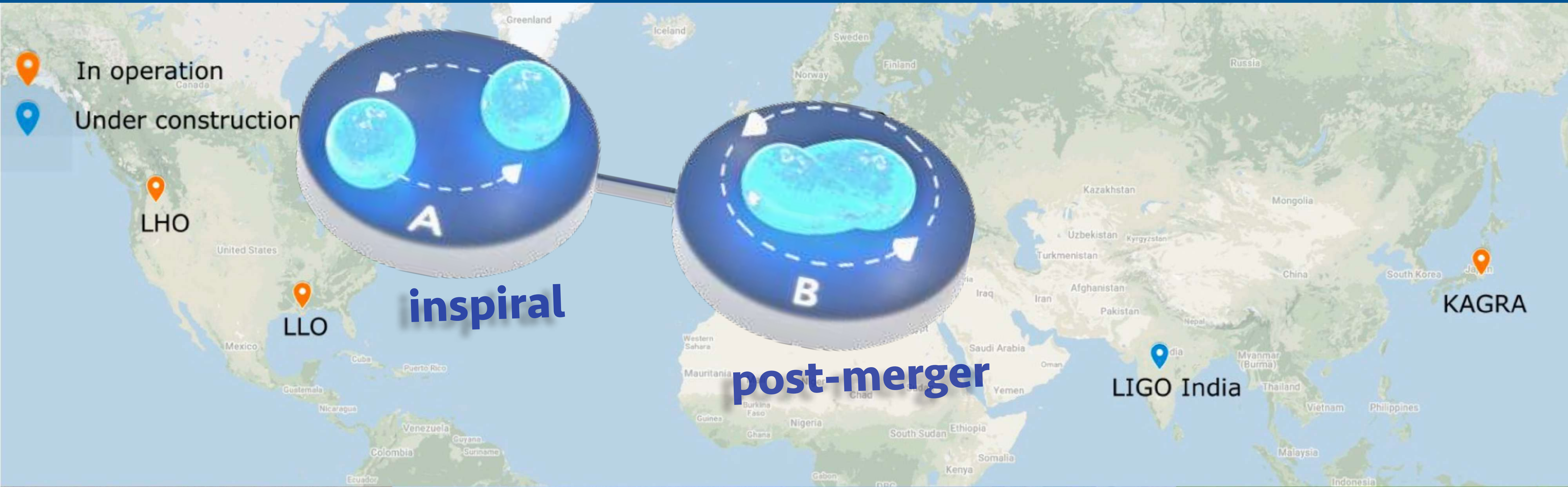
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



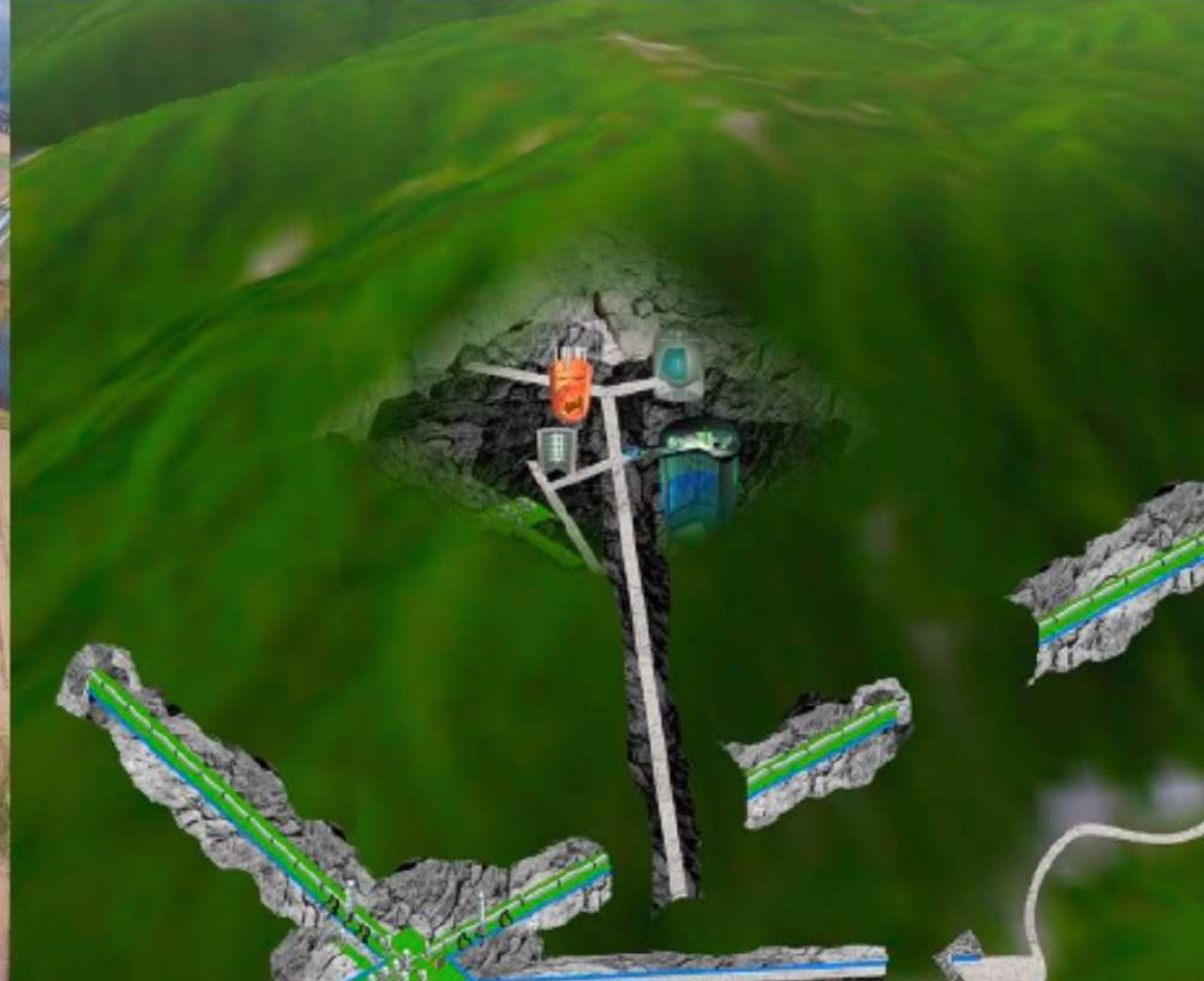
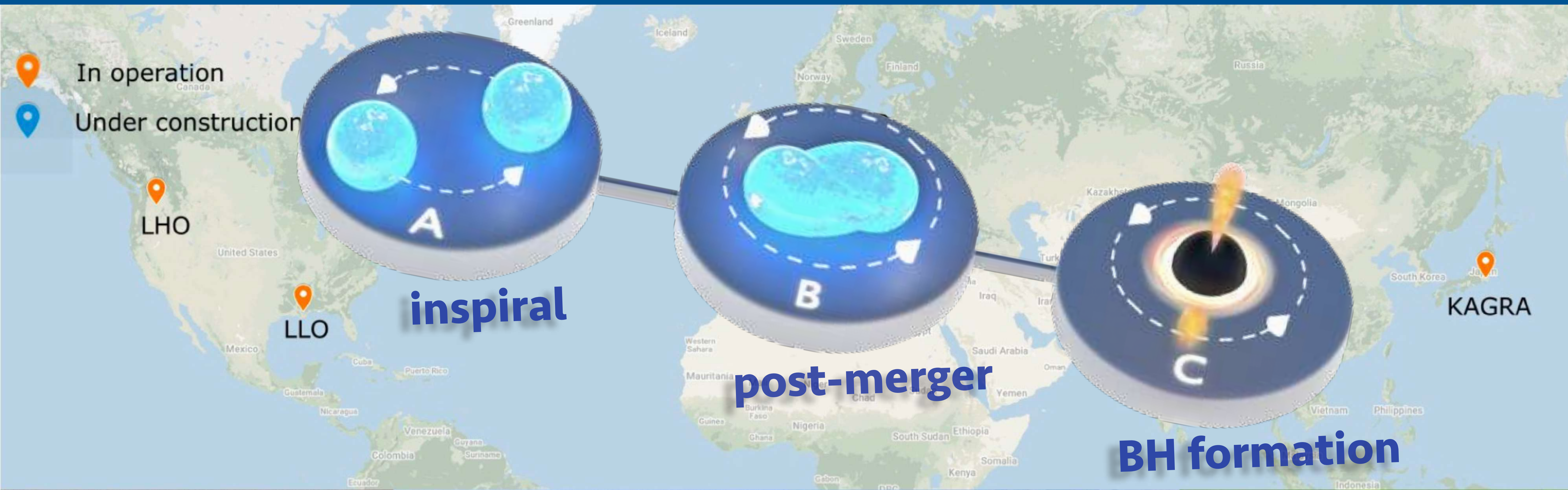
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)

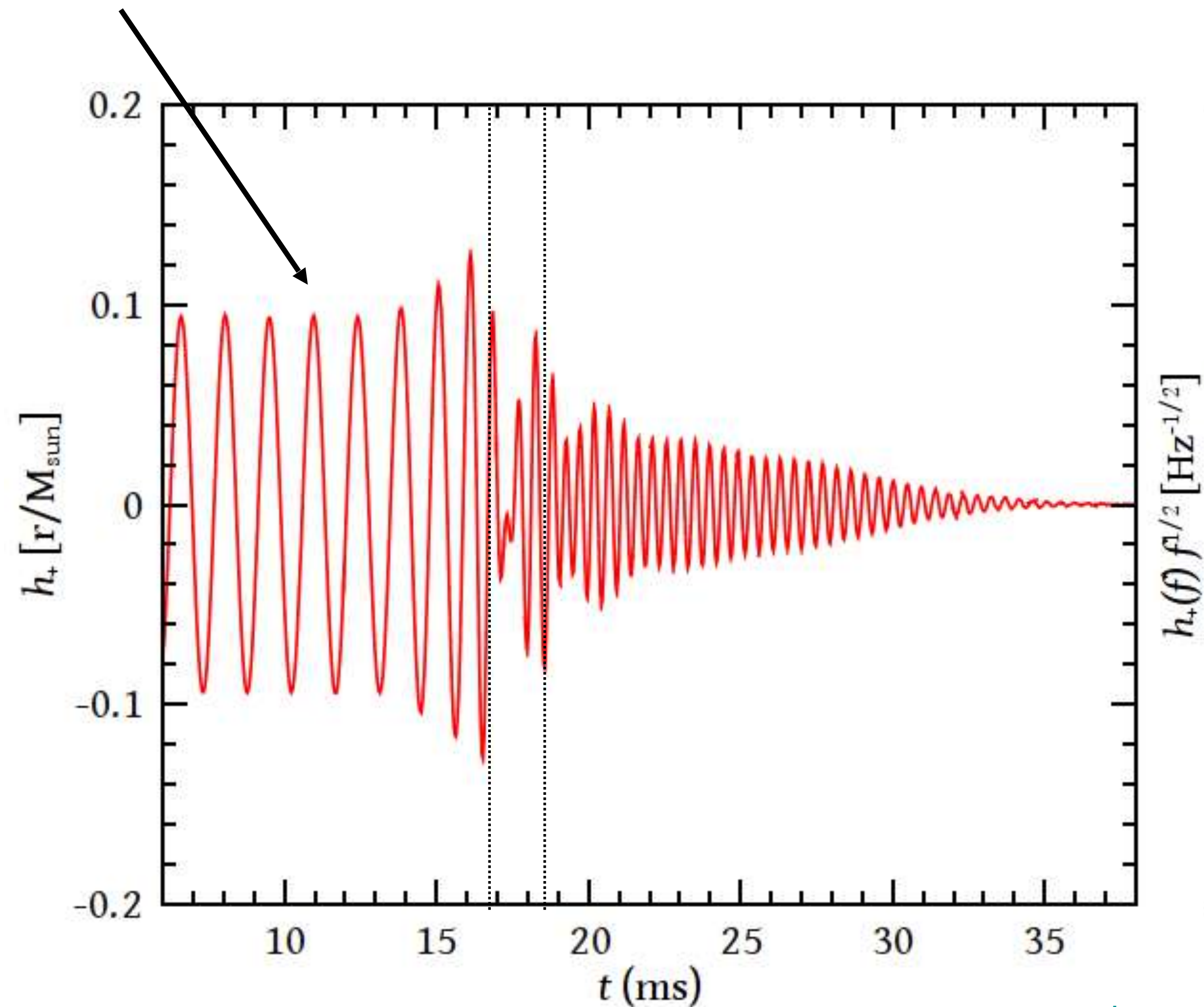


INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:
inspiral, *merger* and *post-merger oscillations*.

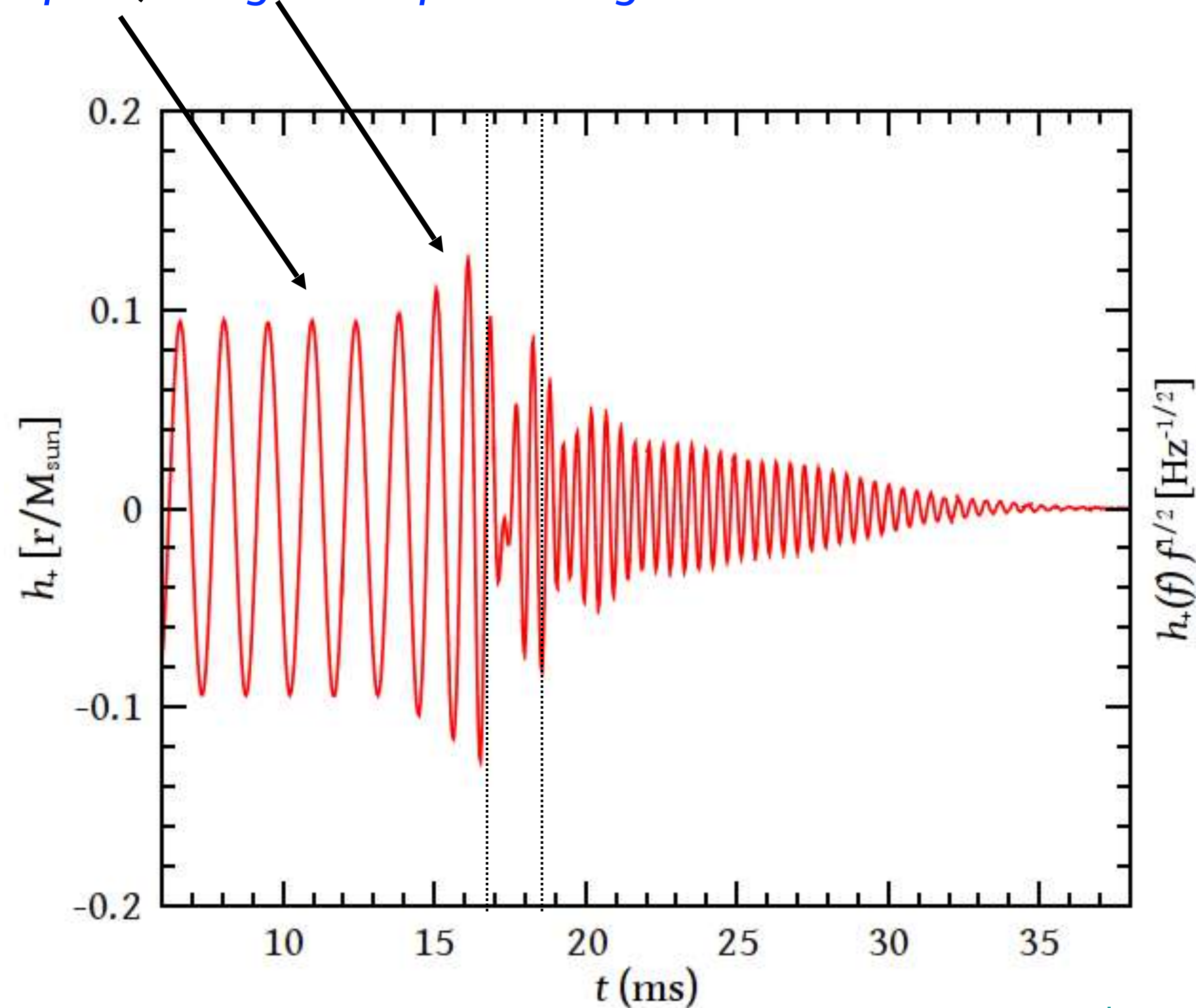


Stergioulas et al. (2011)

POST-MERGER PHASE IN BNS MERGERS

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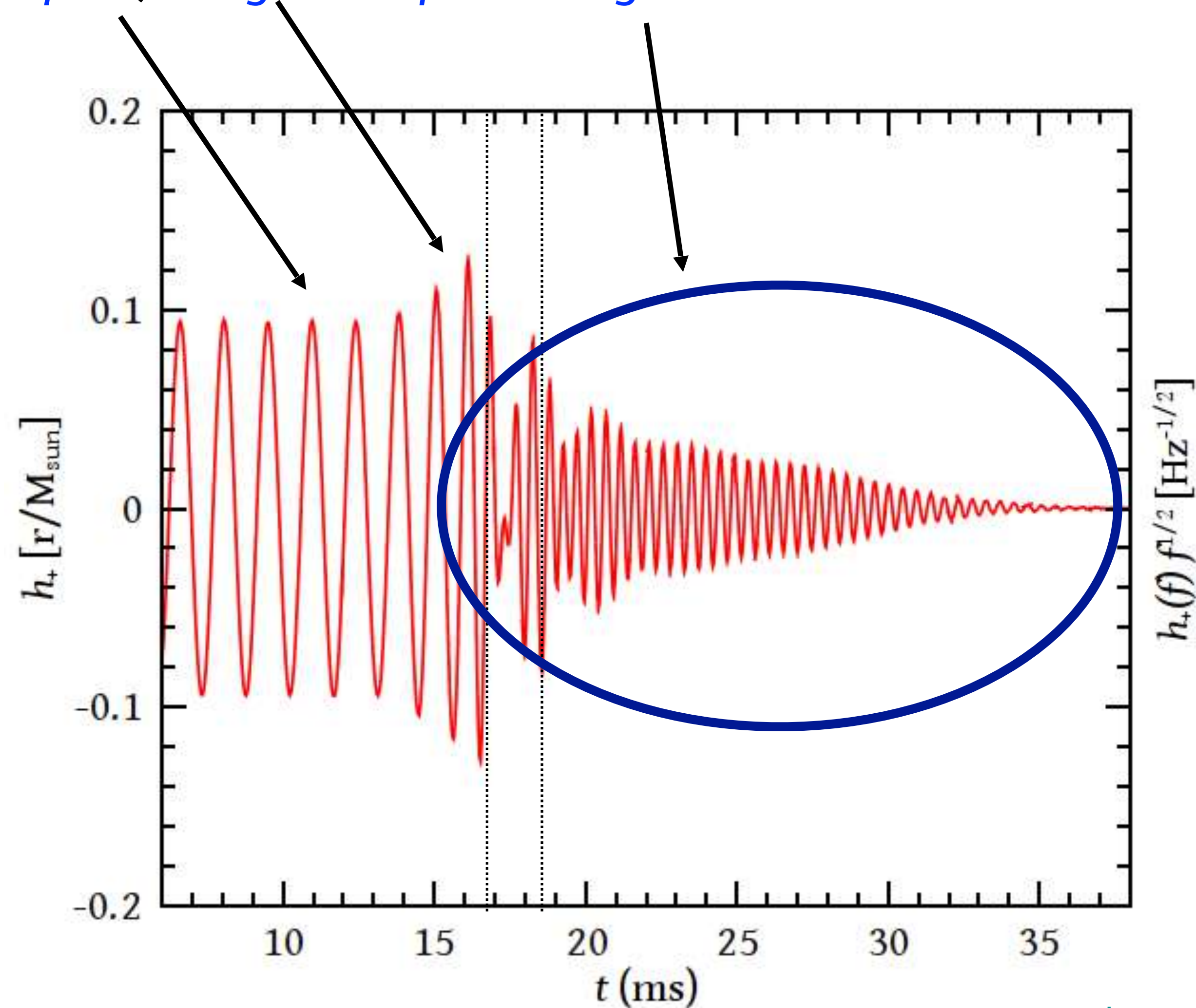


Stergioulas et al. (2011)

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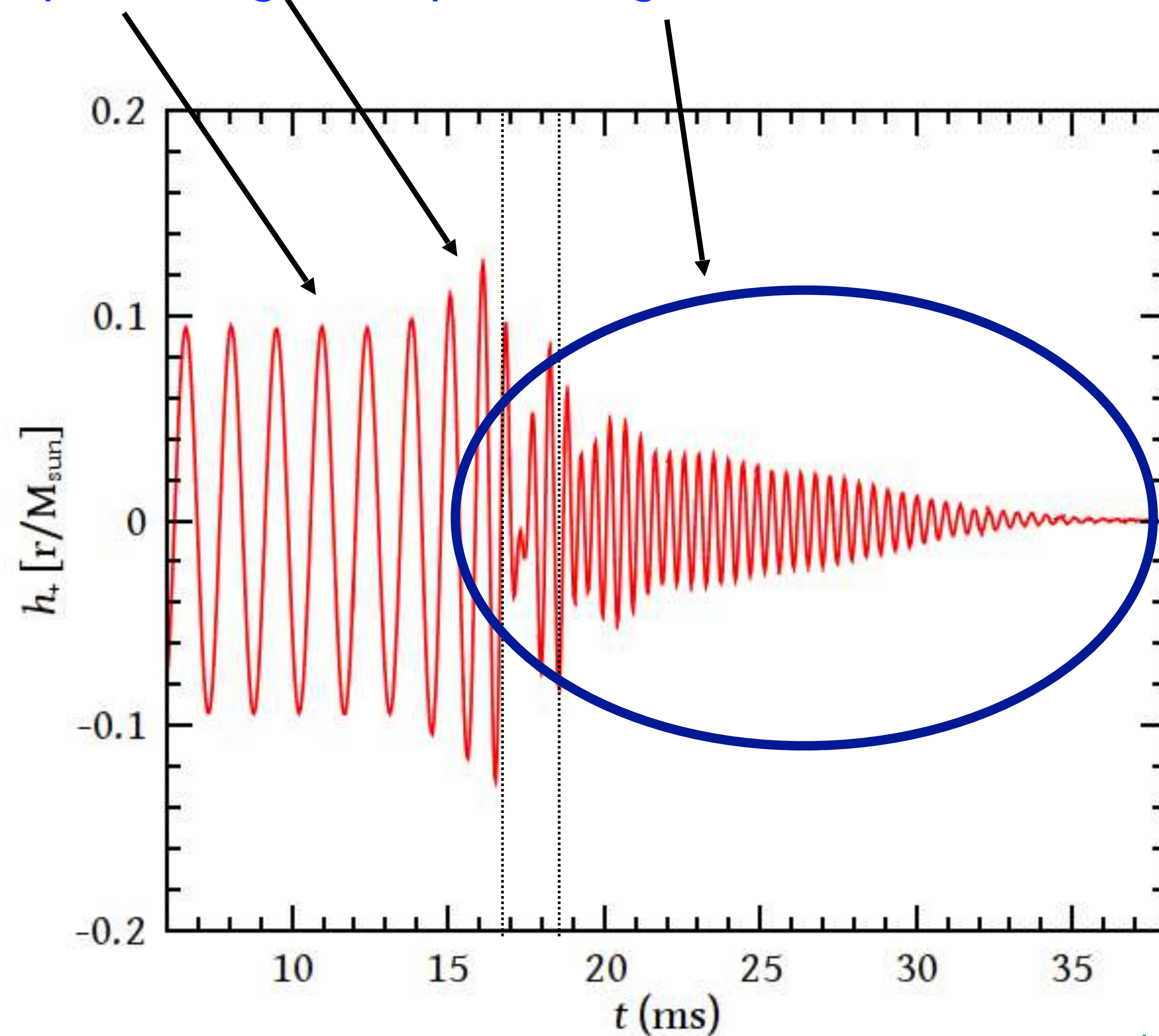


Stergioulas et al. (2011)

POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:

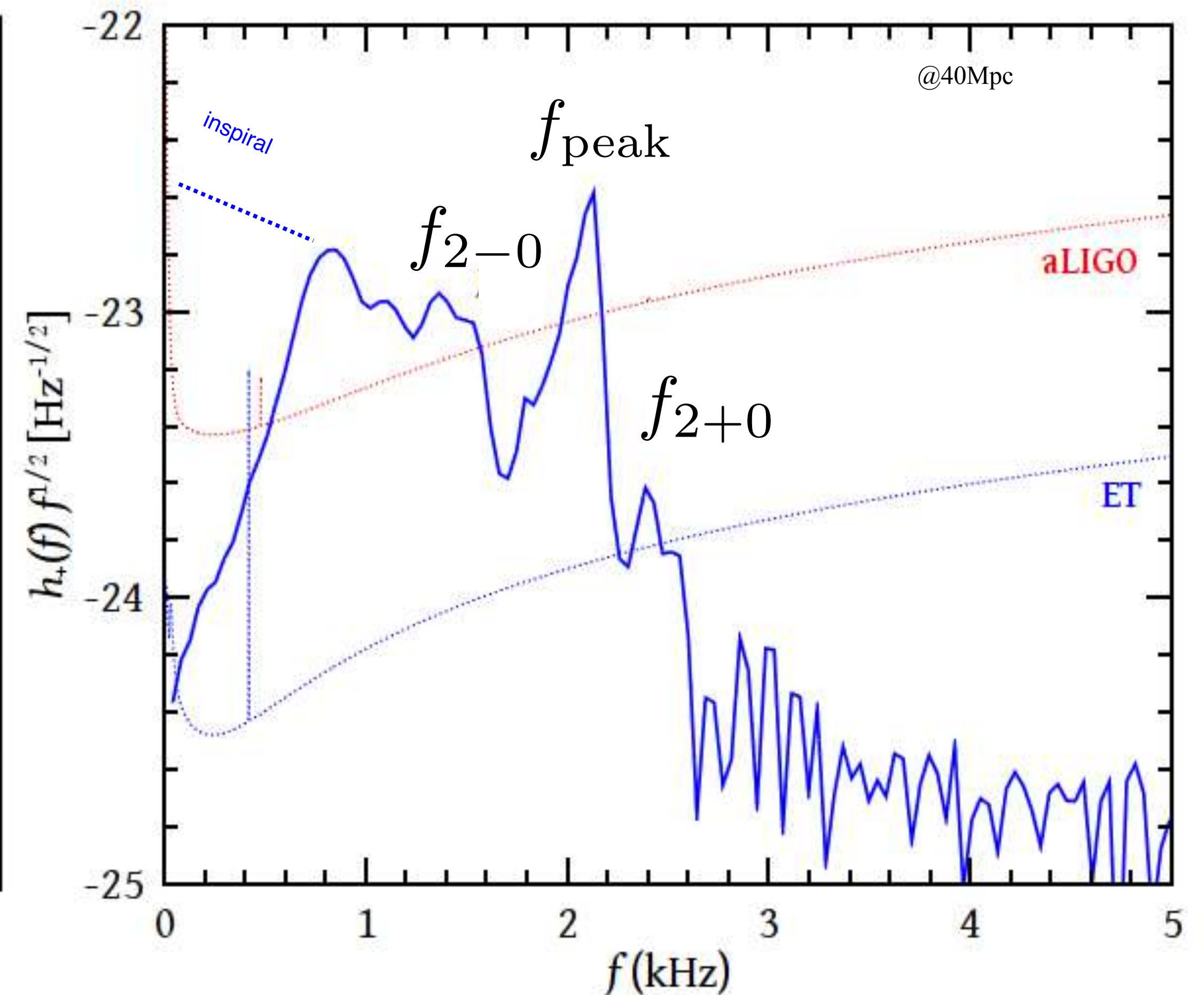
inspiral, *merger* and *post-merger oscillations*.



Frequency domain:

f_{peak} : $l=m=2$ fundamental mode.

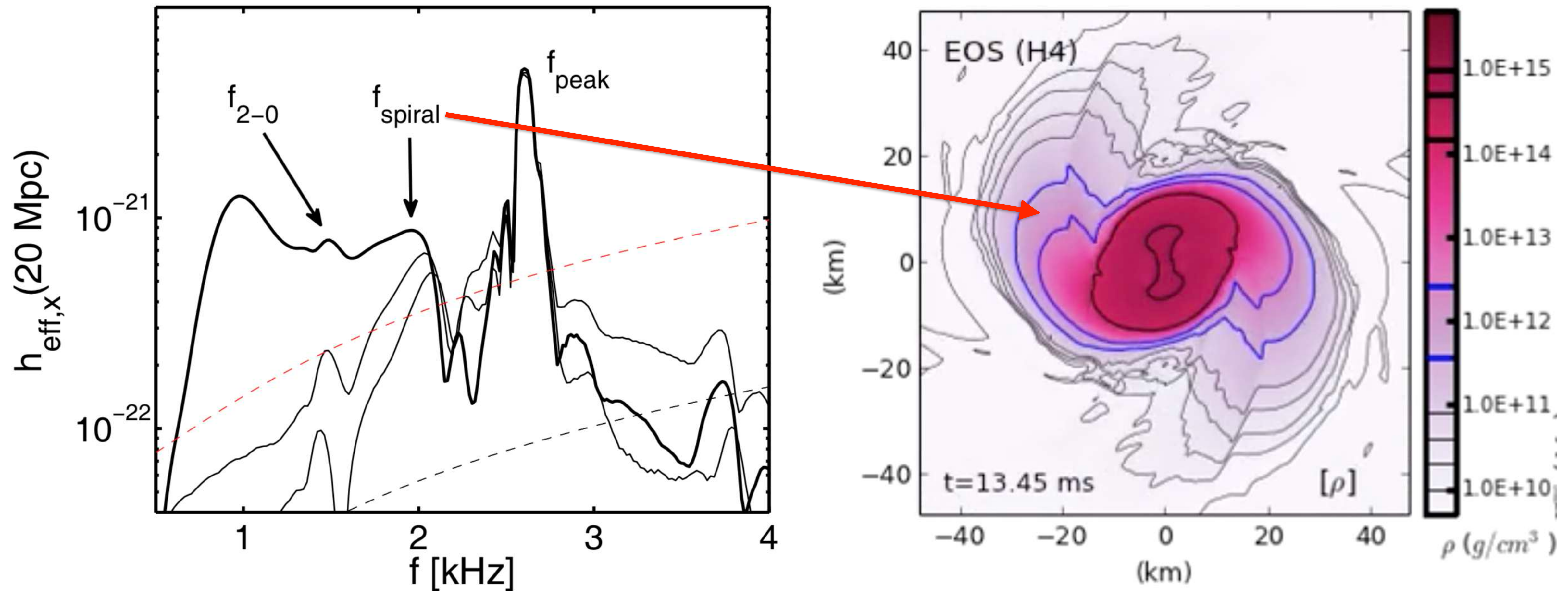
f_{2-0}, f_{2+0} : *nonlinear combination tones*



Stergioulas et al. (2011)

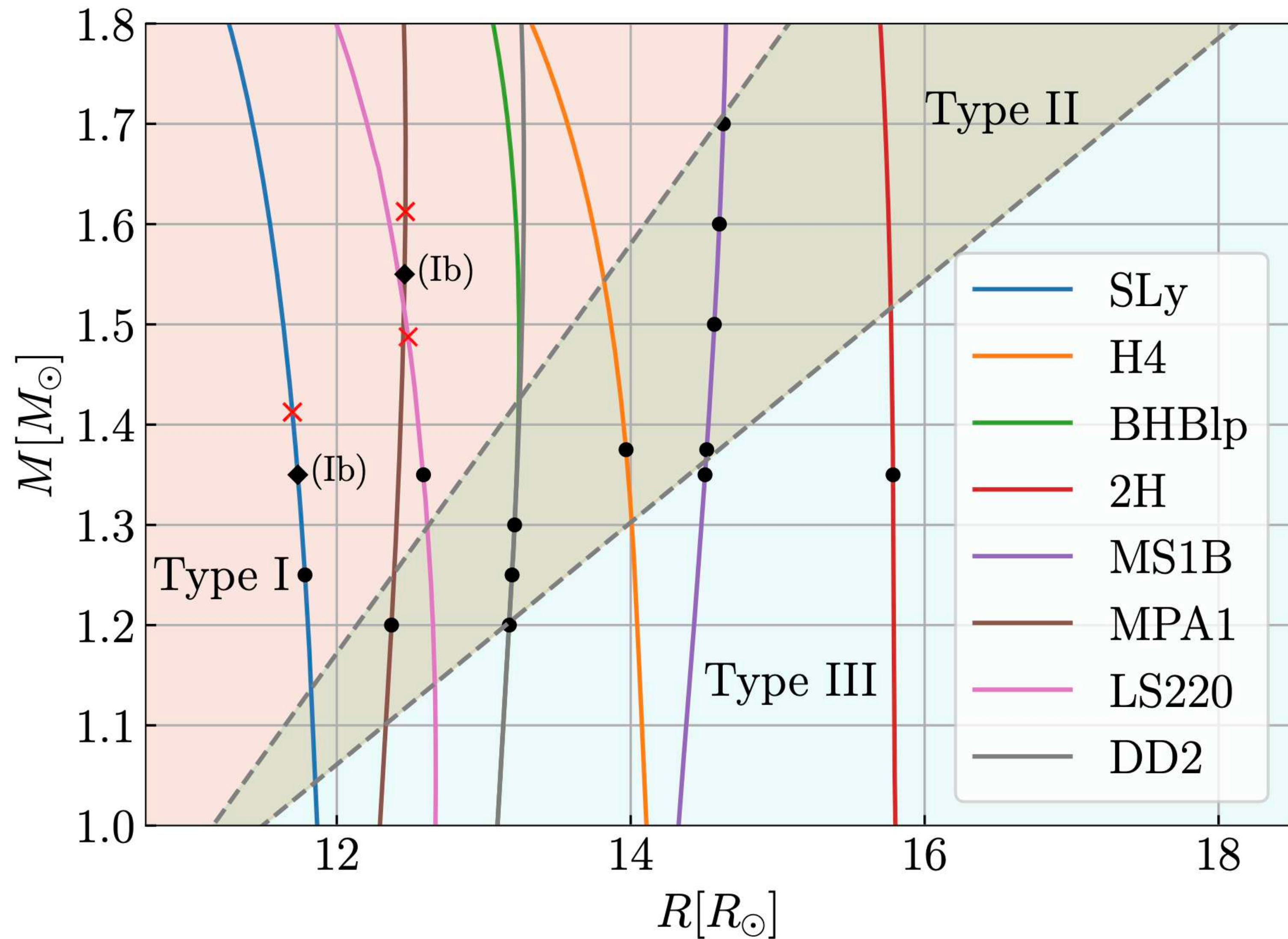
POST-MERGER PHASE IN BNS MERGERS

Orbiting spiral arms also lead to a distinct frequency f_{spiral}



Bauswein & Stergioulas (2015)

CLASSIFICATION OF POST-MERGER WAVEFORMS



Bauswein & Stergioulas (2015)

Vretinaris, Bauswein & Stergioulas (2020)

Type I:

f_{2-0} stronger than f_{spiral}

Type II:

f_{2-0} comparable to f_{spiral}

Type III:

f_{spiral} stronger than f_{2-0}

Type Ib:

(close to M_{thres})

Vretinaris et al. (2025)

EMPIRICAL RELATIONS OF POST-MERGER FREQUENCIES

$$f_{\text{peak}} M_{\text{chirp}} = 1.392 - 0.108 M_{\text{chirp}} + 51.70 \tilde{\Lambda}^{-1/2}$$

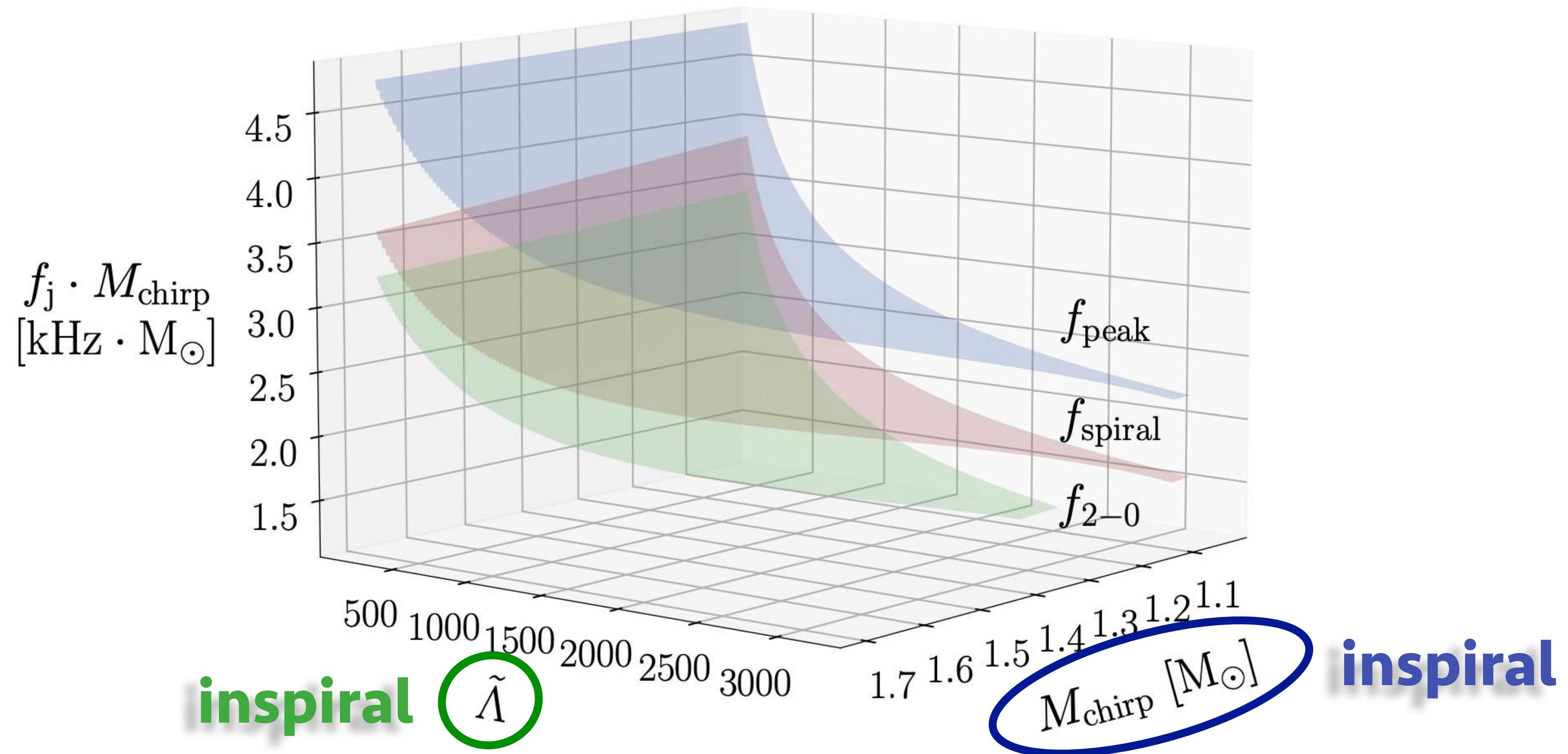
Vretinaris, Bauswein & Stergioulas (2020)

$$f_{2-0} M_{\text{chirp}} = 0.558 - 0.406 M_{\text{chirp}} + 48.696 \tilde{\Lambda}^{-1/2}$$

Vretinaris et al. (2025)

$$f_{\text{spiral}} M_{\text{chirp}} = 1.2 - 0.442 M_{\text{chirp}} + 45.819 \tilde{\Lambda}^{-1/2}$$

Vretinaris et al. (2025)



EMPIRICAL RELATIONS OF POST-MERGER FREQUENCIES

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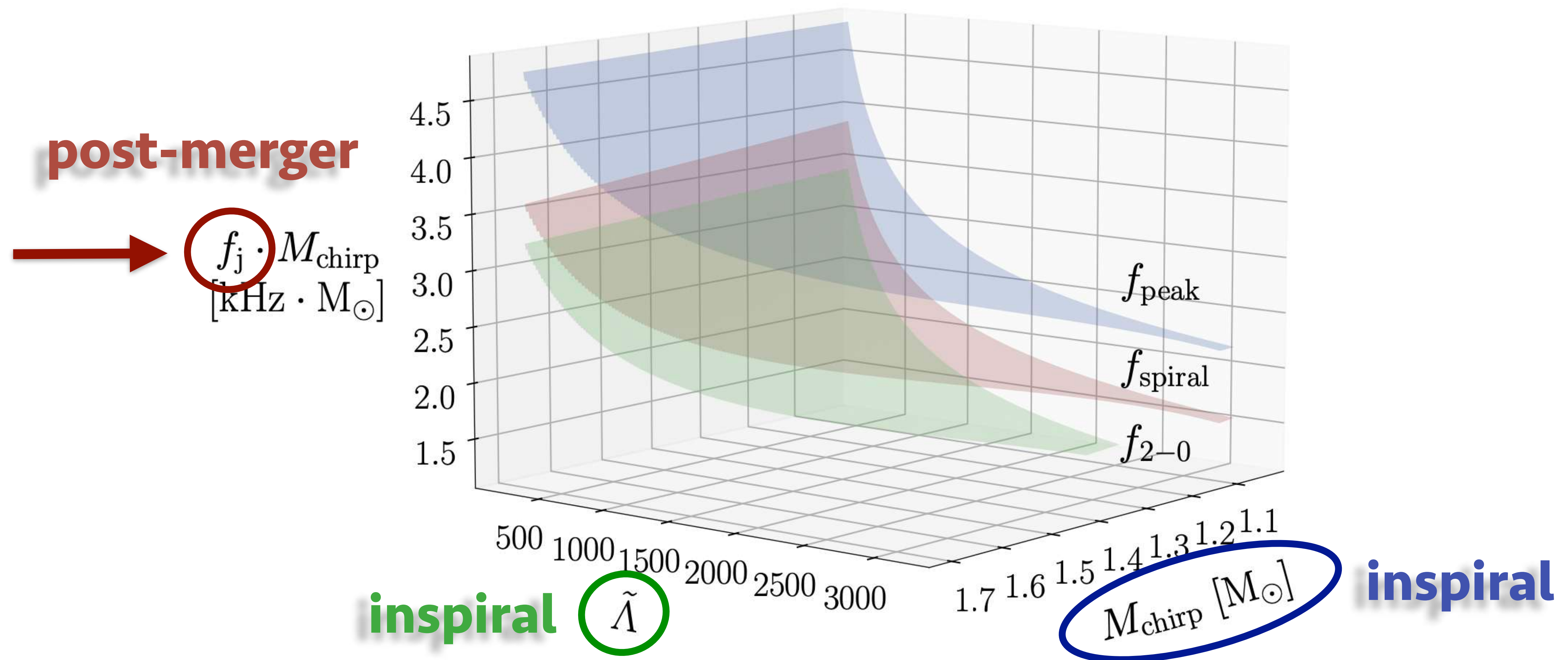
Vretinaris, Bauswein & Stergioulas (2020)

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Vretinaris et al. (2025)

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Vretinaris et al. (2025)



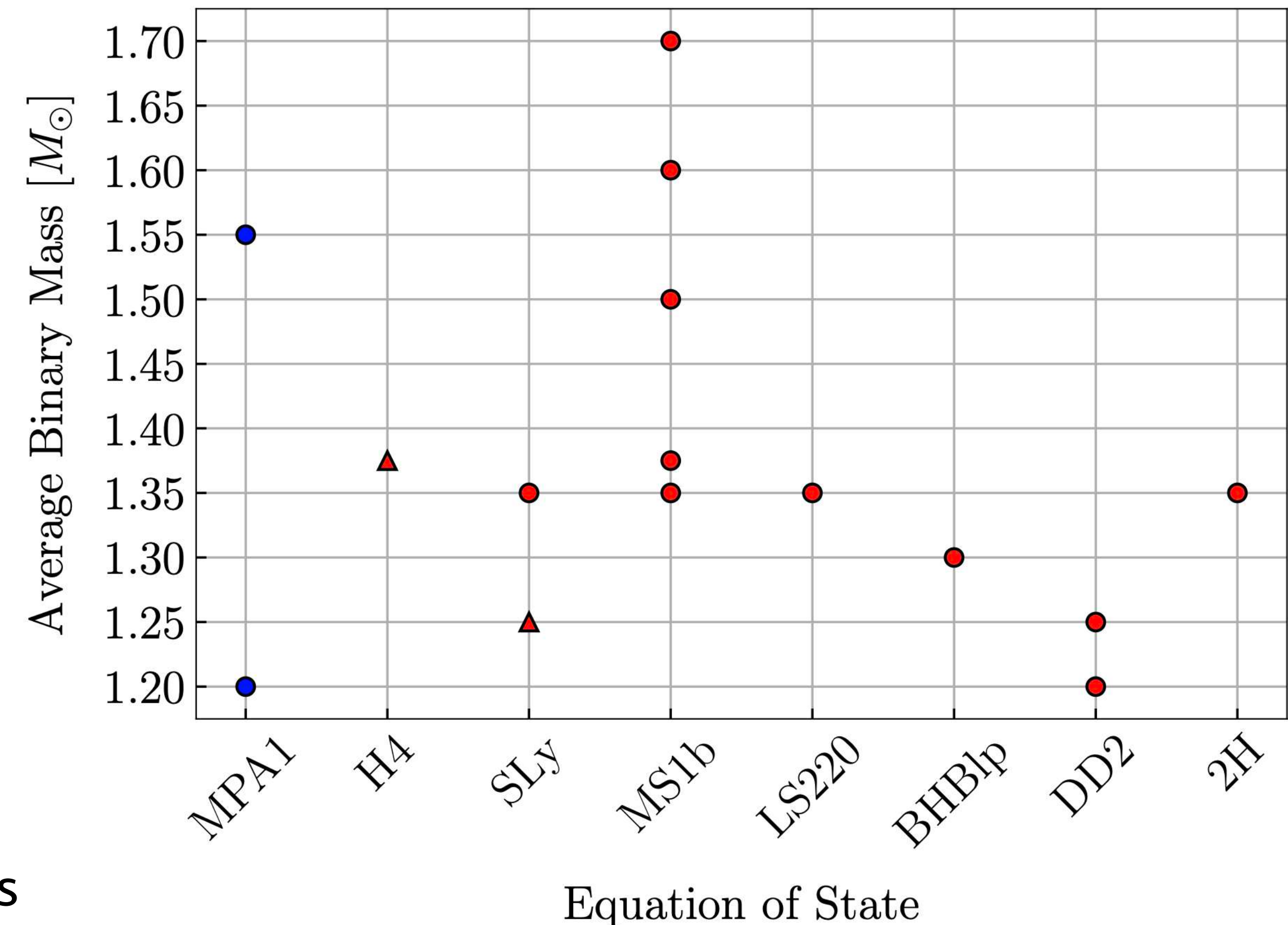
ACCELERATION OF POST-MERGER INFERENCE

13 numerical waveforms from the CoRe database (Gonzalez et al. 2022)

+2 numerical waveforms from Souldanis, Bauswein & Stergioulas (2022)

Label	EOS	q	(Average) Mass	References
THC:0036:R03	SLy	1.0	1.350	[47]
THC:0019:R05	LS220	1.0	1.350	[101, 102]
BAM:0088:R01	MS1b	1.0	1.500	[99, 100]
THC:0002:R01	BHBlp	1.0	1.300	[101, 102]
THC:0011:R01	DD2	1.0	1.250	[101, 102]
BAM:0070:R01	MS1b	1.0	1.375	[103]
BAM:0065:R03	MS1b	1.0	1.350	[104]
THC:0010:R01	DD2	1.0	1.200	[101, 102]
BAM:0002:R02	2H	1.0	1.350	[104]
BAM:0053:R01	H4	1.5	1.375	[105]
BAM:0124:R01	SLy	1.5	1.250	[103]
BAM:0090:R02	MS1b	1.0	1.600	[99, 100]
BAM:0092:R02	MS1b	1.0	1.700	[99, 100]
Souldanis et al.	MPA1	1.0	1.200	[67]
Souldanis et al.	MPA1	1.0	1.550	[67]

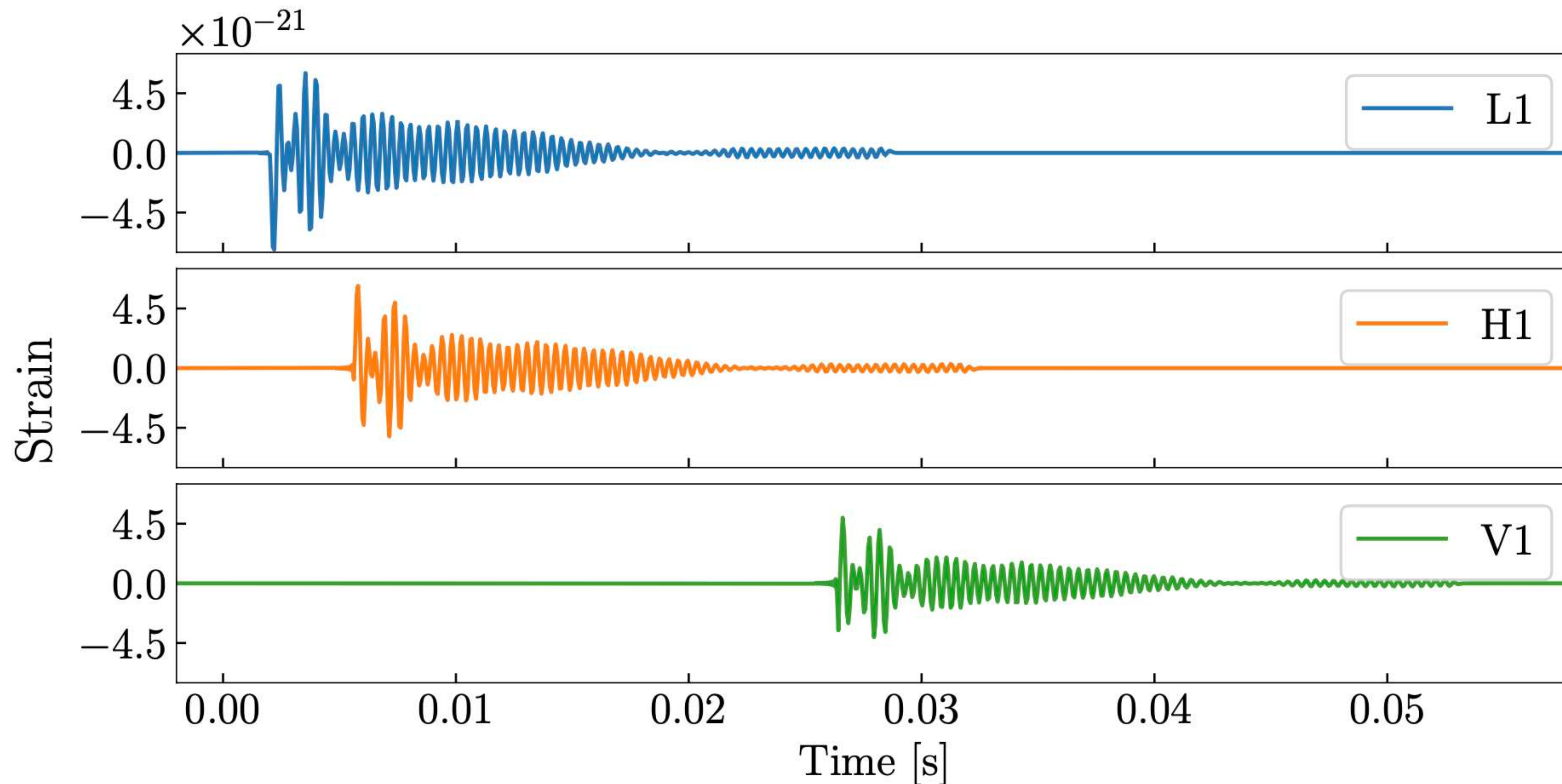
Extension of the set of 9 waveforms used in previous work by Easter et al. (2020)



INJECTIONS IN 3-DETECTOR NETWORK

Waveforms are injected in 3-detector HLV network at design sensitivity, using BILBY (Ashton et al. 2019)

We choose post-merger SNR of 8, 16 and 50, to simulate detection by 3G network (ET/CE) at distances as close as 200Mpc.



Several analytic models exist in the time- and frequency-domains.

Here, we extend the analytic model of Easter et al. (2020) as follows:

$$\begin{aligned} h(\boldsymbol{\theta}, t) &= h_+(\boldsymbol{\theta}, t) - ih_\times(\boldsymbol{\theta}, t) \\ &= \sum_{j=1}^4 [h_{j,+}(\boldsymbol{\theta}, t) - ih_{j,\times}(\boldsymbol{\theta}, t)] \\ h_{j,+}(\boldsymbol{\theta}, t) &= A_j \exp \left[-\frac{t}{T_j} \right] \cos [2\pi f_j t (1 + a_j t) + \psi_j] \end{aligned}$$

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Intrinsic parameters

$$\boldsymbol{\theta} = \{A_j, T_j, f_j, a_j, \psi_j\} \quad \text{for } j \in [1, 4]$$

$h_{j,\times}(\boldsymbol{\theta}, t)$ is obtained by applying a $\pi/2$ phase shift to $h_{j,+}(\boldsymbol{\theta}, t)$

- We have added a 4th oscillator at high frequencies $> f_{\text{peak}}$ (e.g. f_{2+0})
- Amplitudes A_j are free parameters

INFORMED PRIORS

In Easter et al. (2020) flat priors in a wide frequency range of 1-5 kHz for every oscillator were used.

- Here, we take advantage of the [empirical relations](#) to set [Gaussian priors](#) in a [narrow frequency range](#) around each expected frequency.
- In addition, the priors [differ](#), according to the [type of the post-merger](#) waveform:
 - Type I: Gaussian priors, $\mathcal{N}(f_{2-0}, \sigma^2)$ for f_{2-0} and uniform priors $\mathcal{U}(1, 5)$ [kHz] for f_{spiral} .
 - Type II: Gaussian priors, $\mathcal{N}(f_{2-0}, \sigma^2)$ for f_{2-0} and $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$ for f_{spiral} .
 - Type III: Gaussian priors, $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$ for f_{spiral} and uniform priors $\mathcal{U}(1, 5)$ [kHz] for f_{2-0} .

where $\sigma = 3 \times \text{max error of empirical relations}$. For f_{peak} : Gaussian ; for f_4 : flat in $[f_{\text{peak}} + 0.3\text{kHz}, 5\text{kHz}]$.

priors for A_j : uniform in $[-24, -19]$

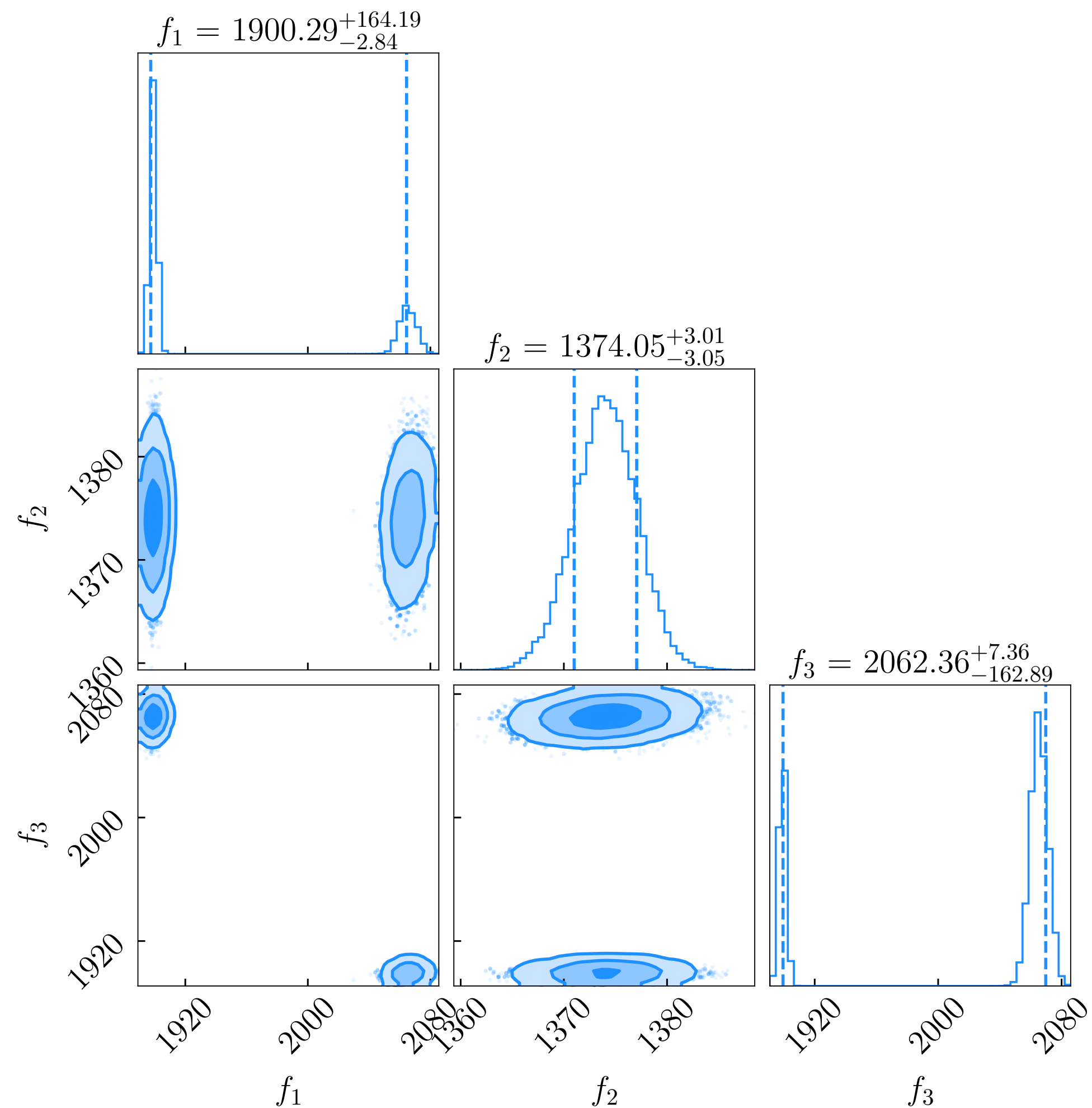
priors for a_j : uniform in $[-6.4, 6.4]$

priors for remaining parameters: as in Easter et al. (2020)

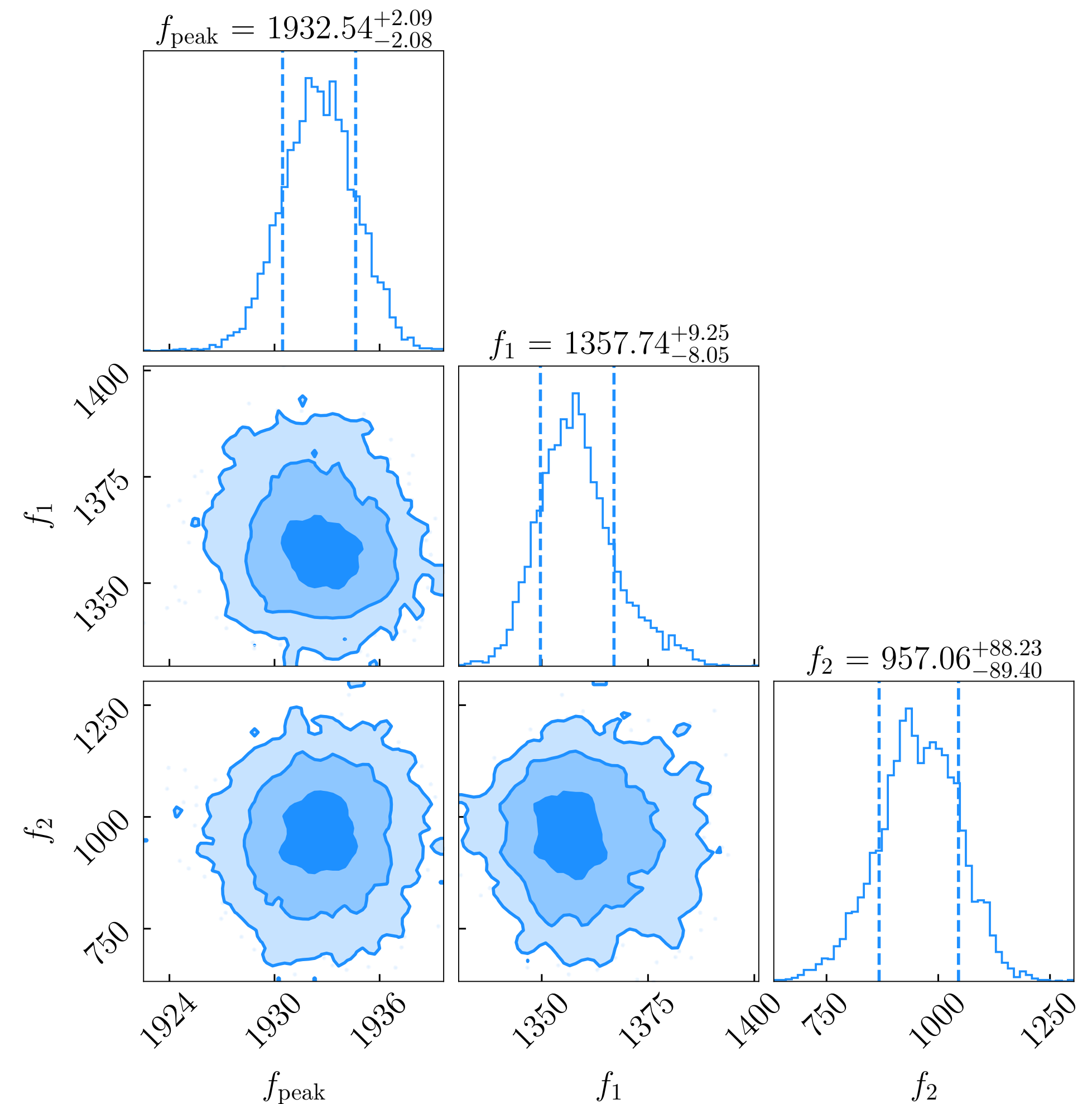
POSTERIOR DISTRIBUTIONS

EOS 2H 1.35+1.35, SNR = 50

using flat priors



using informed priors (through empirical relations)

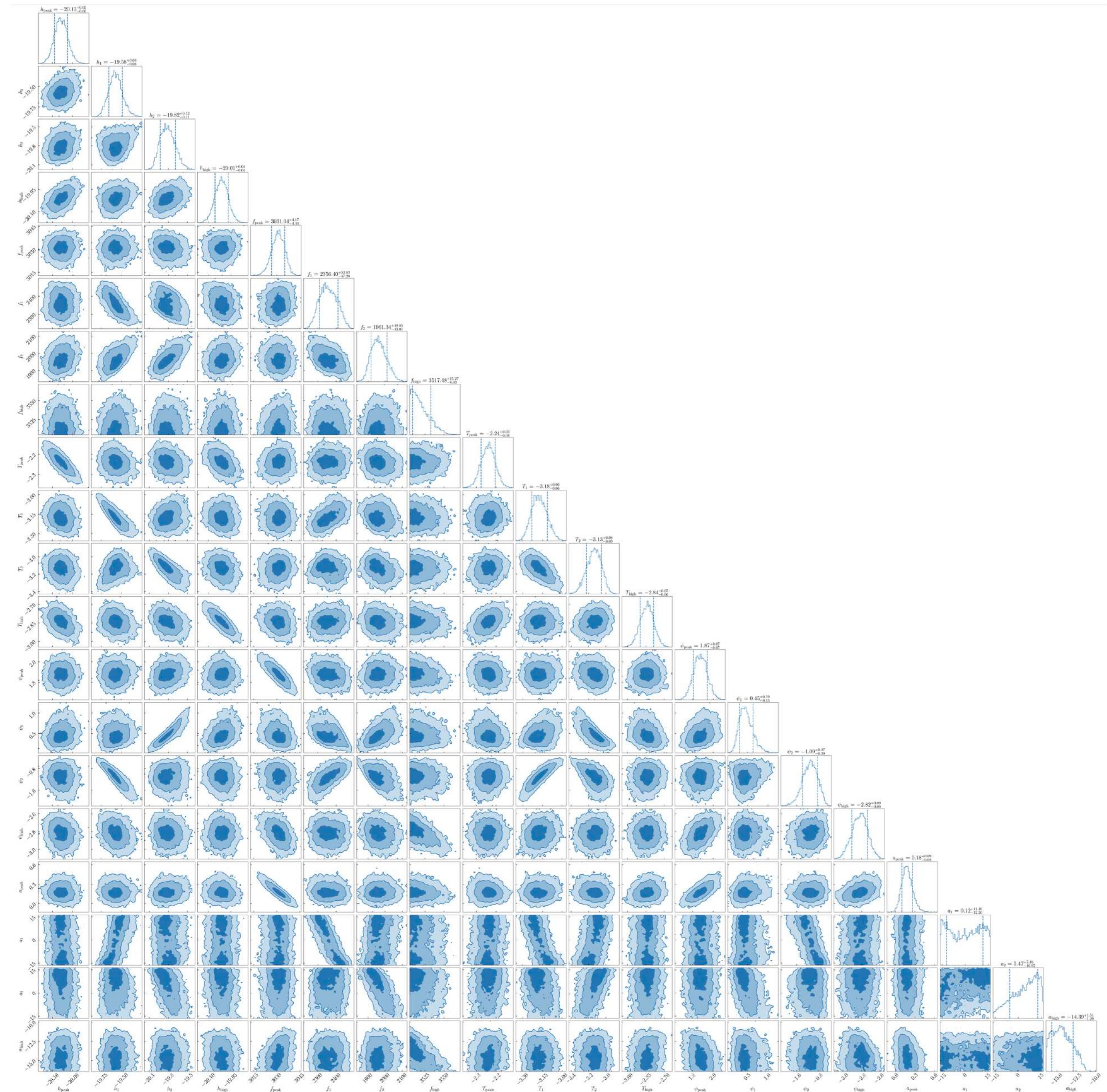


POSTERIOR DISTRIBUTIONS

EOS MPA 1.55+1.55, SNR = 50

using informed priors

all parameters



POCOMC: PRECONDITIONED MONTE CARLO SAMPLER

Preconditioned Monte Carlo Sampling (Karamanis et al. 2022)

PMC targets an **annealed version of the posterior**, with density given by

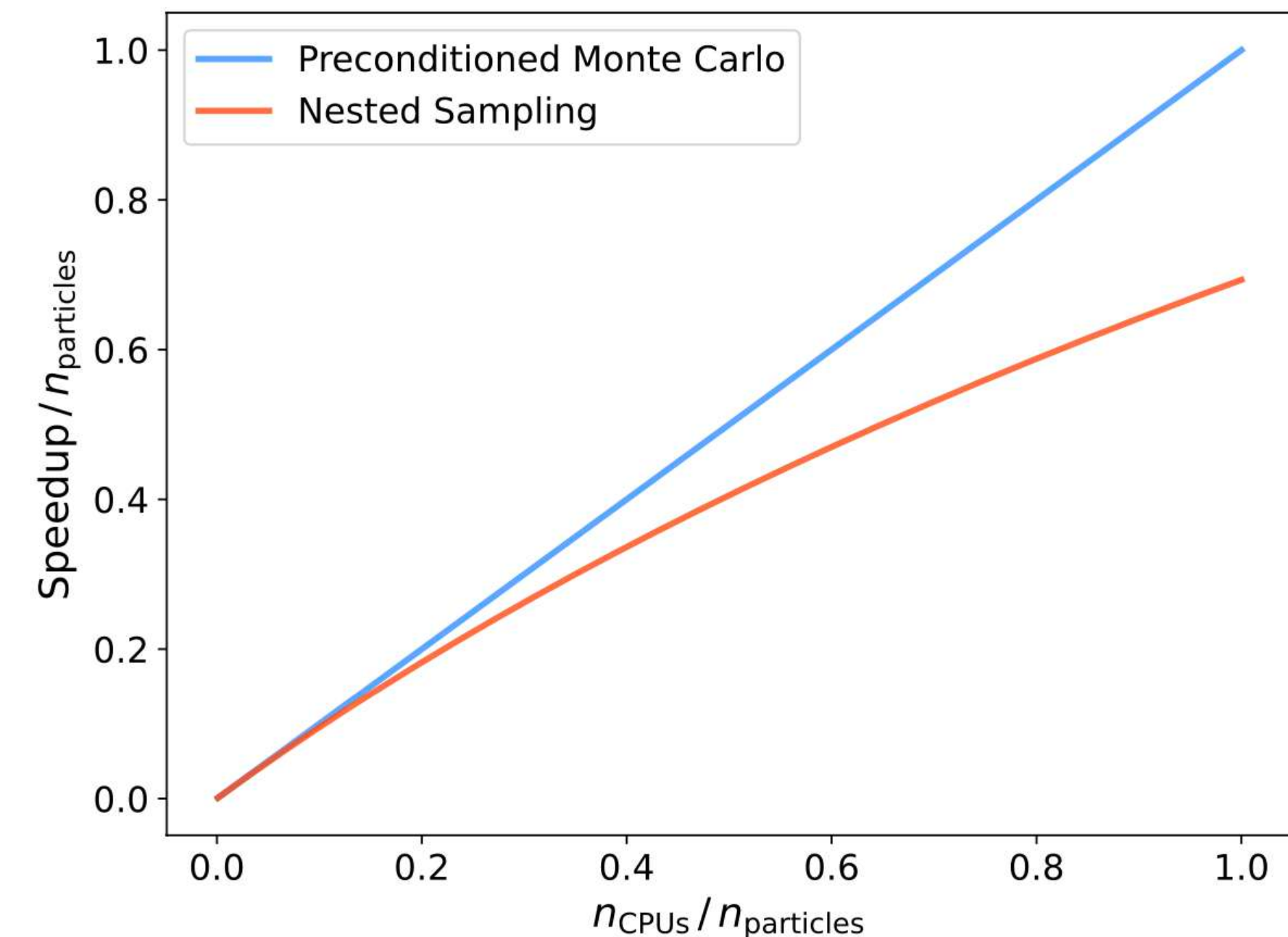
$$p_t(\boldsymbol{\theta} \mid d) \propto \mathcal{L}^{\beta_t}(\boldsymbol{\theta} \mid d)\pi(\boldsymbol{\theta})$$

where β_t a parameter (inverse temperature).

We use 2000 particles that **transition from the prior ($\beta_0 = 0$) to the posterior distribution ($\beta_T = 1$)**, through a sequence of reweighing, resampling and mutation steps.

pocomc

<https://github.com/minaskar/pocomc>



PocoMC is highly parallelizable

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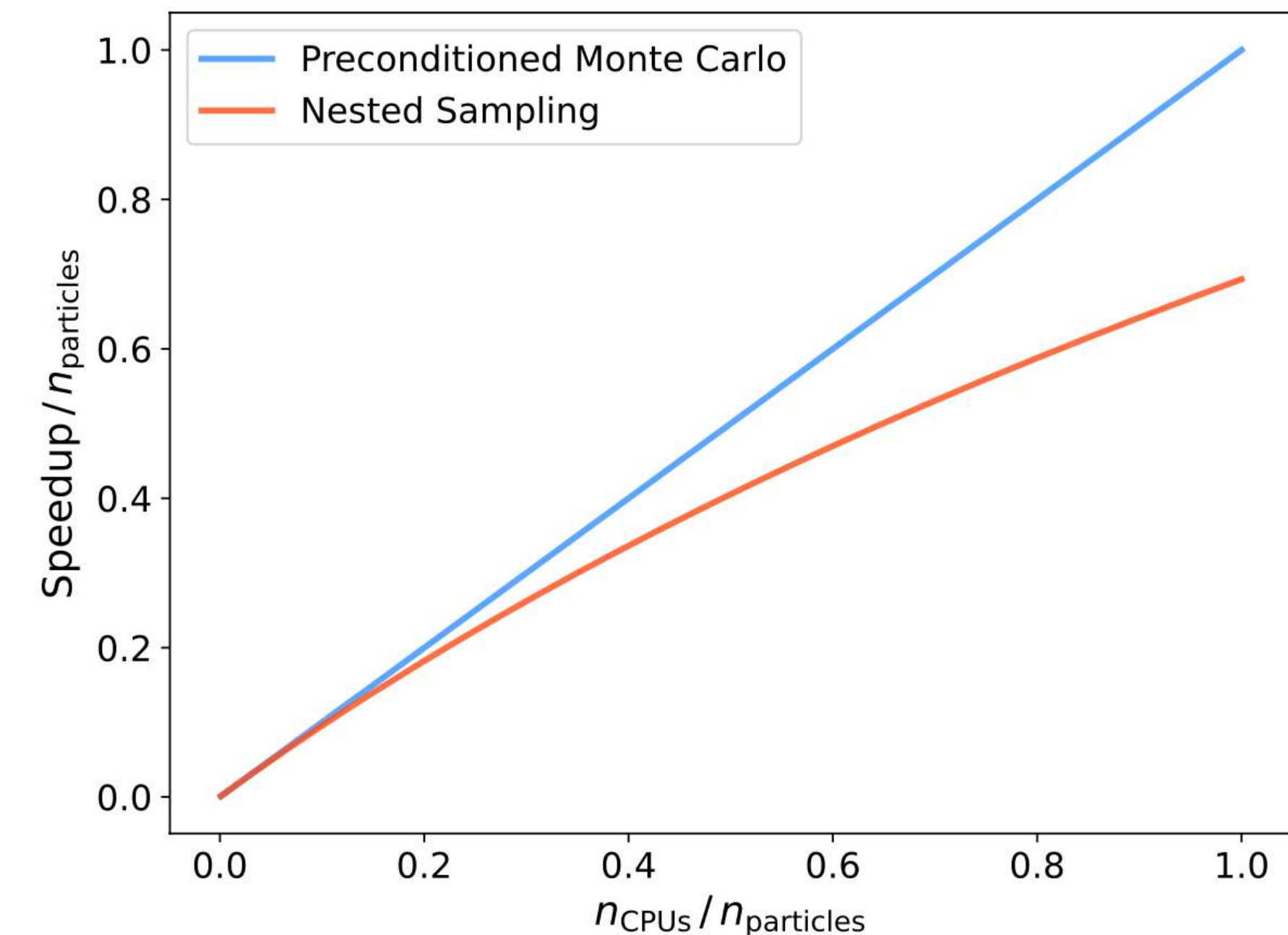
We use 2000 particles that **transition from the prior** ($\beta_0 = 0$) to **the posterior distribution** ($\beta_T = 1$), through a sequence of reweighing, resampling and mutation steps.

After each iteration, a **normalizing flow** transforms the **distribution to a simpler one** (almost Gaussian), decorrelating the parameters. This allows for a much faster sampling.

On same number of CPUs: pocoMC is **~10 times faster** than dynesty.

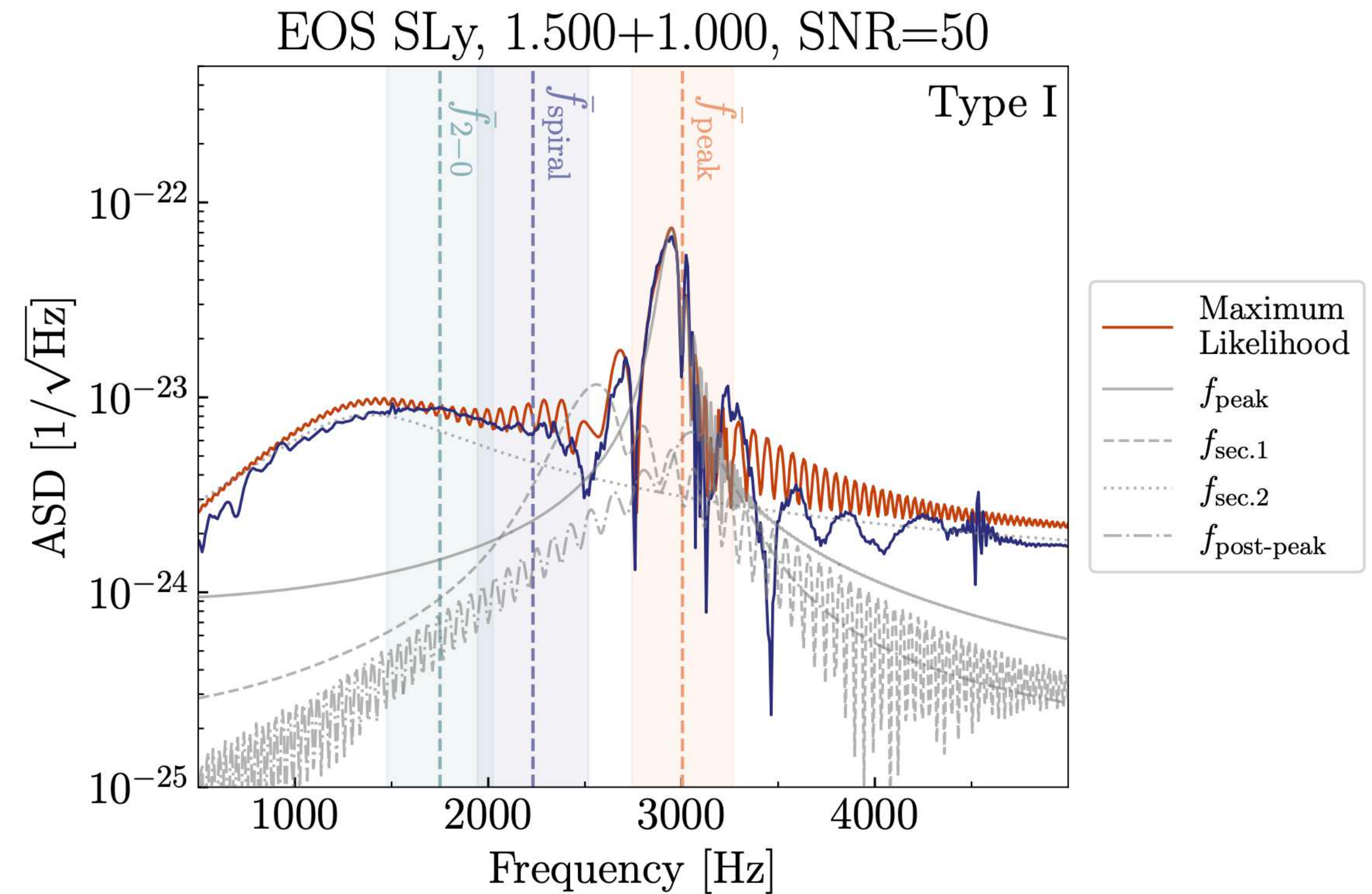
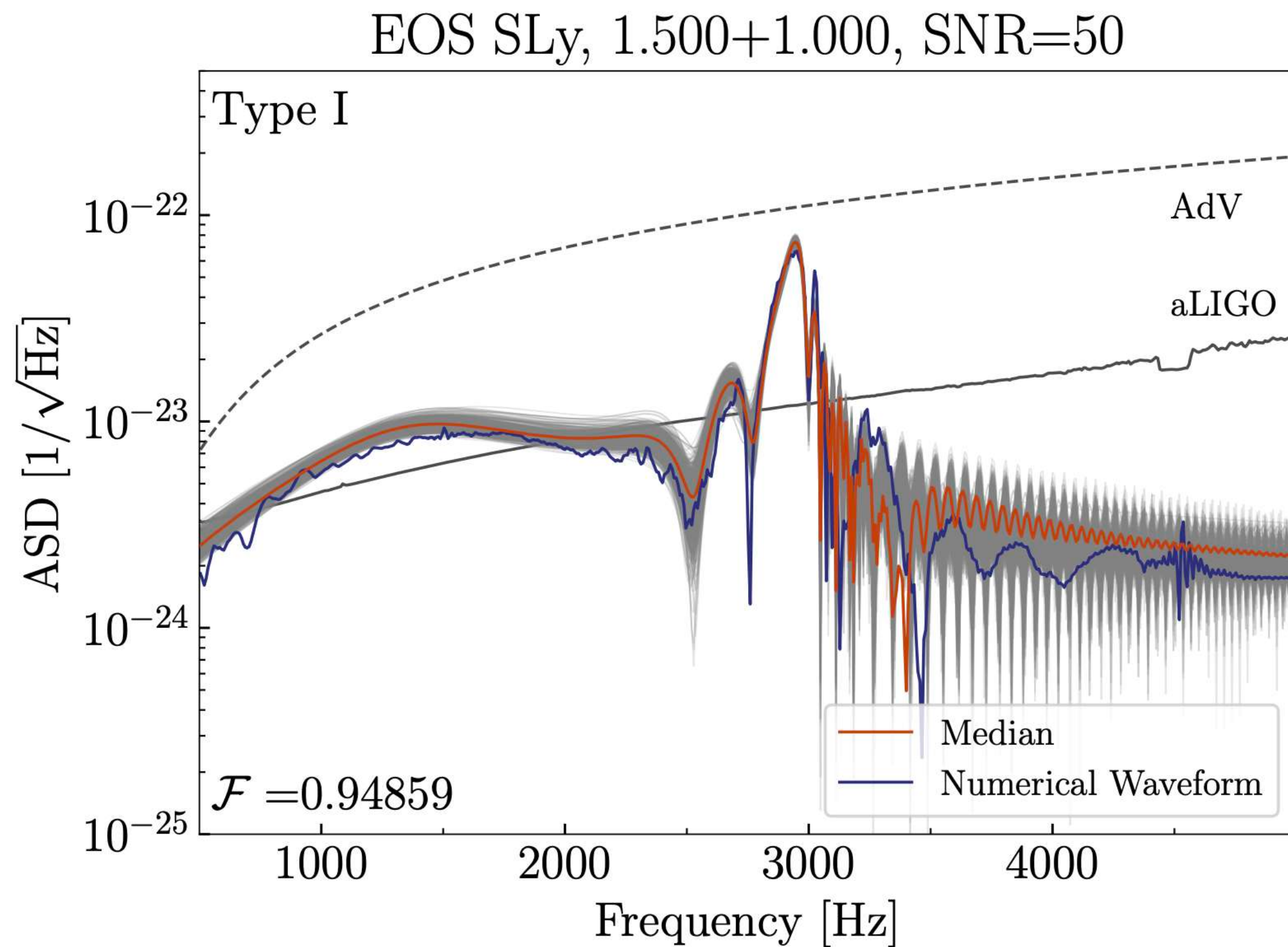
pocomc

<https://github.com/minaskar/pocomc>

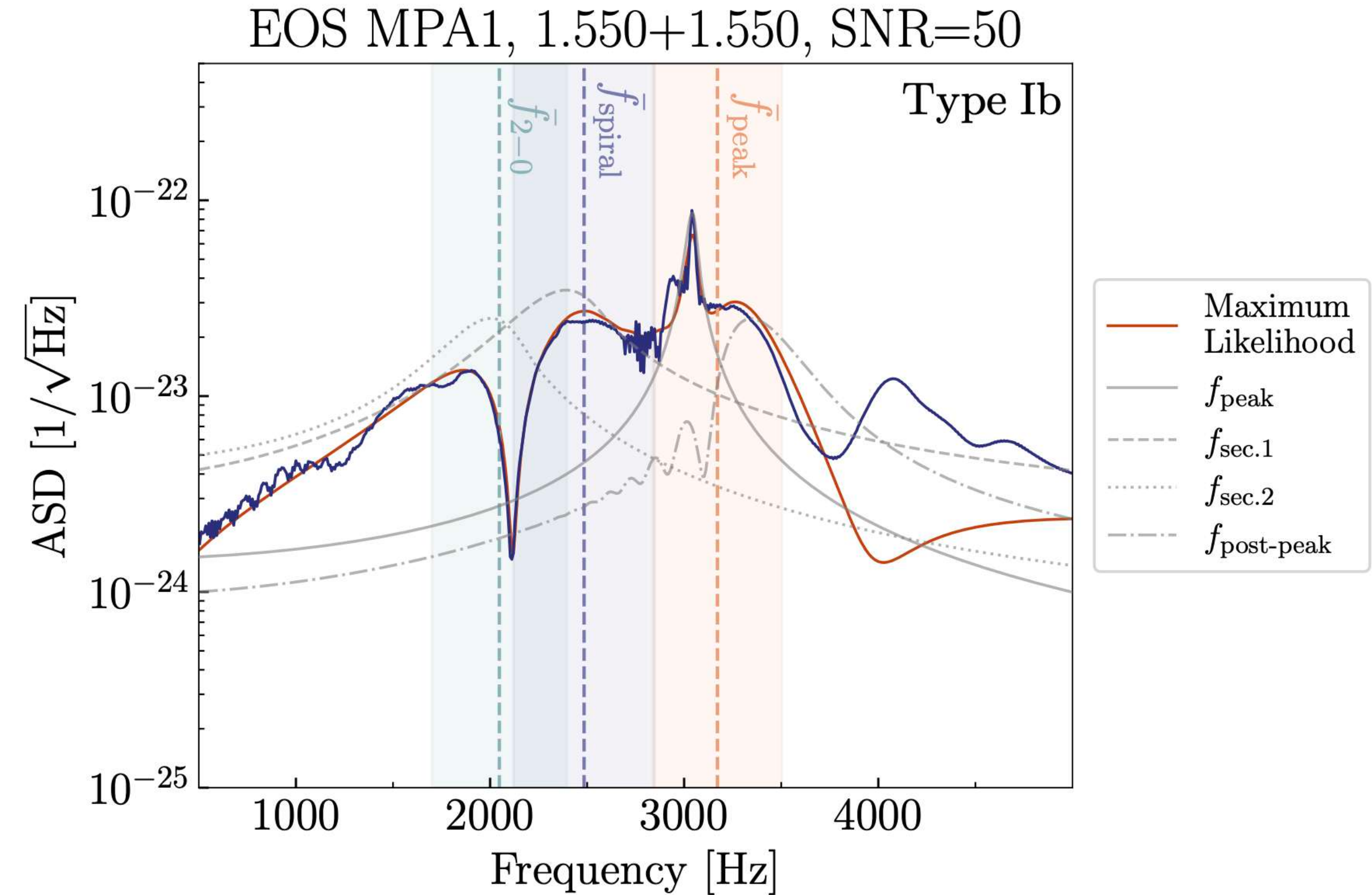
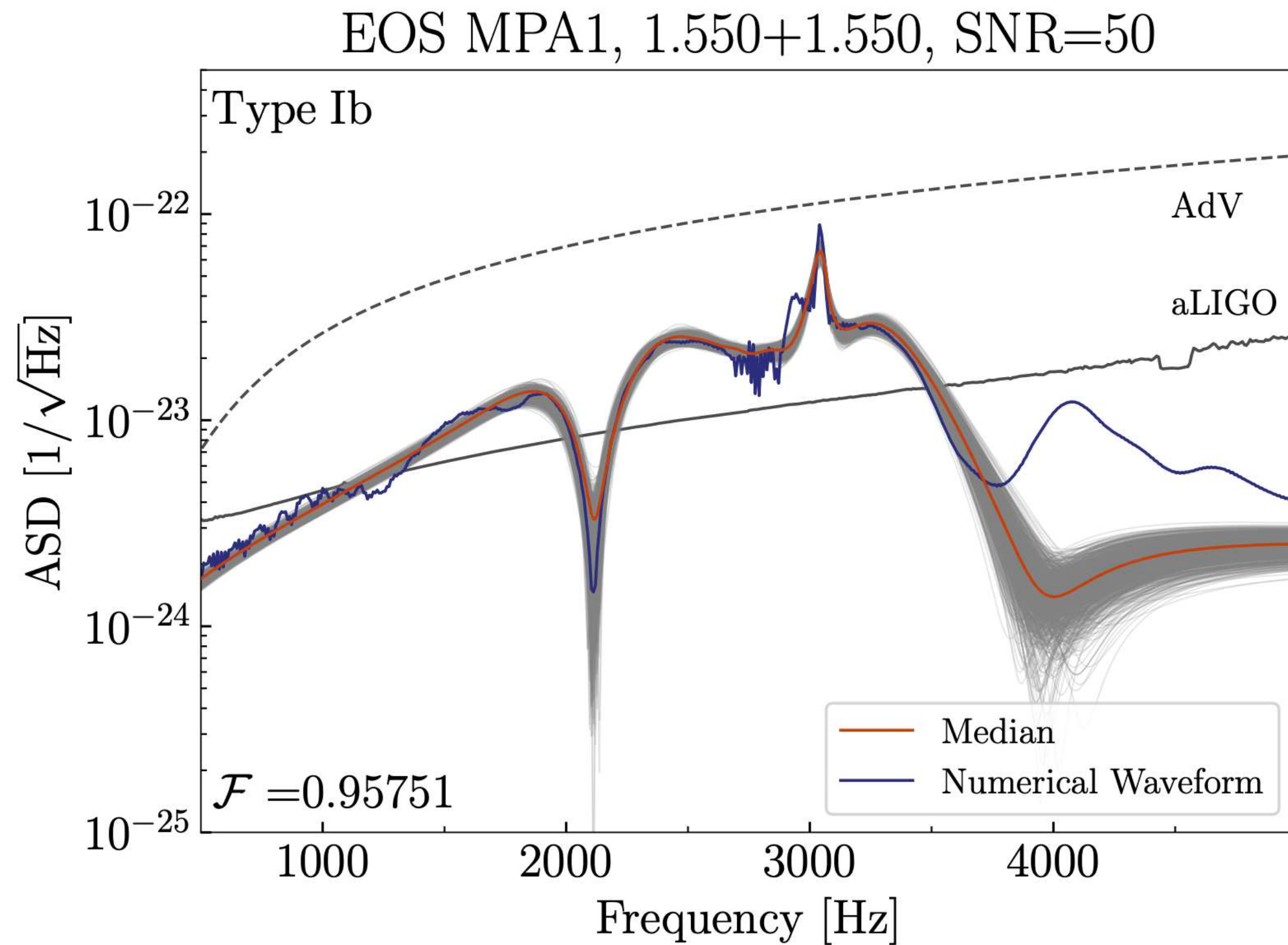


PocoMC is highly parallelizable

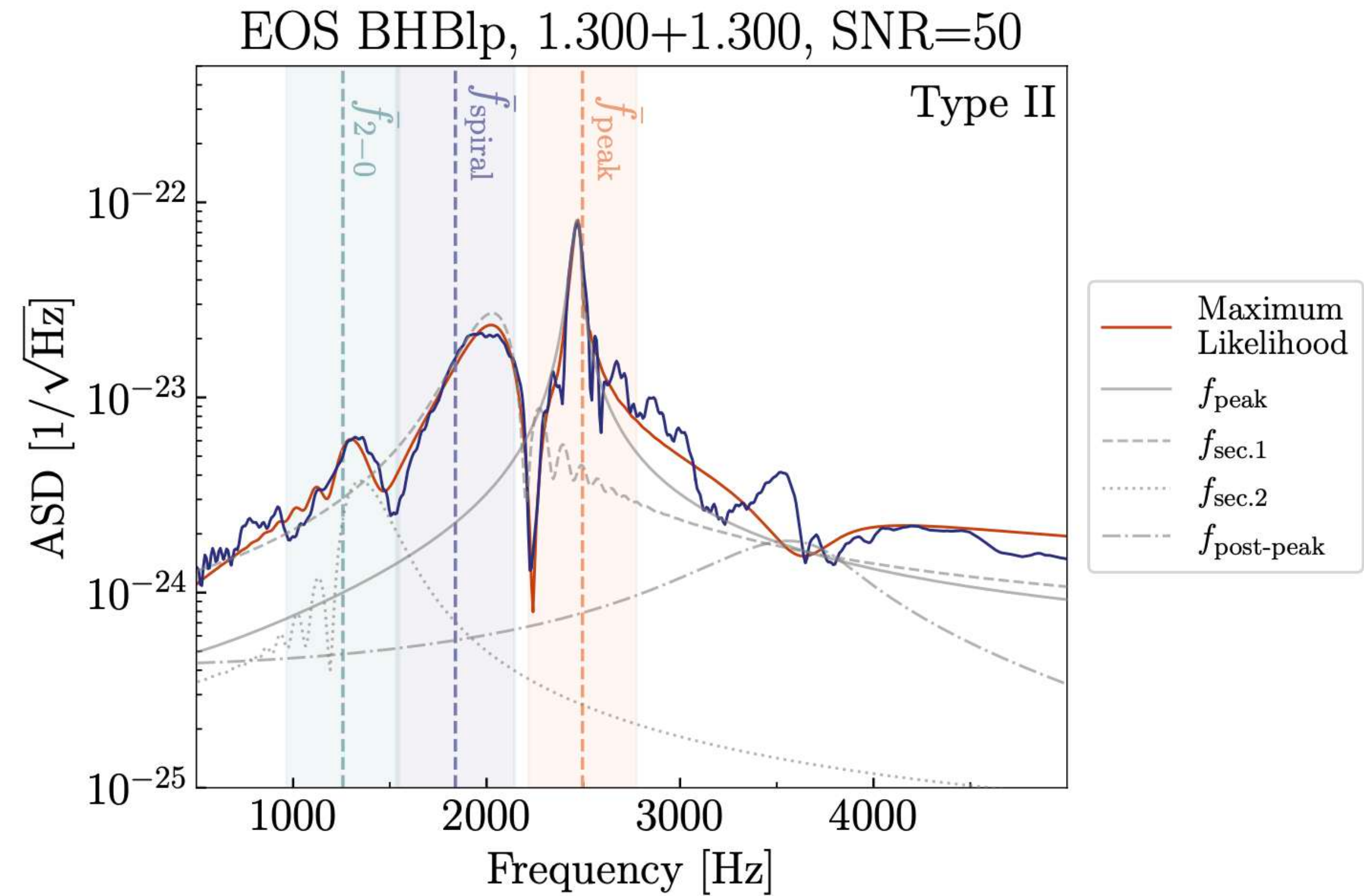
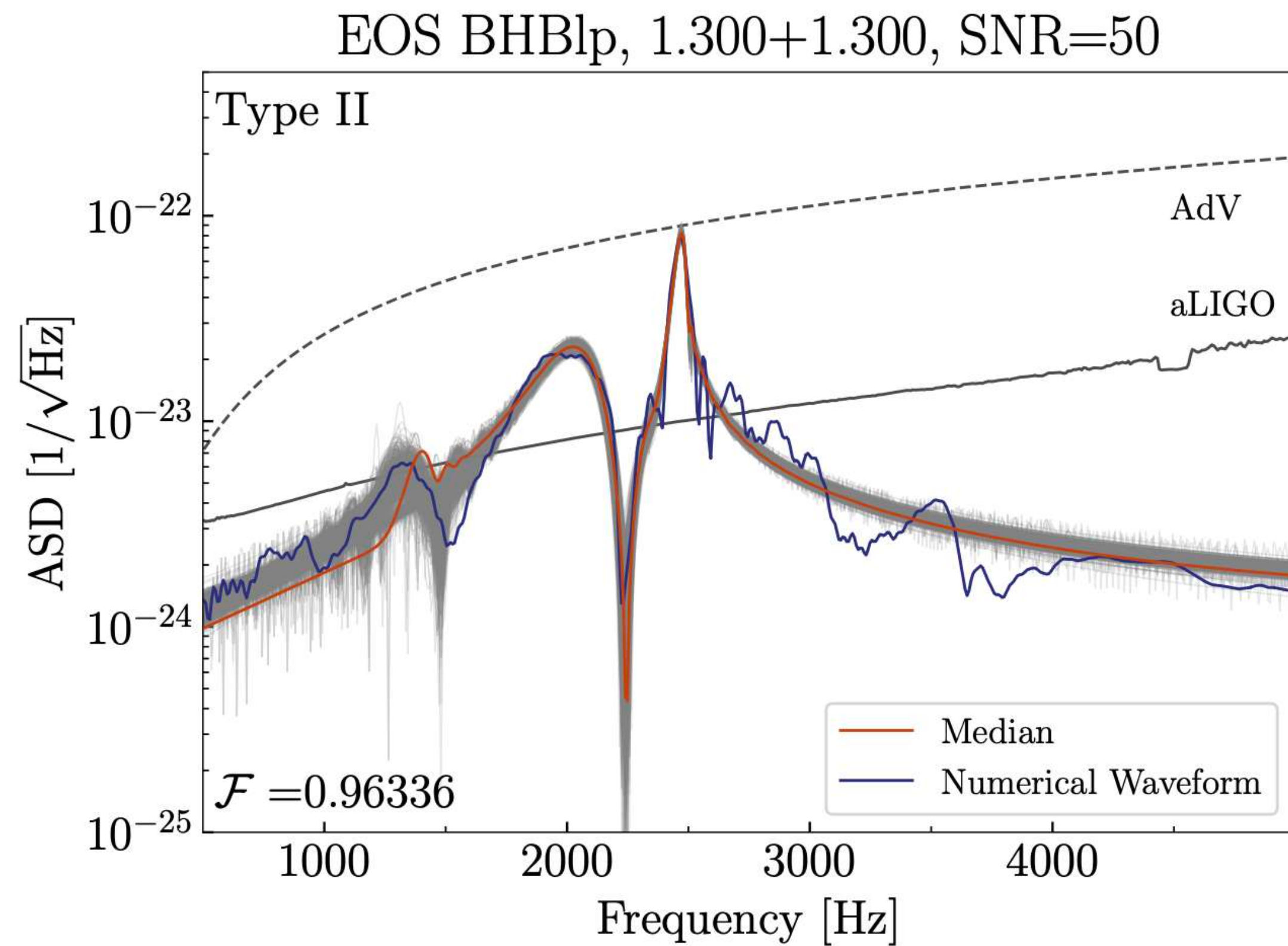
RECONSTRUCTION IN THE FREQUENCY DOMAIN



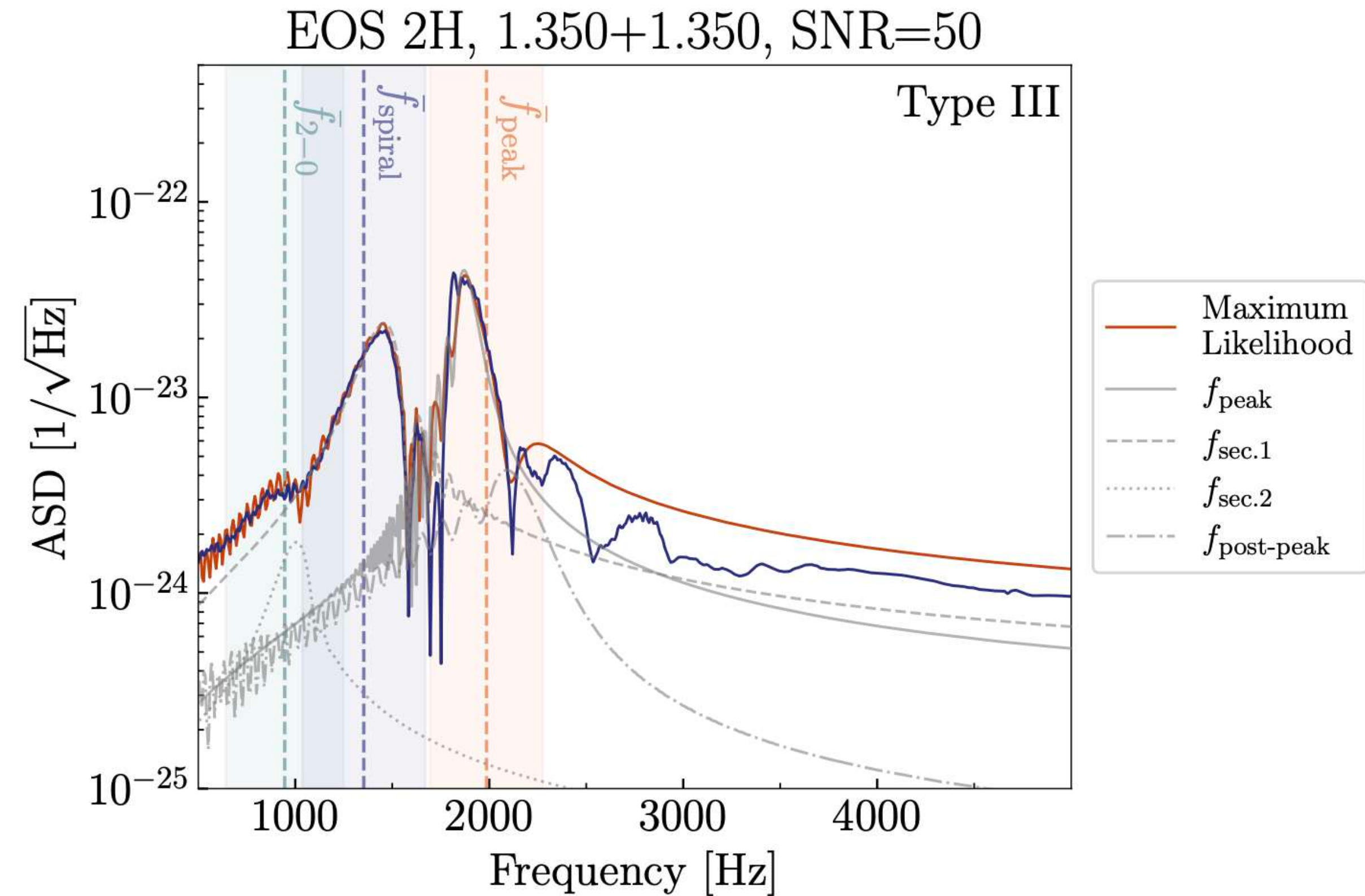
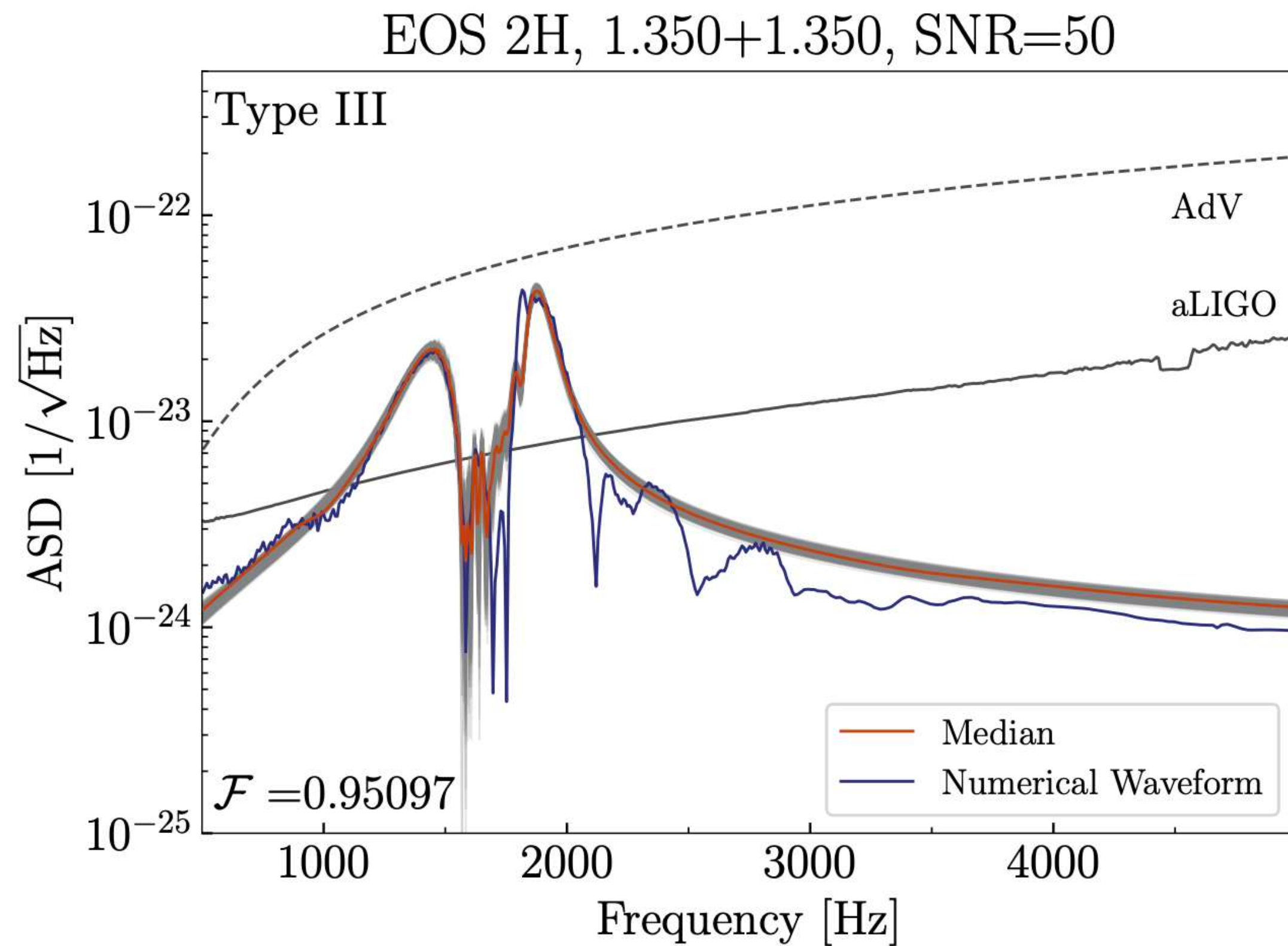
RECONSTRUCTION IN THE FREQUENCY DOMAIN



RECONSTRUCTION IN THE FREQUENCY DOMAIN



RECONSTRUCTION IN THE FREQUENCY DOMAIN

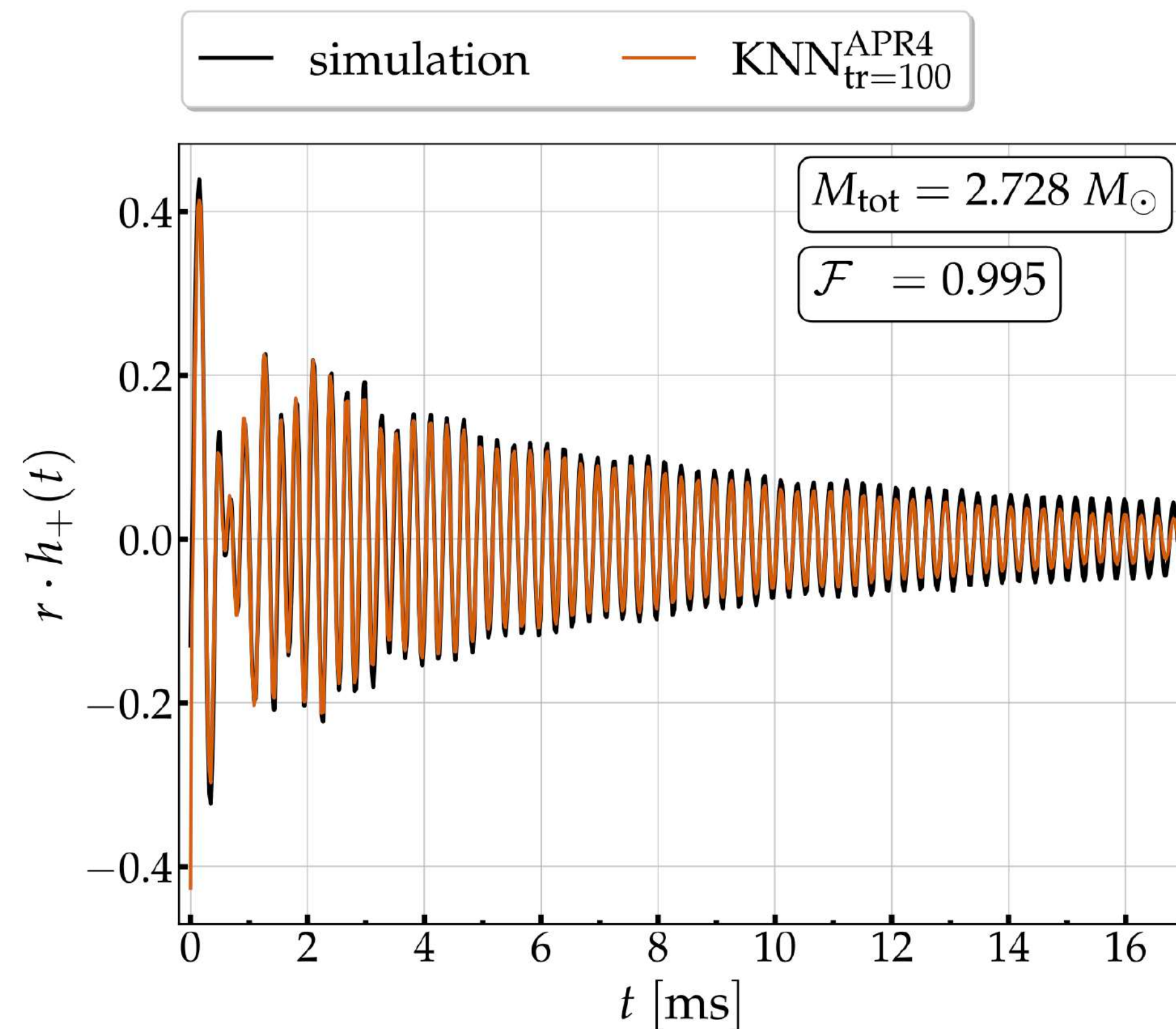


APPLICATION OF MACHINE LEARNING TO THE POST-MERGER PHASE

Problem: Only O(200) substantially different numerical BNS simulations are currently available.

Solution: Construct surrogate model of post-merger GWs as function of e.g. M , q , $\text{EOS}(\Lambda)$

Time domain surrogate model using
K-Nearest Neighbor (KNN) regression:

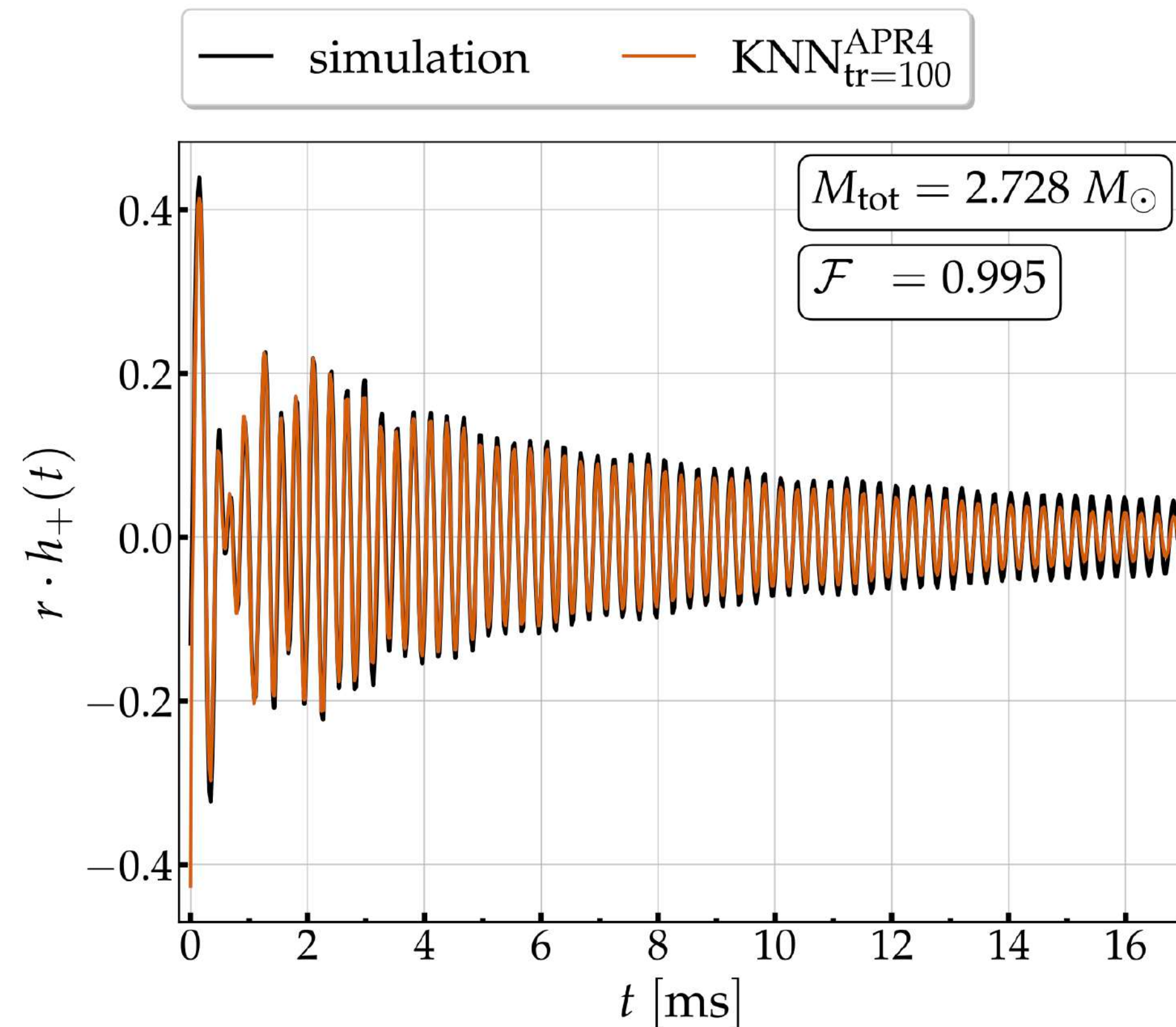


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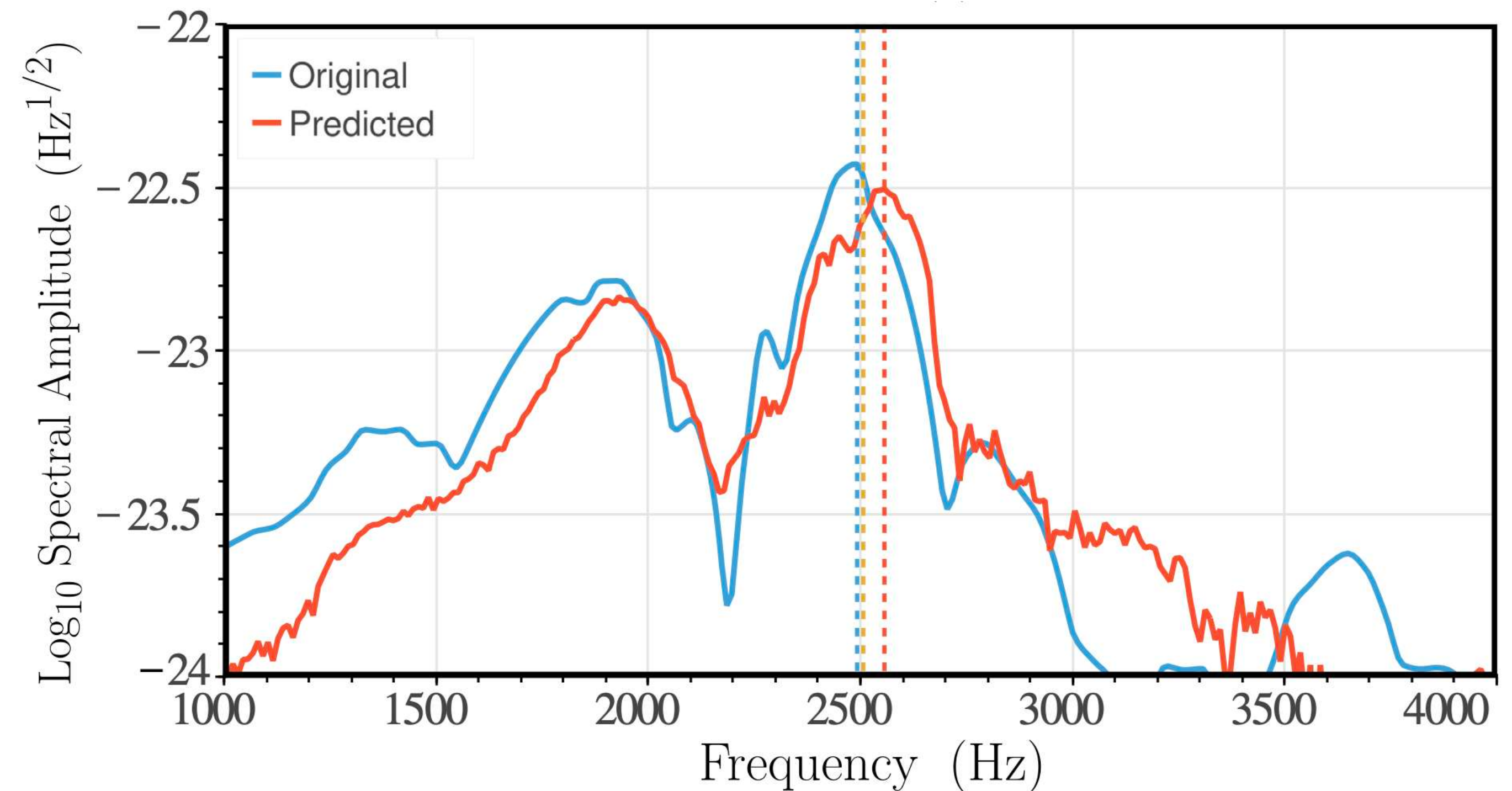
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Time domain surrogate model using
K-Nearest Neighbor (KNN) regression:



Soultanis et al. (2025)

Frequency domain surrogate model using
Artificial Neural Networks (ANN) regression:



Pesios et al. (2024)

K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

Training set: 20-100 different M_{tot}
($q=1$) between 2.4 and 2.8 M_{sun} .

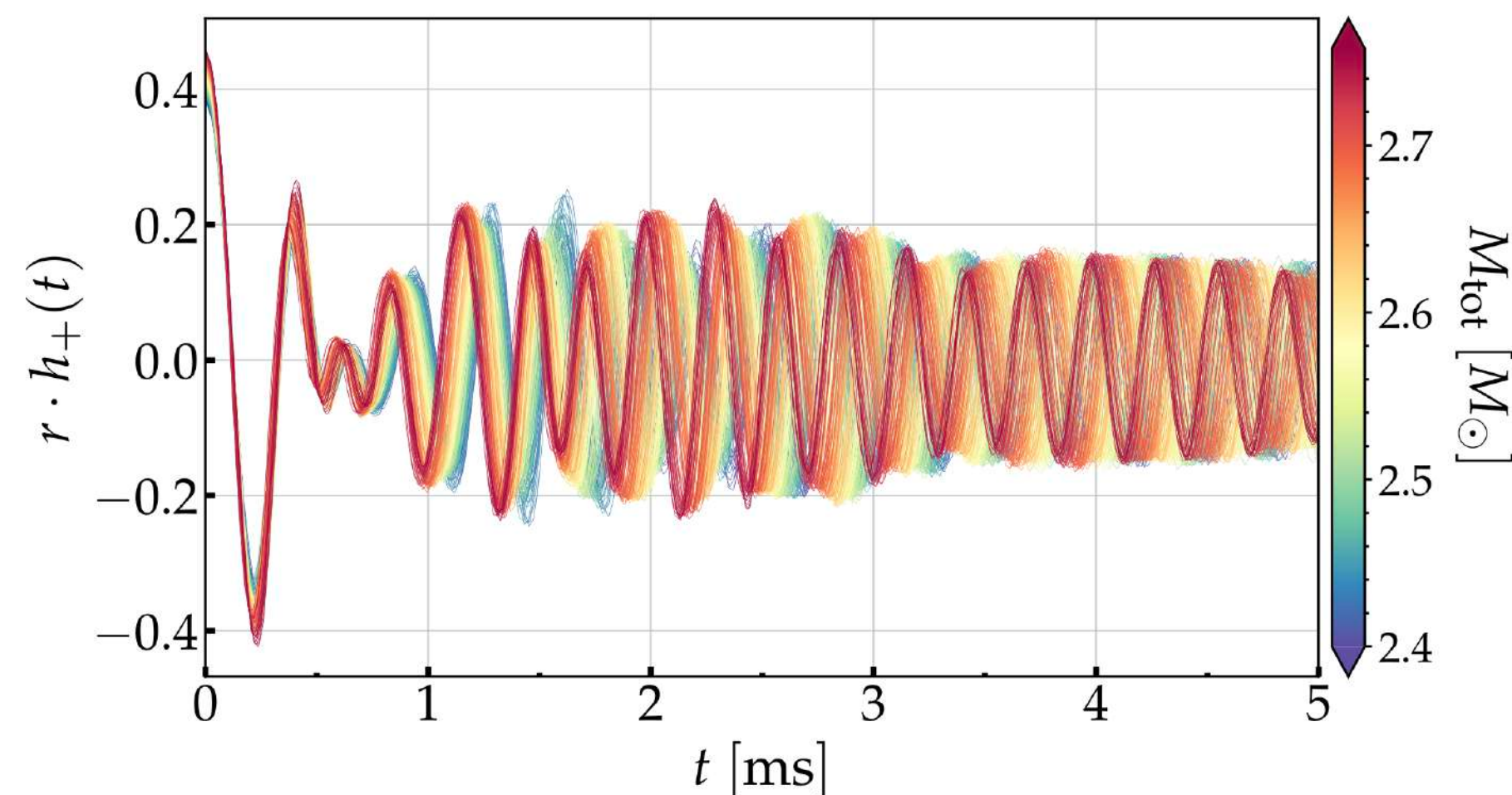
Choose specific EOS (APR4; SFHX).

Complex GW strain:

$$h(t) = h_+(t) + ih_\times(t)$$

$$= |h(t)| \cdot e^{+i\phi(t)},$$

Signals are aligned at merger time:



K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

Training set: 20-100 different M_{tot} ($q=1$) between 2.4 and 2.8 M_{sun} .

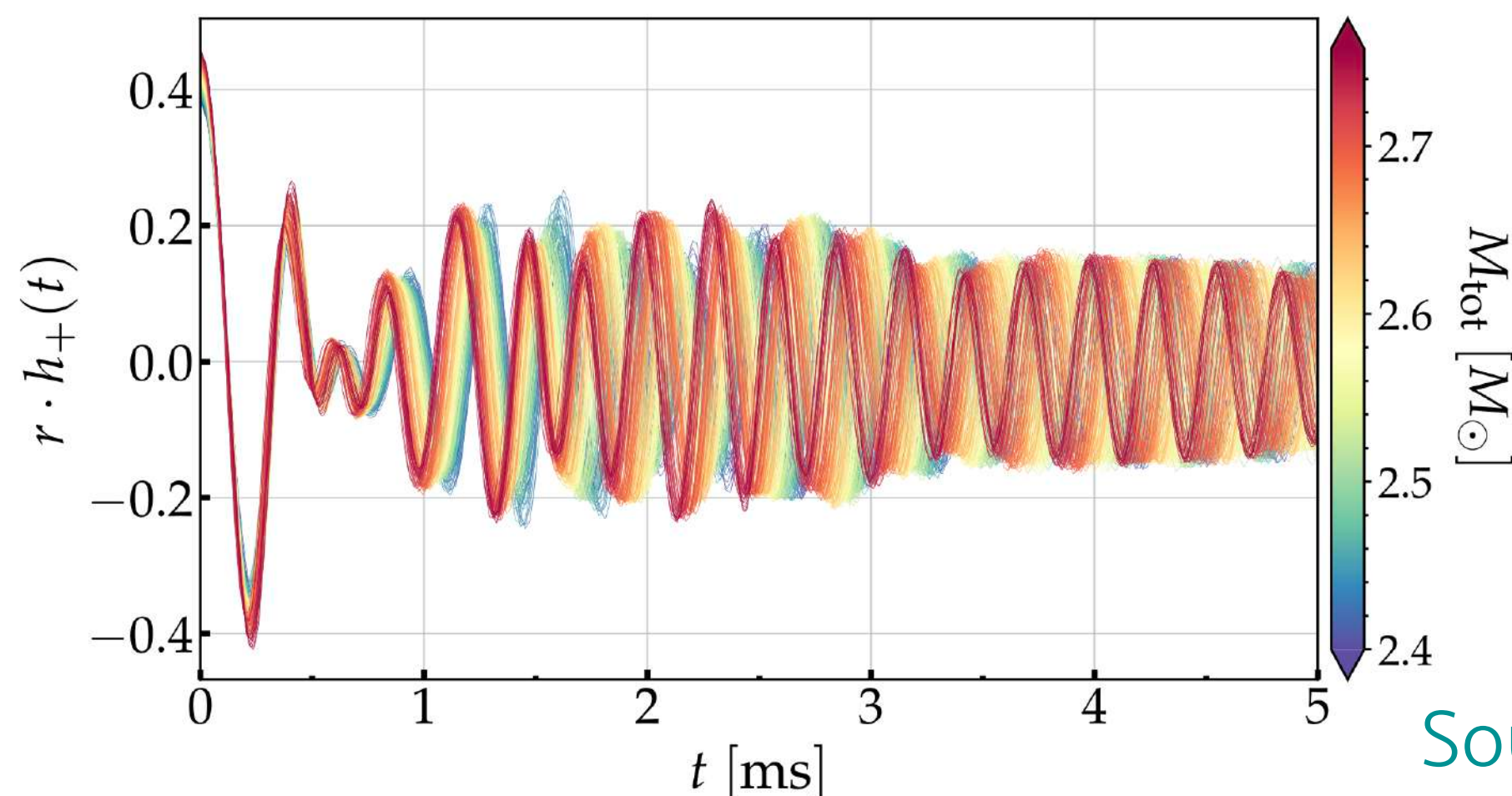
Choose specific EOS (APR4; SFHX).

Complex GW strain:

$$h(t) = h_+(t) + ih_\times(t)$$

$$= |h(t)| \cdot e^{+i\phi(t)},$$

Signals are aligned at merger time:



Input features: $\vec{X}_i = \{M_{\text{tot}}, t_j\}$

Predictions: $\vec{Y}_i = \text{strain data}$

KNN algorithm: For given input $\vec{X}_0$, find set N_0 of K nearest neighbors

The prediction is a weighted average

$$\vec{Y}_0 = \frac{1}{K} \sum_{\vec{X}_i \in \mathcal{N}_0} \frac{w_i \cdot \vec{Y}_i}{W}, \quad \text{where } W = \sum_{\vec{X}_i \in \mathcal{N}_0} w_i$$

and $w_i = 1/d_i$ where d_i is the distance between $\vec{X}_0$ and $\vec{X}_i$.

Hyperparameters: K and w_i
(tuned to optimal choices using a validation set)

Noise-weighted inner product for two signals:

$$\langle h_1(t), h_2(t) \rangle \equiv 4 \operatorname{Re} \int_0^\infty df \frac{\tilde{h}_1(f) \cdot \tilde{h}_2^*(f)}{S_h(f)}$$

Overlap:

$$\mathcal{O} \equiv \frac{\langle h_1(t), h_2(t) \rangle}{\sqrt{\langle h_1(t), h_1(t) \rangle \langle h_2(t), h_2(t) \rangle}}$$

Faithfulness (maximized overlap)

$$\mathcal{F} \equiv \max_{\phi_0, t_0} \frac{\langle h_1(t), h_2(t) \rangle}{\sqrt{\langle h_1(t), h_1(t) \rangle \langle h_2(t), h_2(t) \rangle}}$$

K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

Noise-weighted inner product for two signals:

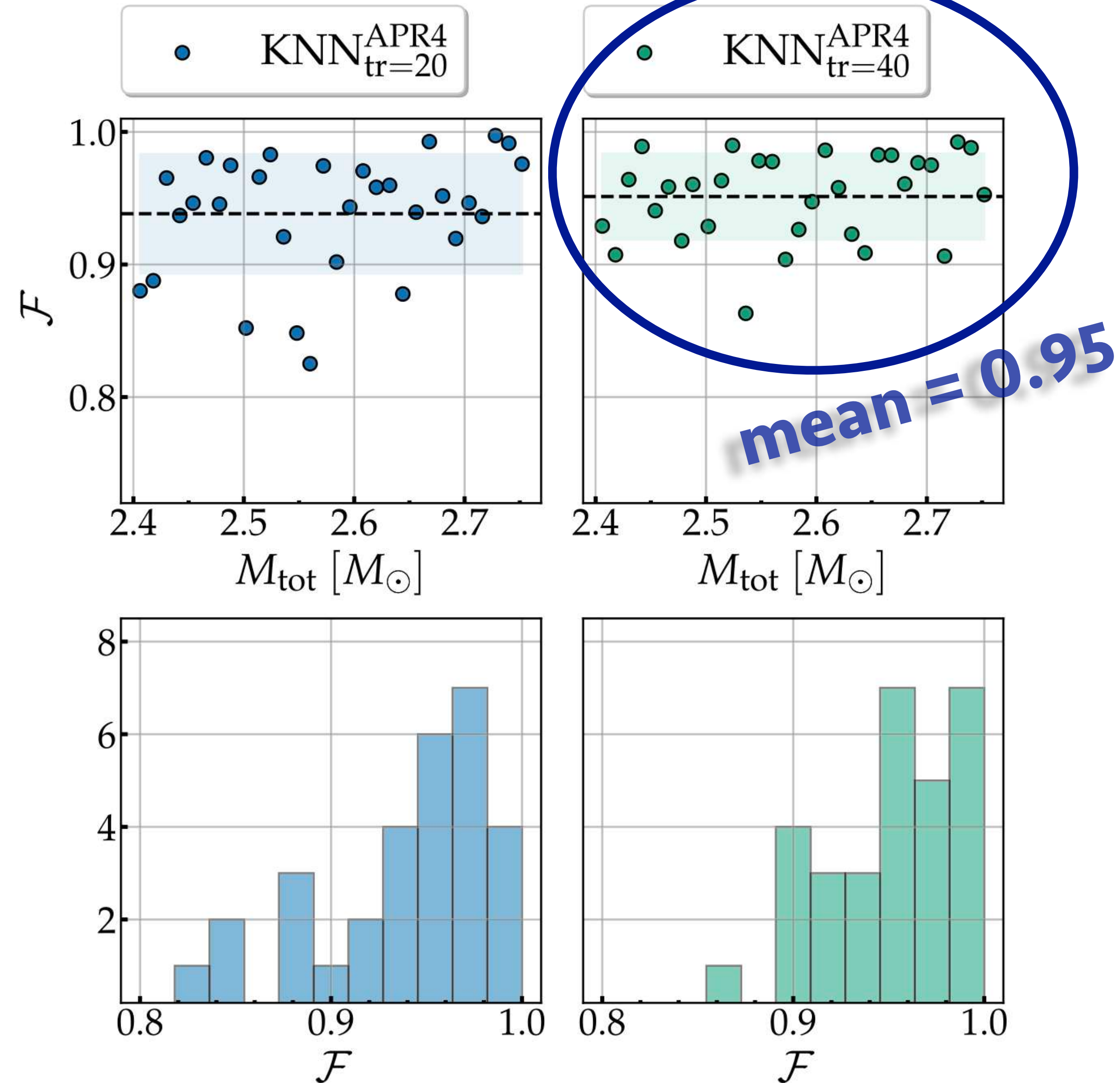
$$\langle h_1(t), h_2(t) \rangle \equiv 4 \operatorname{Re} \int_0^\infty df \frac{\tilde{h}_1(f) \cdot \tilde{h}_2^*(f)}{S_h(f)}$$

Overlap:

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Faithfulness (maximized overlap)

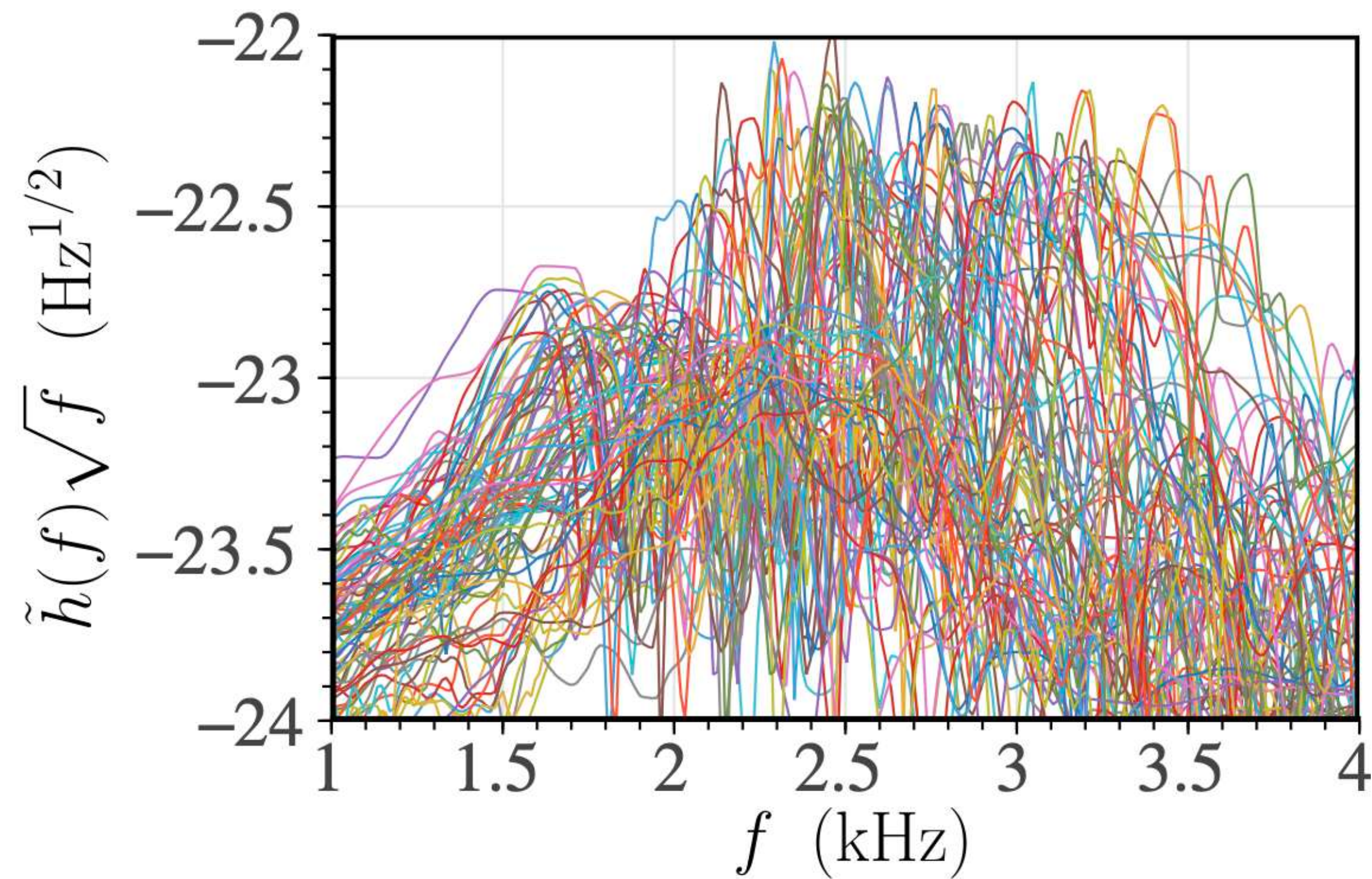
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ANN REGRESSION IN THE FREQUENCY DOMAIN

Expanded training set: 87 equal-mass models using 14 different EOS

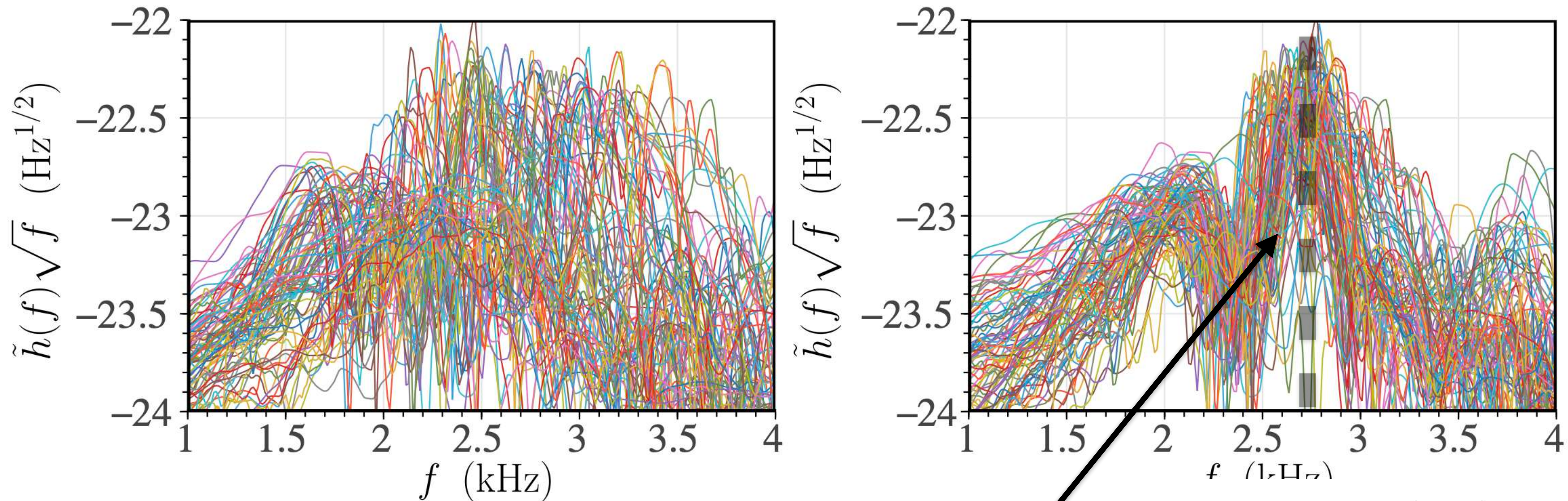
Surrogate model now depends on both mass and tidal deformability.



ANN REGRESSION IN THE FREQUENCY DOMAIN

Expanded training set: 87 equal-mass models using 14 different EOS

Surrogate model now depends on both mass and tidal deformability.

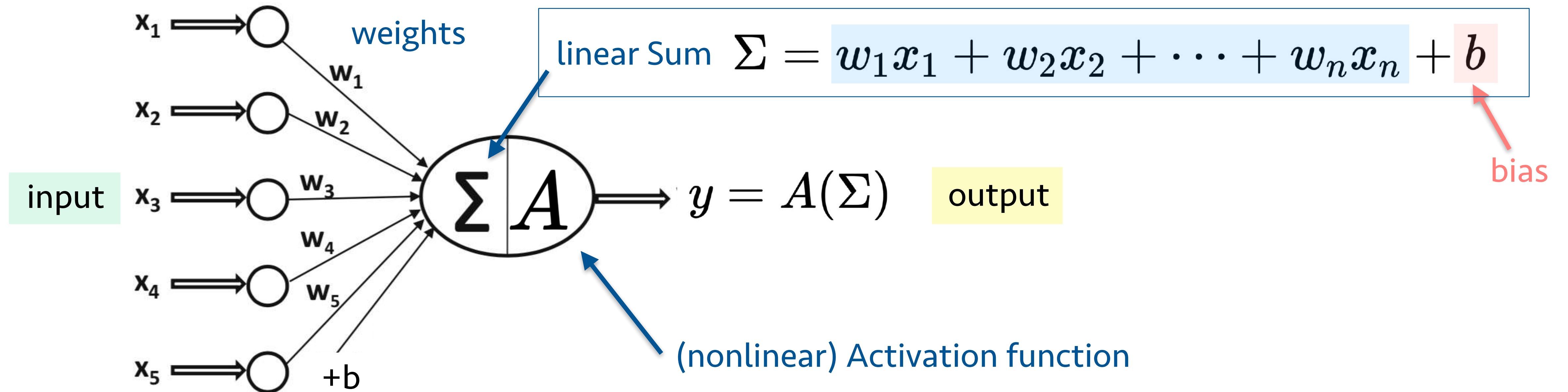


Partial alignment of spectra using empirical relation: $f_{\text{peak}}(\kappa_2^\tau, M) = 4 \frac{\beta_1}{M} \ln \left(\frac{\beta_0}{8\kappa_2^\tau} \right)$

Pesios, Koutalios, Kugiumtzis, Stergioulas (2024)

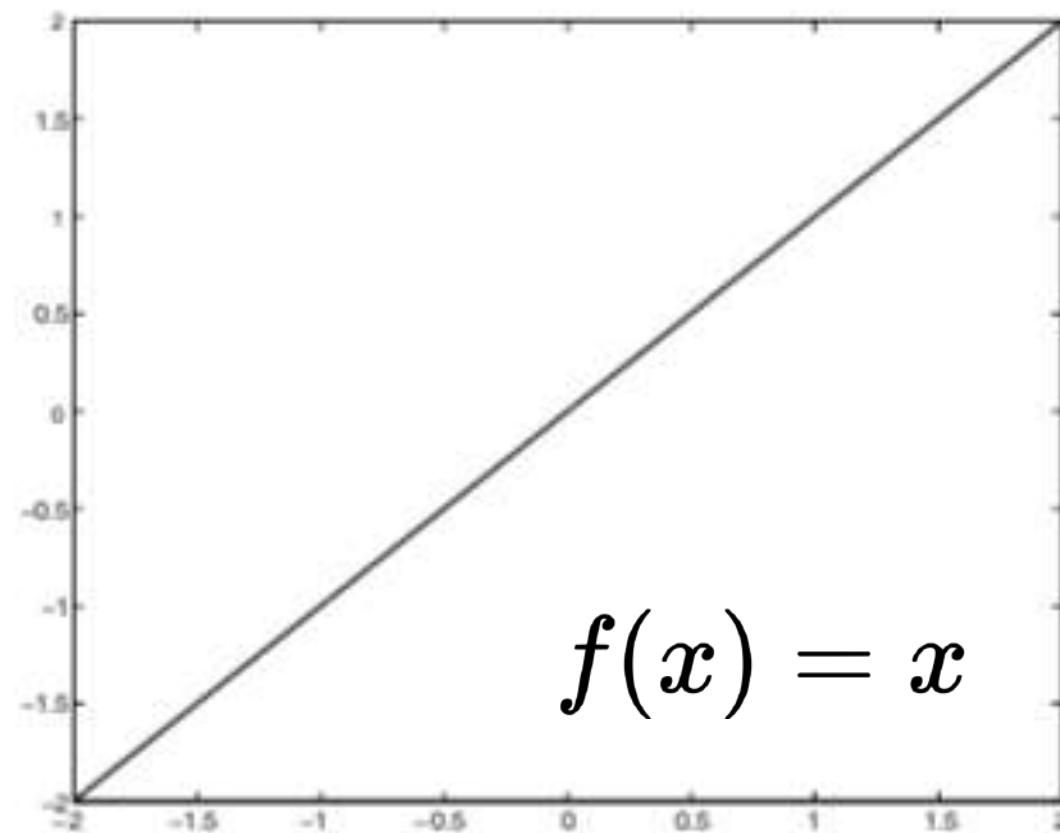
ARTIFICIAL NEURON

- Each **neuron** in the network maps several **input values** $x_1, \dots, x_n$ to an **output value** y

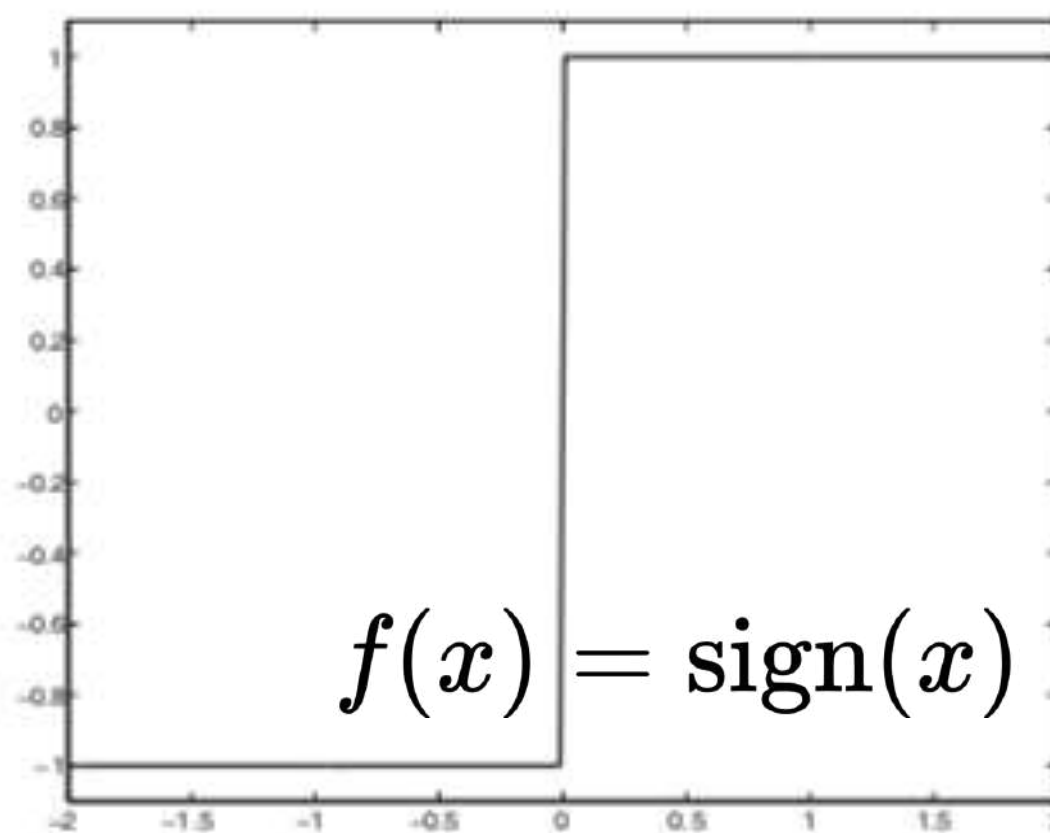


ACTIVATION FUNCTIONS

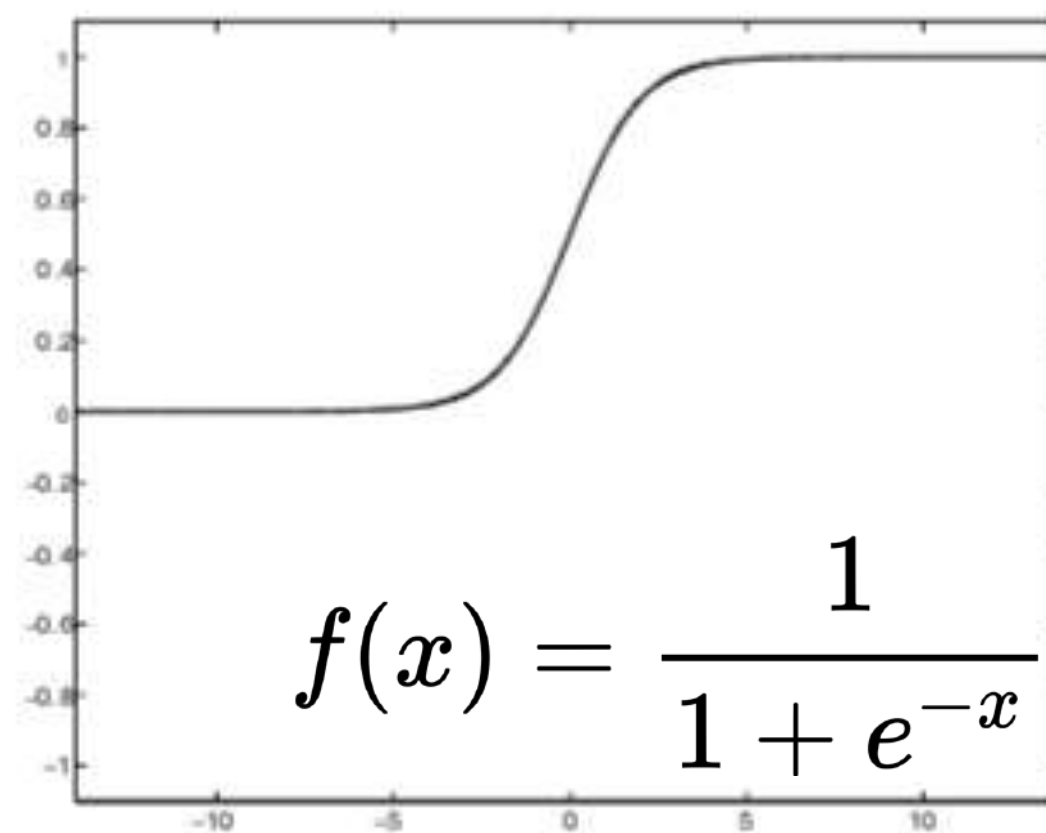
- Different common activation functions:



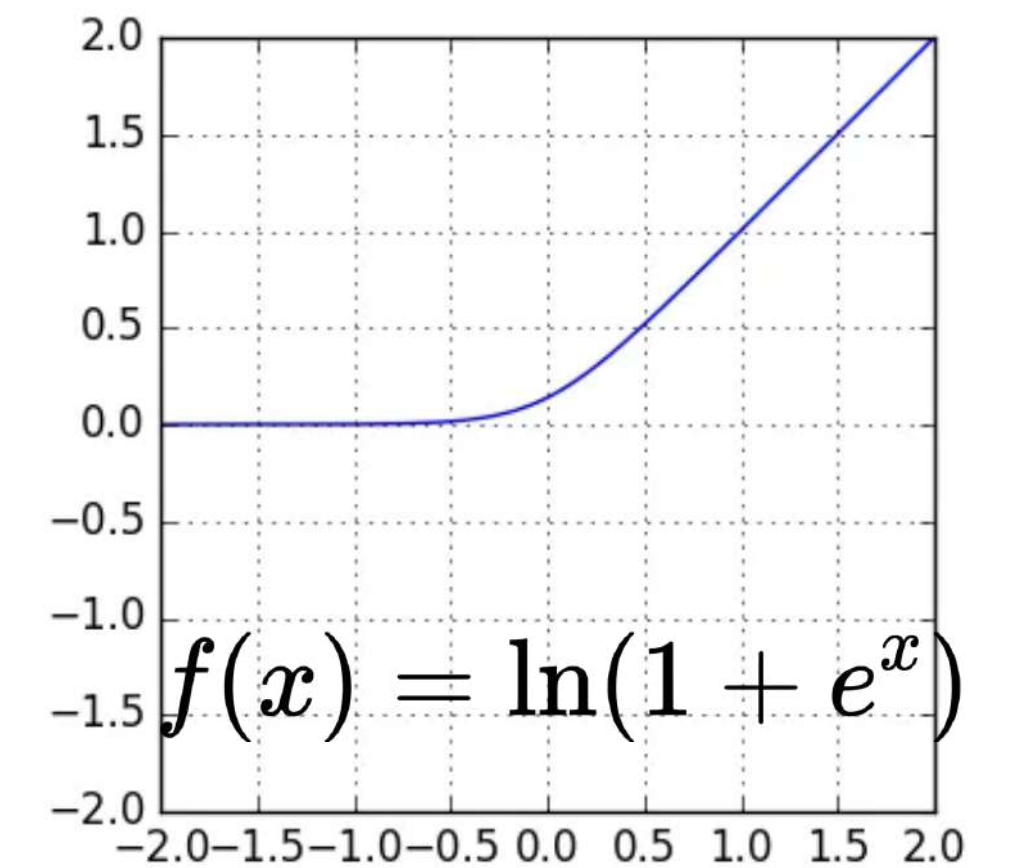
(a) Identity



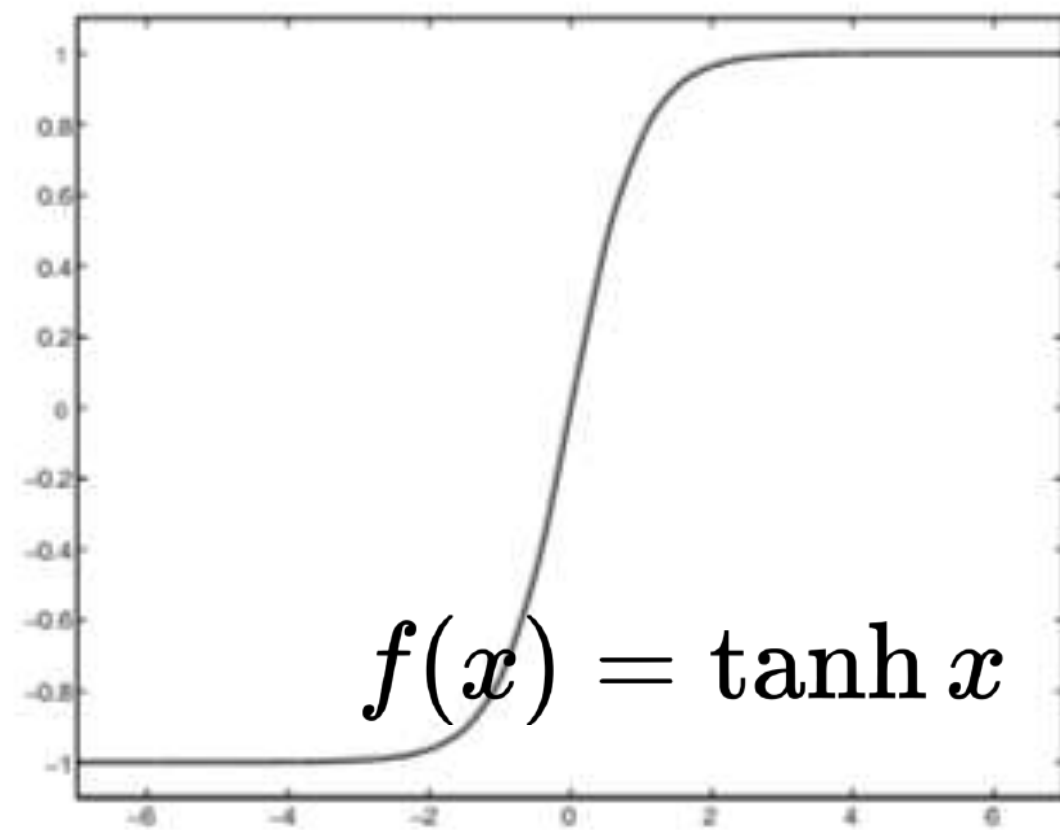
(b) Sign



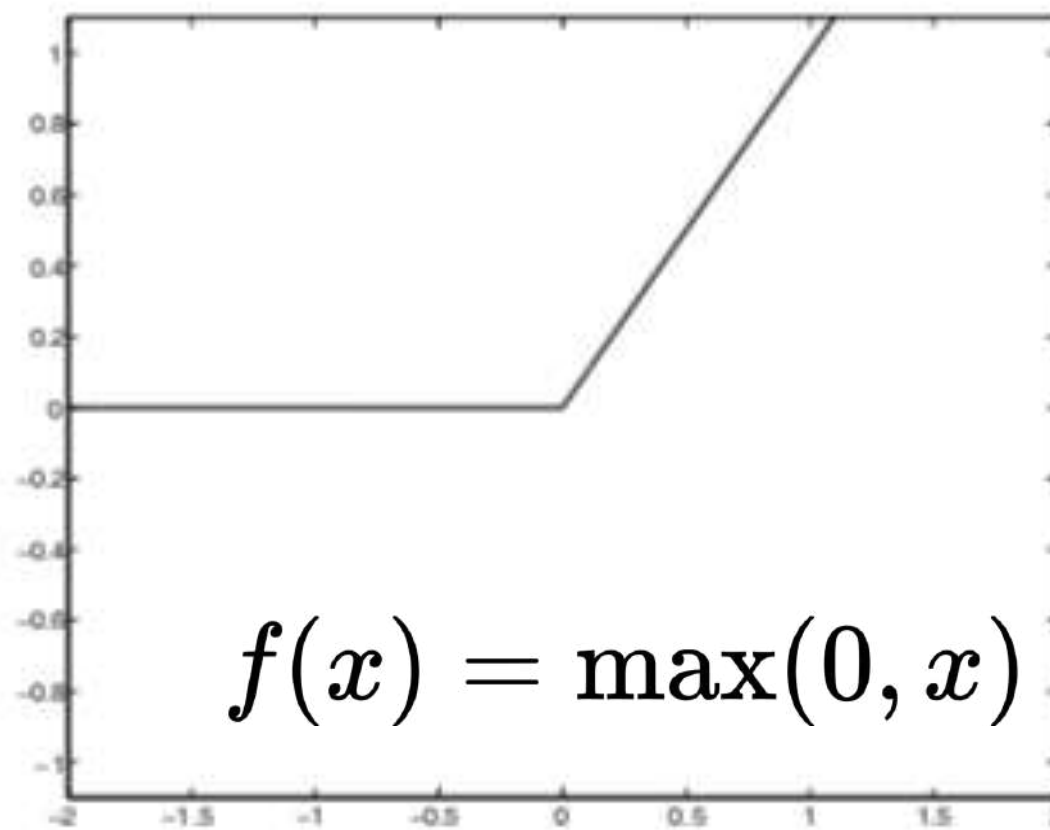
(c) Sigmoid (logistic function)



Softplus

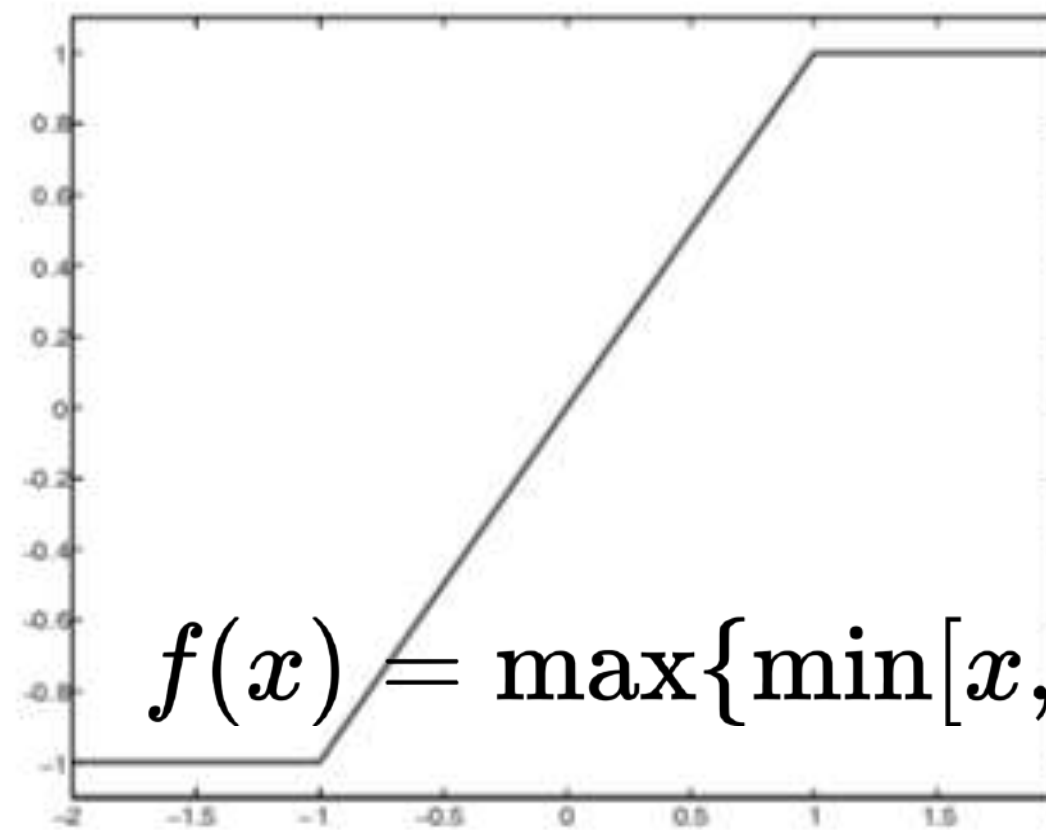


(d) Tanh



(e) ReLU

(Rectified Linear Unit)



(f) Hard Tanh

ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

1) Mass, 2) tidal coupling constant, 3) dR/dM

Prediction:

Magnitude of GW spectrum (1-4 kHz).

ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

1) *Mass*, 2) *tidal coupling constant*, 3) *dR/dM*

Prediction:

Magnitude of GW spectrum (1-4 kHz).

4-layer feed-forward ANN

Added Gaussian noise and dropout layers

Adam optimizer

Layer	Type	Shape	Activation	Params
1	Gaussian noise (0.1)	(None, 3)	...	0
2	Dense	(None, 200)	Linear	800
3	Gaussian noise (0.05)	(None, 200)	...	0
4	Dropout (0.15)	(None, 200)	...	0
5	Dense	(None, 400)	Sigmoid	80400
6	Gaussian noise (0.1)	(None, 400)	...	0
7	Dropout (0.15)	(None, 400)	...	0
8	Dense	(None, 400)	Sigmoid	160400
9	Gaussian noise (0.1)	(None, 400)	...	0
10	Dropout (0.05)	(None, 400)	...	0
11	Dense	(None, 370)	Linear	148370

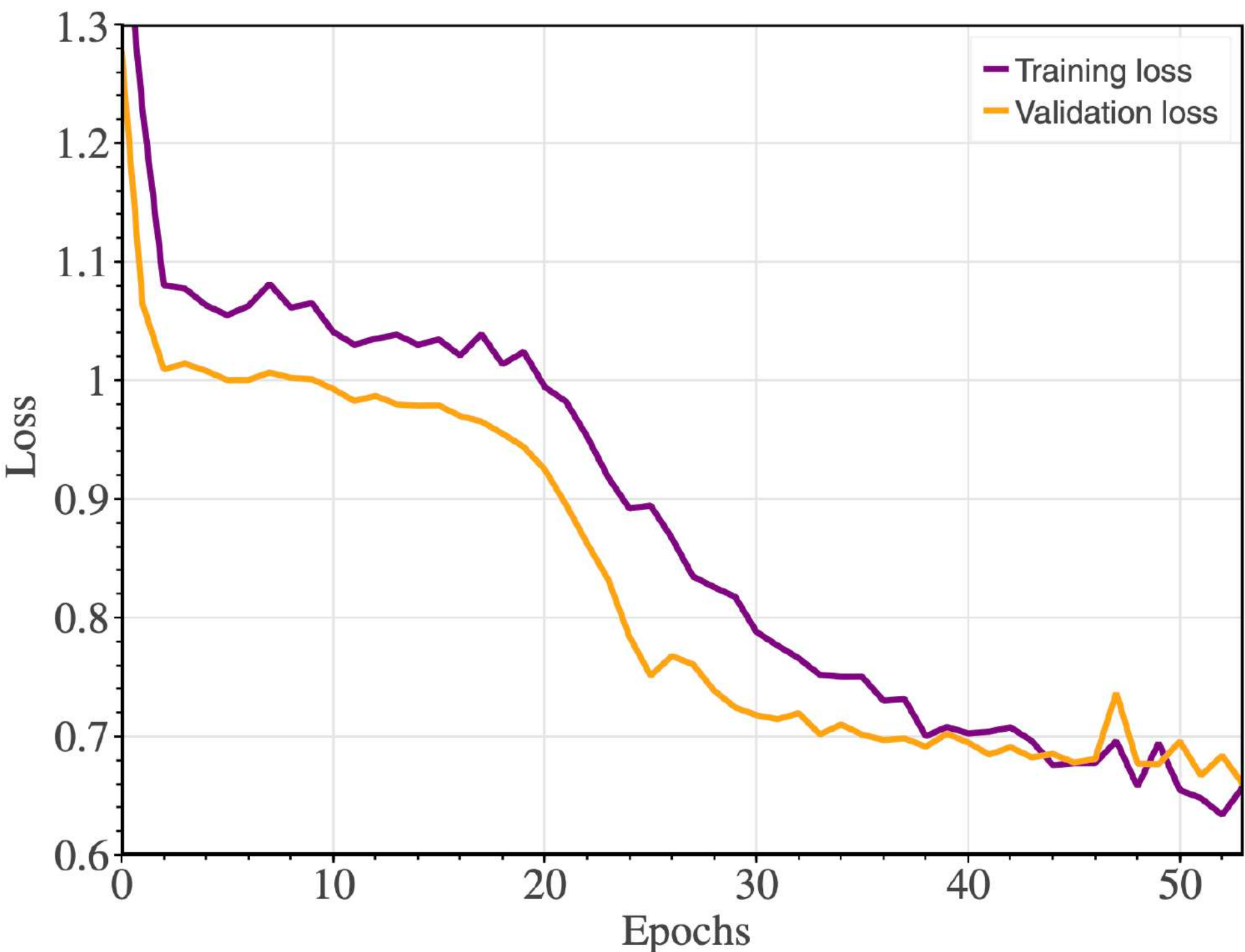
ANN SURROGATE IN THE FREQUENCY DOMAIN

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6	Gaussian noise (0.1)	(None, 400)	...	0
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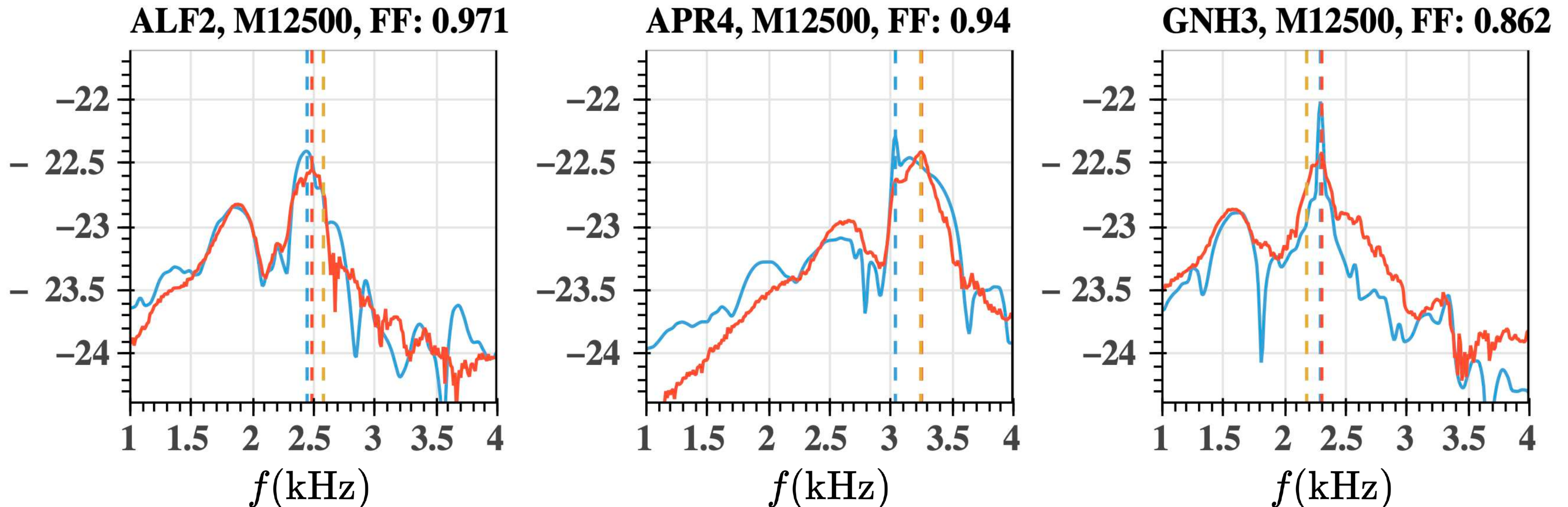
ANN SURROGATE IN THE FREQUENCY DOMAIN

Typical examples of predicted magnitudes of GW spectra

FF = 0 = overlap

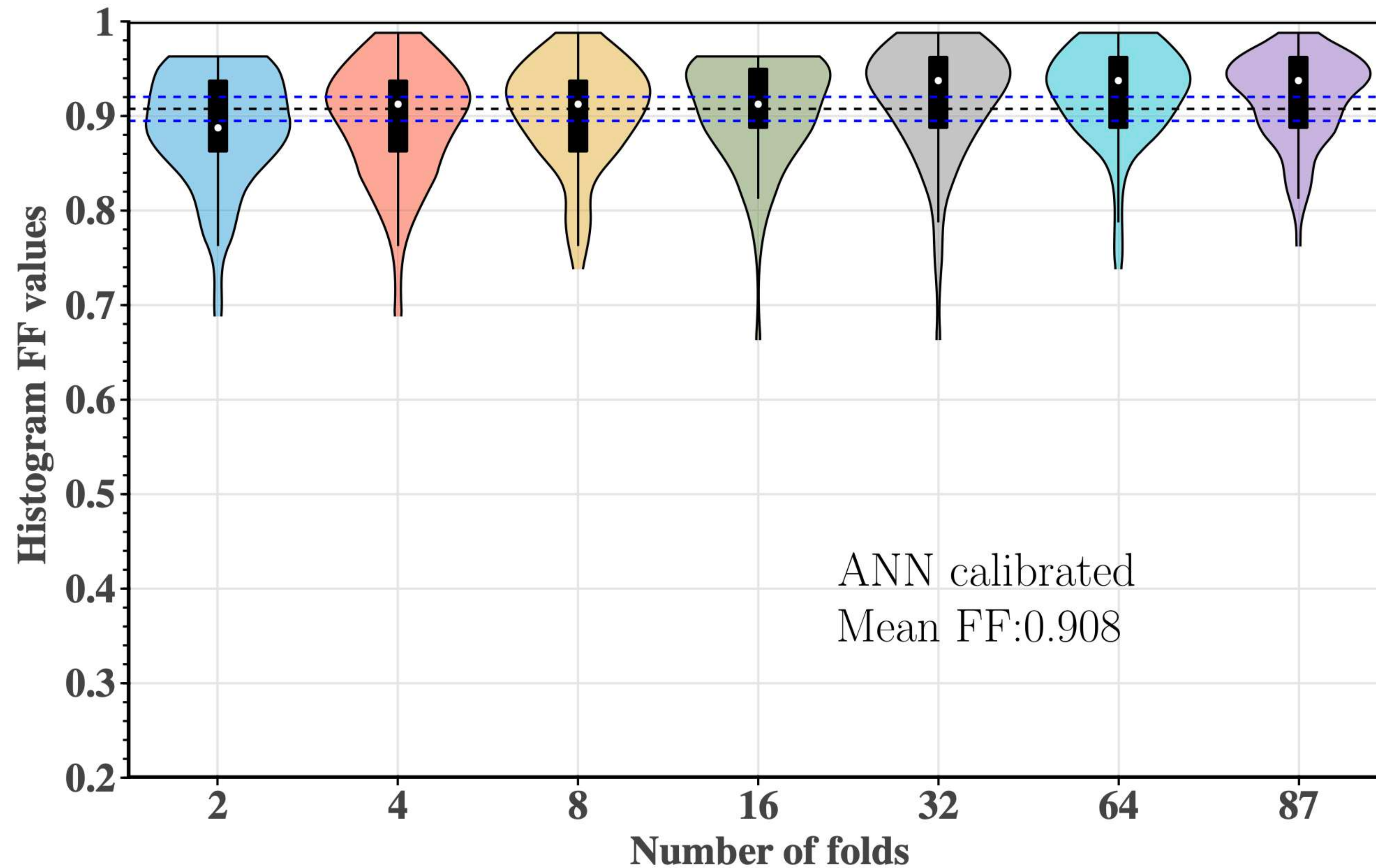
Impact of uncertainty in empirical relation offset by re-calibration of spectra.

ANN outperforms multivariate linear regression.



ANN SURROGATE IN THE FREQUENCY DOMAIN

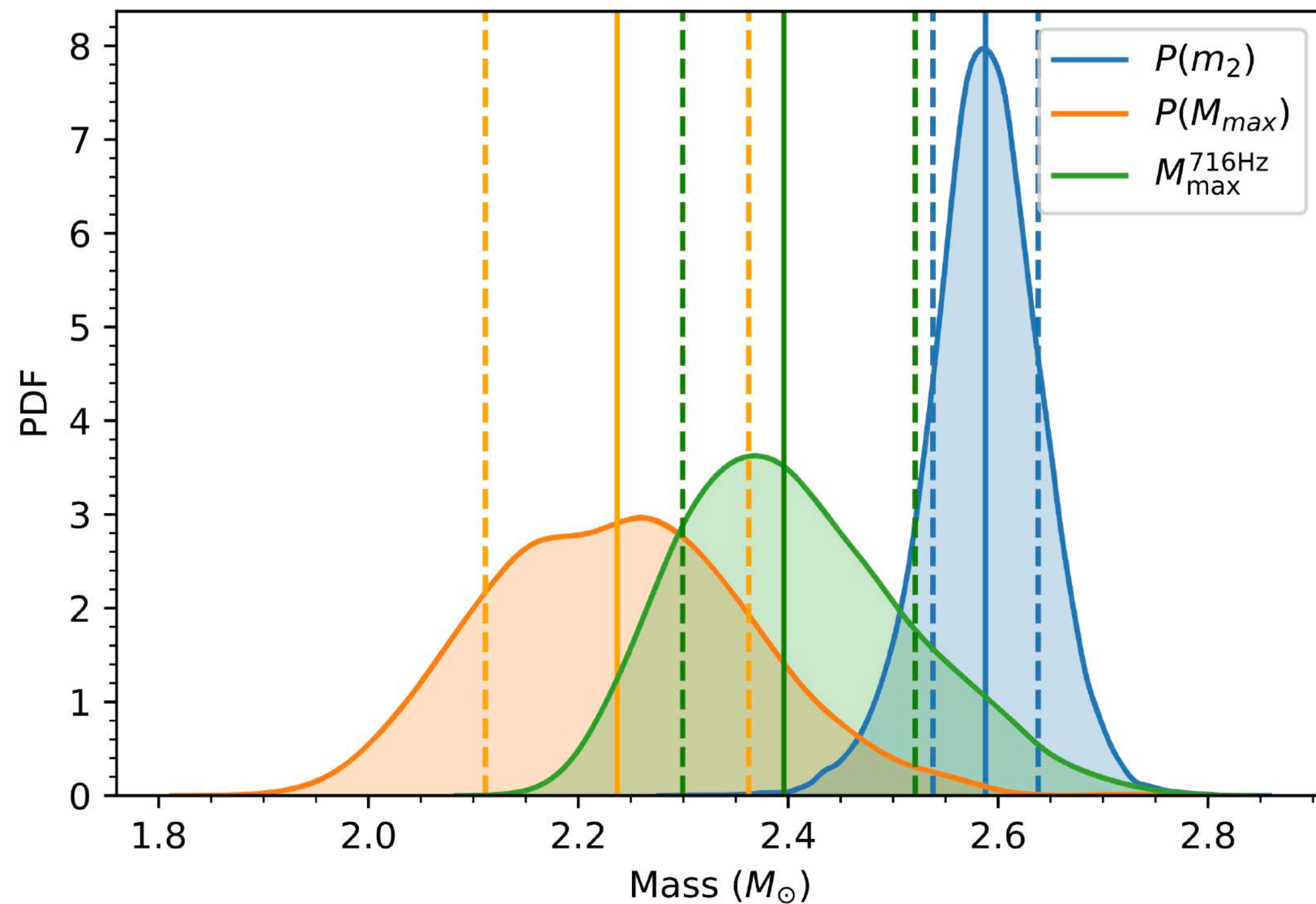
Cross-validation study of fitting factors distribution:



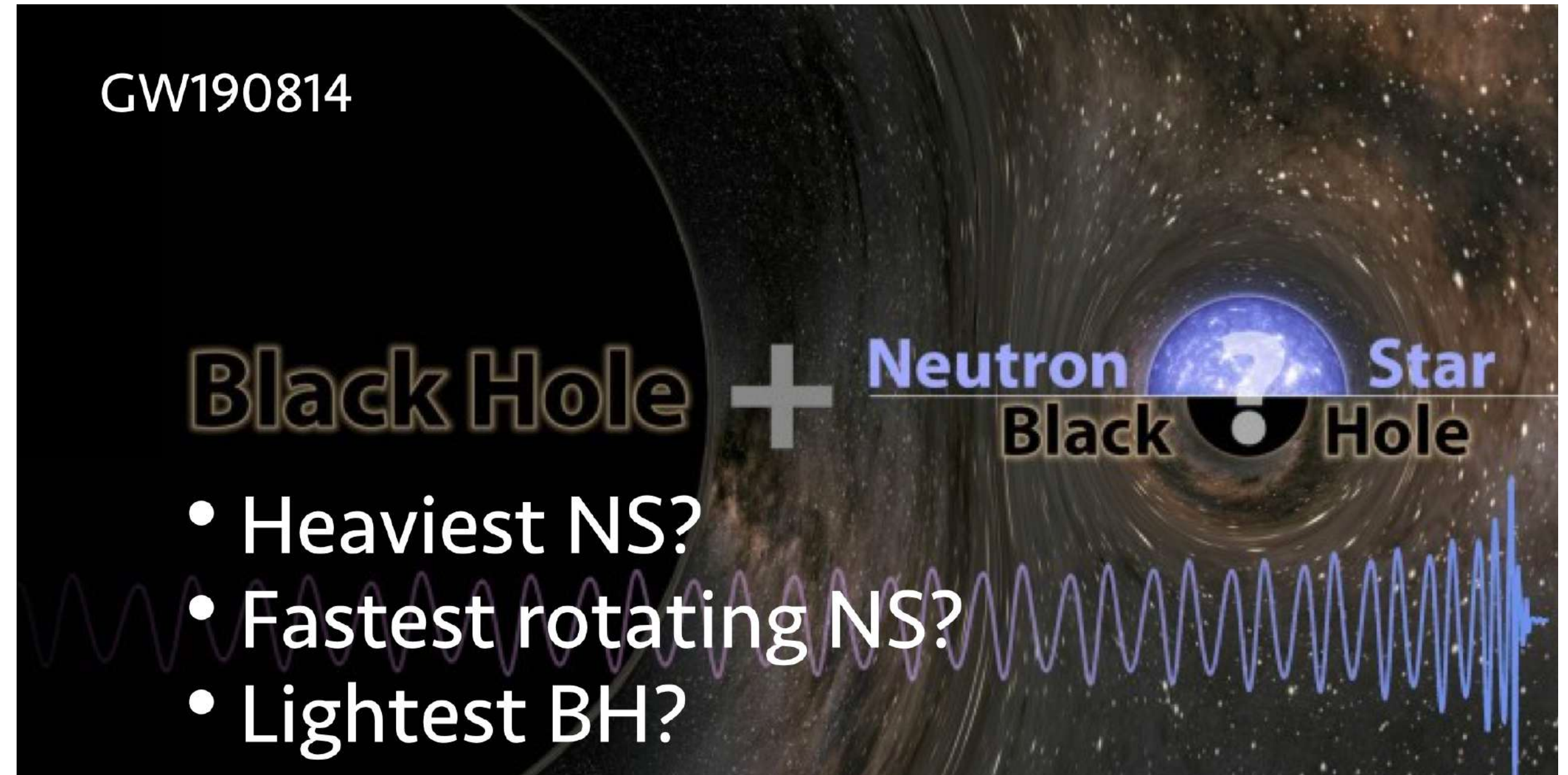
PART C.
NEUTRON STAR MODELS IN ALTERNATIVE
THEORIES OF GRAVITY

HIGH MASS NEUTRON STARS?

What was the nature of the lighter component in GW190814?

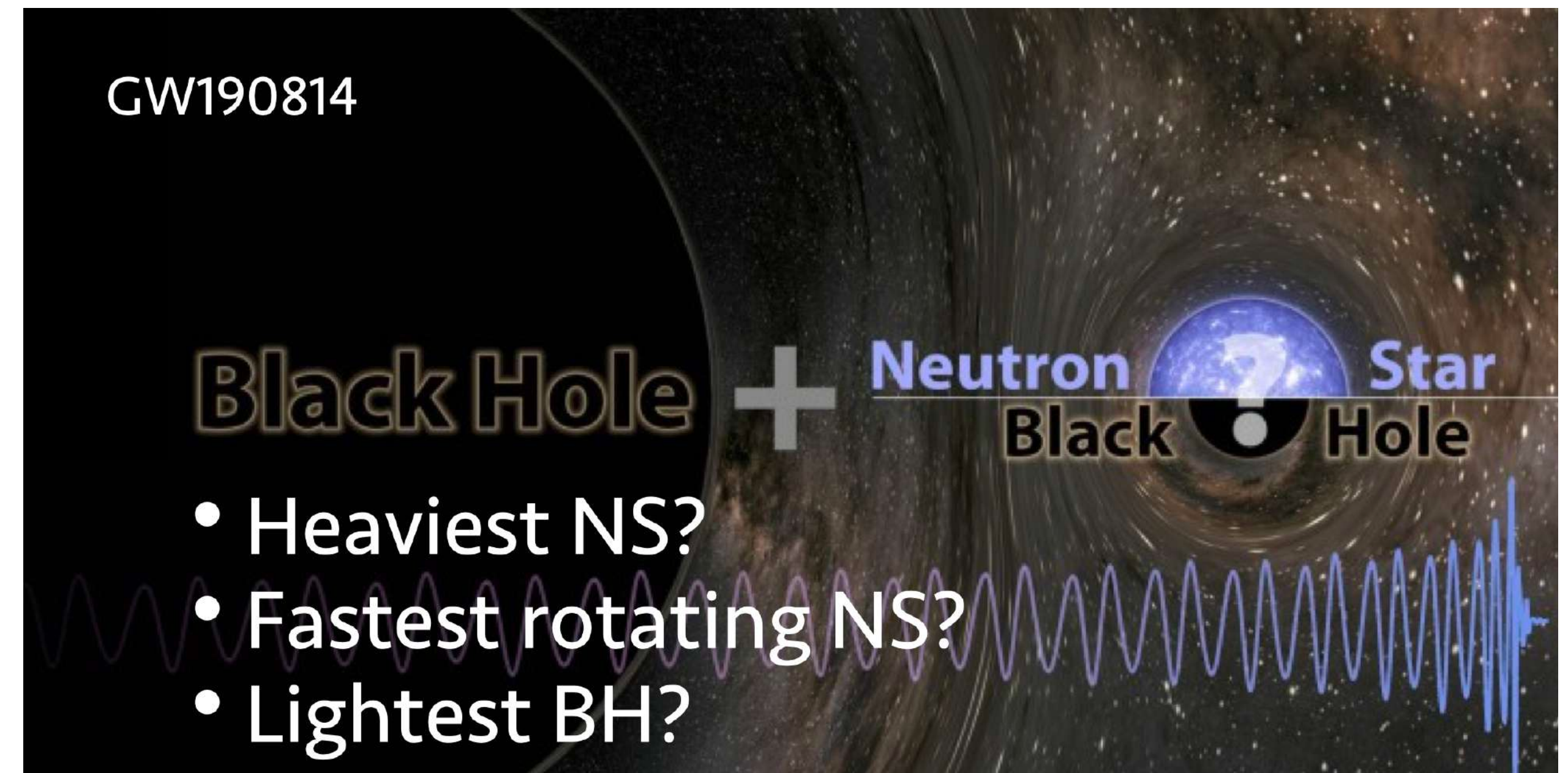
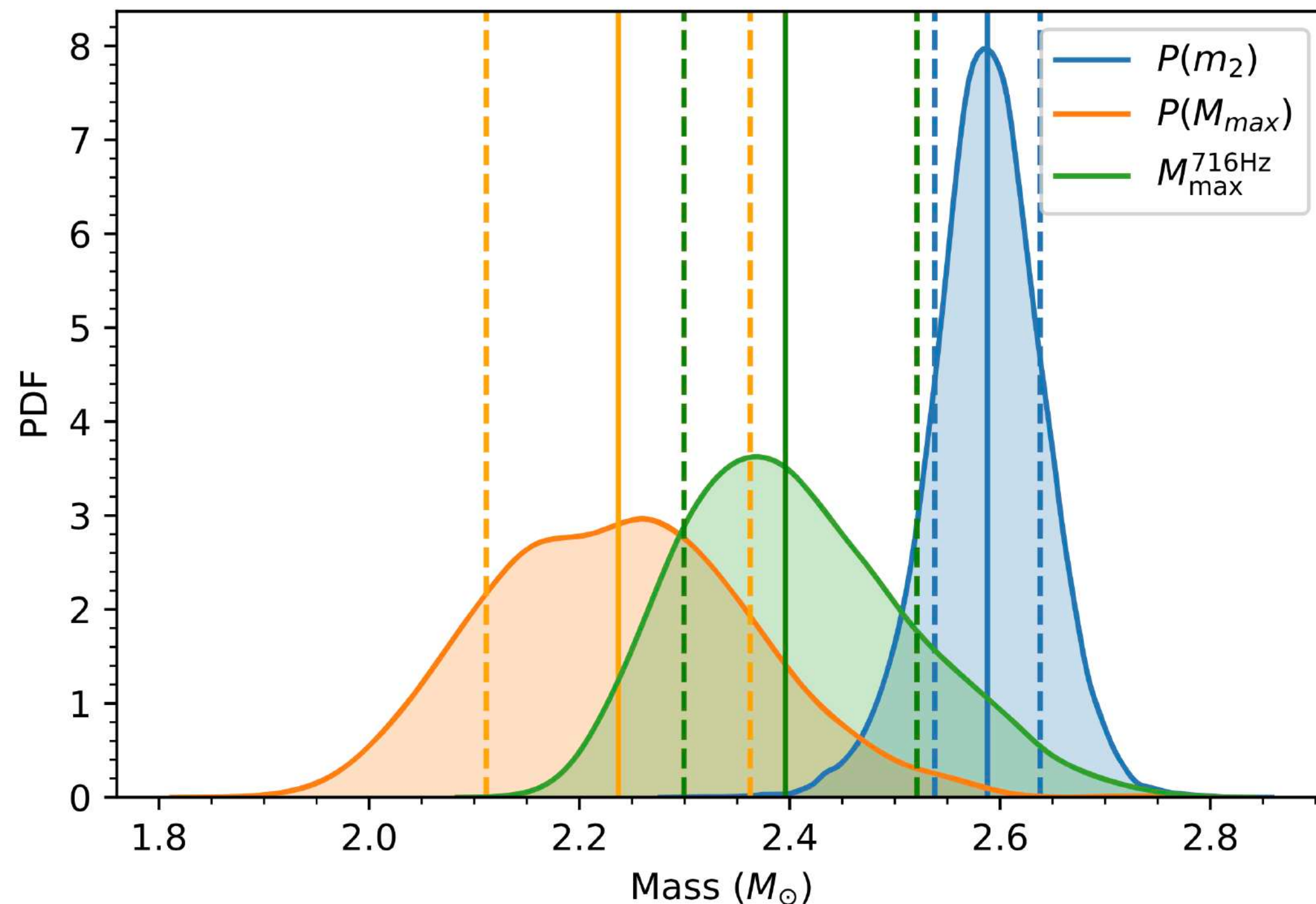


Biswas, Nandi, Char, Bose, Stergioulas (2021)



HIGH MASS NEUTRON STARS?

What was the nature of the lighter component in GW190814?



Biswas, Nandi, Char, Bose, Stergioulas (2021)

Another possibility: if the correct theory of gravity is not GR, then heavier NS might exist!

How can this degeneracy be resolved?

We consider the action

$$S = \frac{1}{2\kappa} \int d^4x \sqrt{-g} \{ R + \alpha [\phi \mathcal{G} + 4G_{\mu\nu} \nabla^\mu \phi \nabla^\nu \phi - 4(\nabla \phi)^2 \square \phi + 2(\nabla \phi)^4] \} + S_m$$

where $\kappa = 8\pi G/c^4$, $\mathcal{G} = R^2 - 4R_{\mu\nu}R^{\mu\nu} + R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}$ is the Gauss-Bonnet scalar and S_m is the matter Lagrangian.

This theory possesses an exact vacuum solution describing nonrotating, static black holes with line element

$$ds^2 = -h(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\Omega^2$$

where

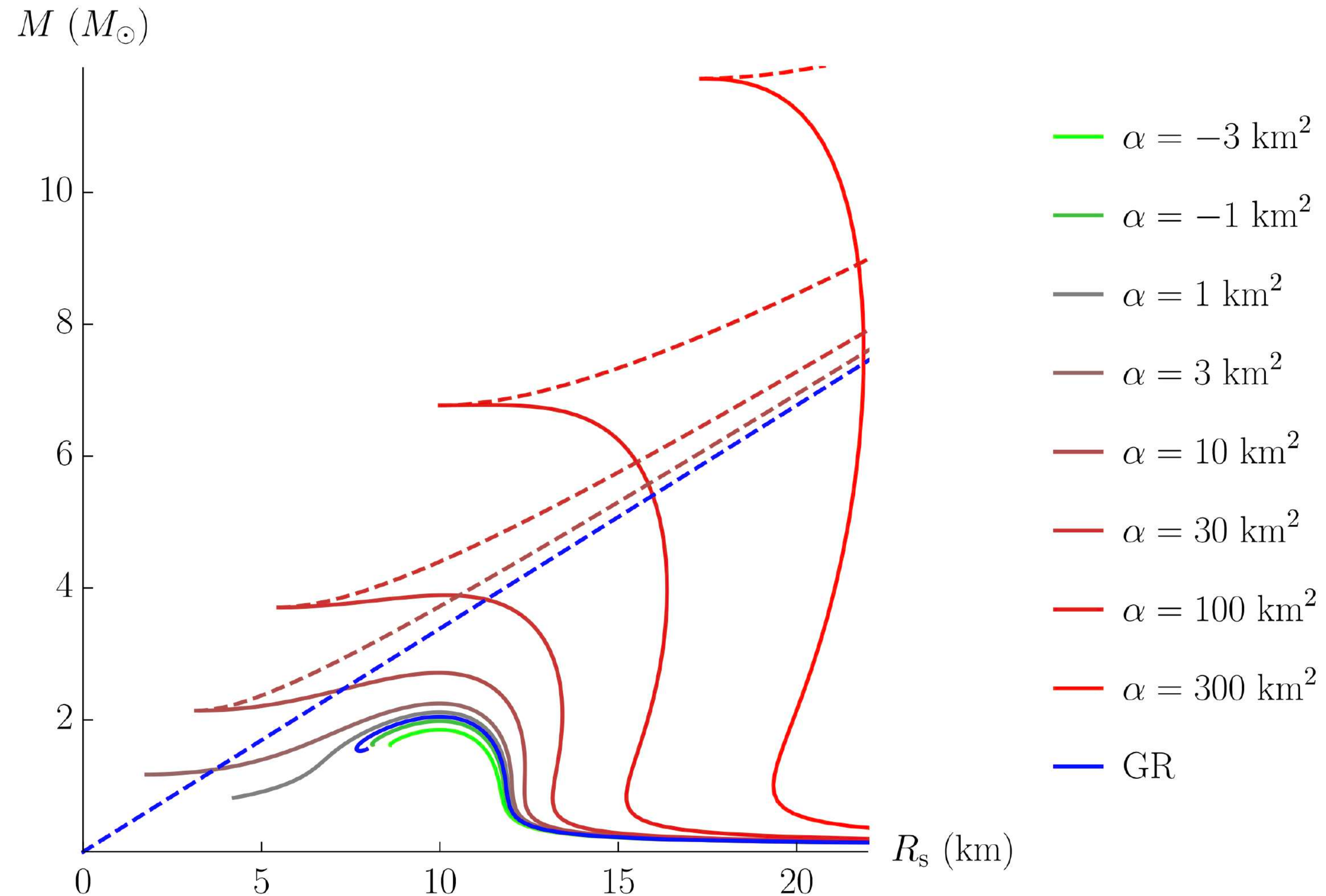
$$h(r) = f(r) = 1 + \frac{r^2}{2\alpha} \left(1 - \sqrt{1 + \frac{8\alpha M}{r^3}} \right) \quad (M \rightarrow \text{ADM mass})$$

and the shift-symmetric scalar field is

$$\phi(r) = \int dr \frac{\sqrt{f}-1}{r\sqrt{f}}$$

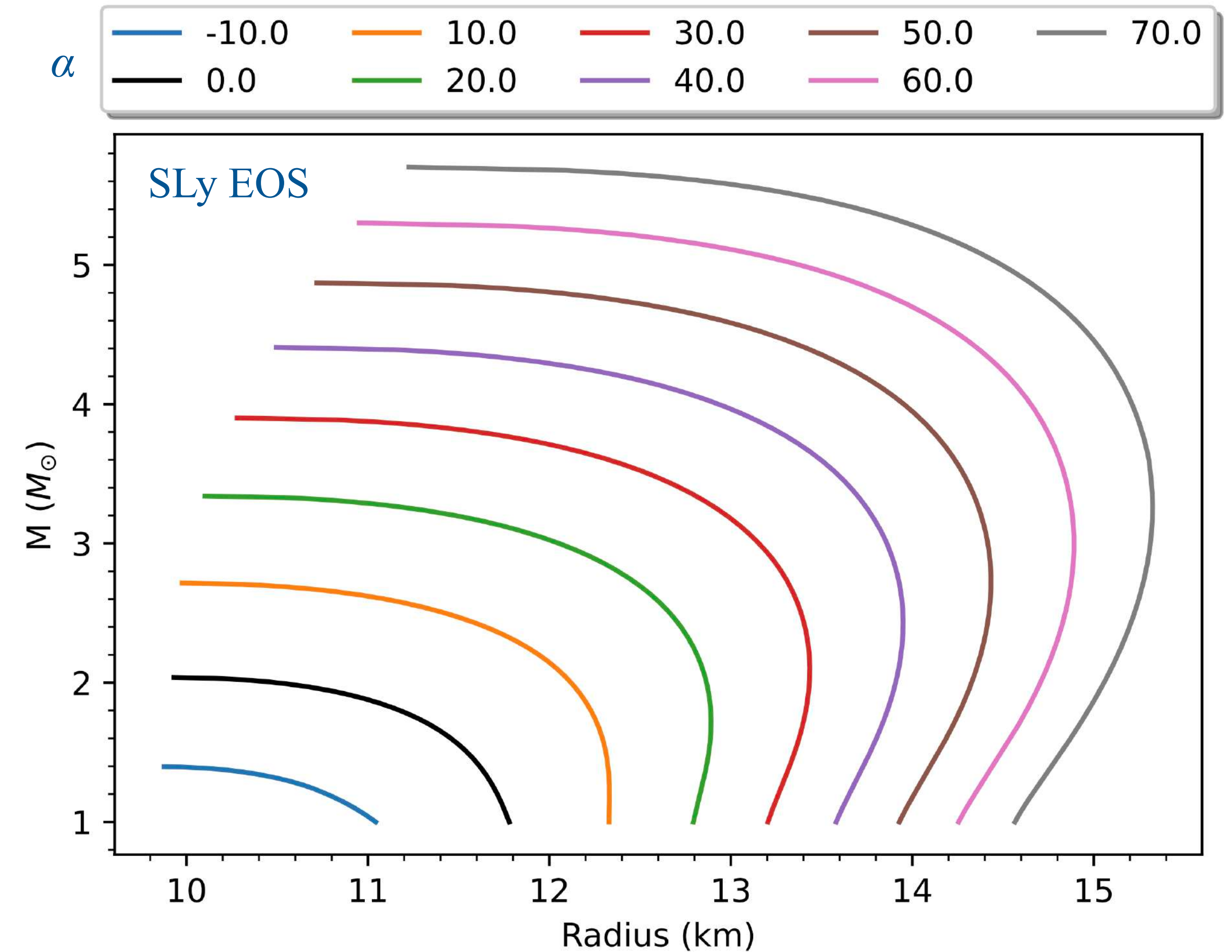
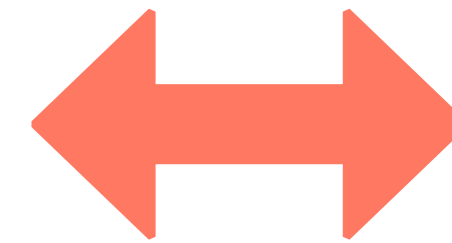
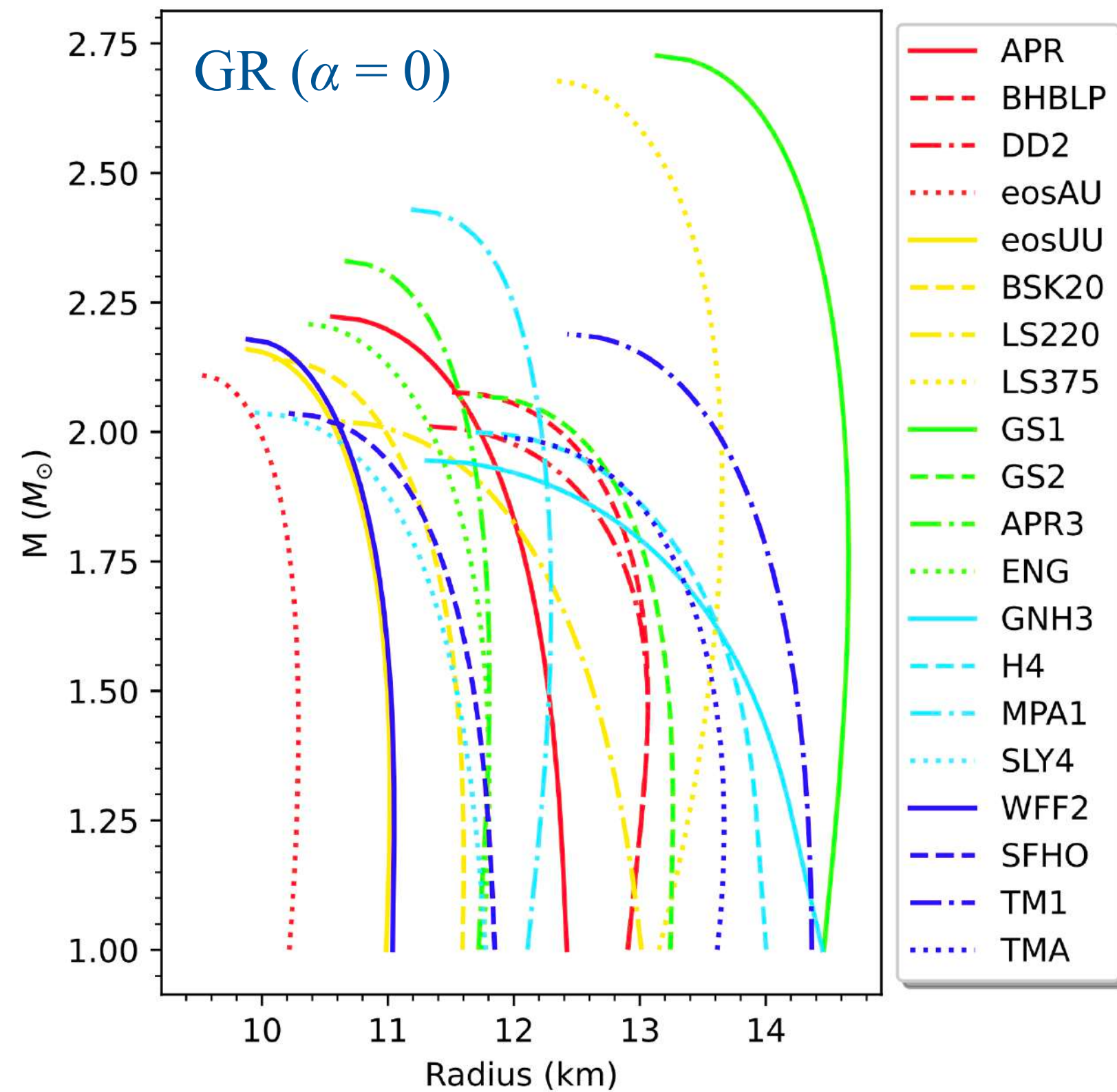
SEQUENCES OF EQUILIBRIUM MODELS

For the **SLy EOS**, we show representative cases of sequences of NS equilibrium models (solid lines) and BHs (dashed lines). For $\alpha > 0$, the NS solutions merge with the minimum mass BH solution.



EOS-GRAVITY DEGENERACY

In this theory, constructing equilibrium sequences for the same EOS, but different α , mimics the effect of using different EOS in GR.



Need to use a large number of observations to break the degeneracy!

ANN SURROGATE MODELS FOR NUMERICAL SOLUTIONS

EOS collection

Name	Number #
APR	1
BHBLP	2
DD2	3
eosAU	4
eosUU	5
BSk20	6
LS220	7
LS375	8
GS1	9
GS2	10
APR3 (PP)	11
ENG (PP)	12
GNH3 (PP)	13
H4 (PP)	14
MPA1 (PP)	15
SLy4 (PP)	16
WFF2 (PP)	17
SFHo	18
TM1	19
TMA	20

Surrogate models

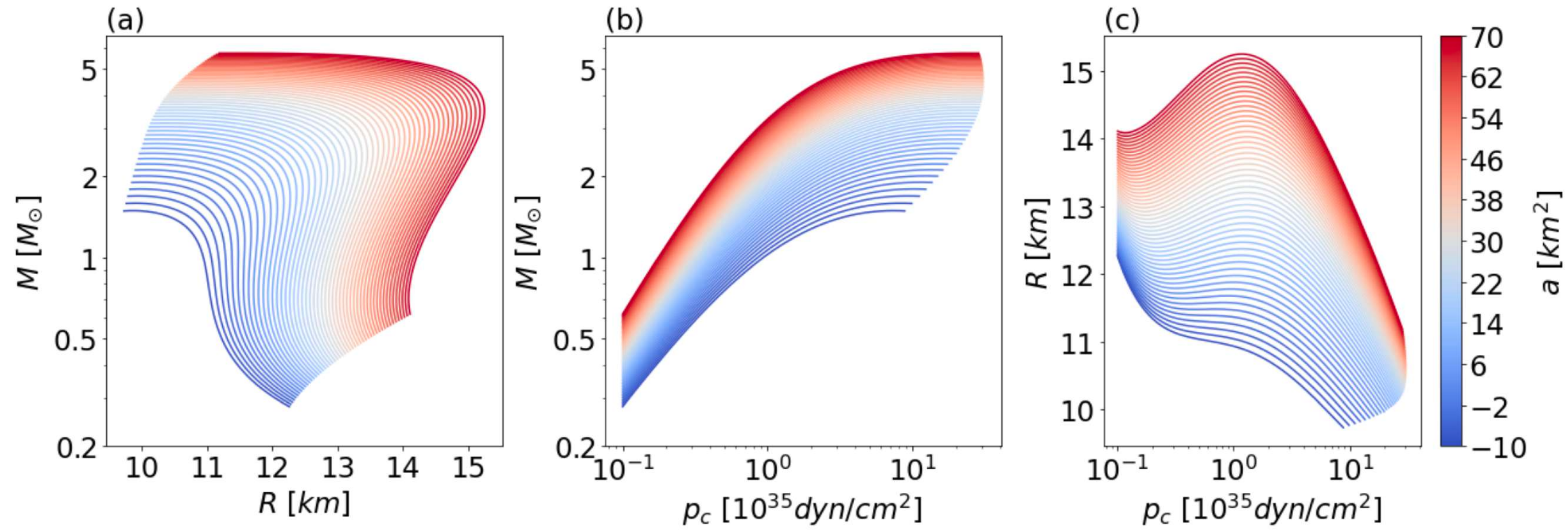
$$f_1(\text{EoS}; \alpha, p_c) \rightarrow (M, R)$$

$$f_2(\text{EoS}; \alpha, M) \rightarrow R$$

Network architecture for each EOS

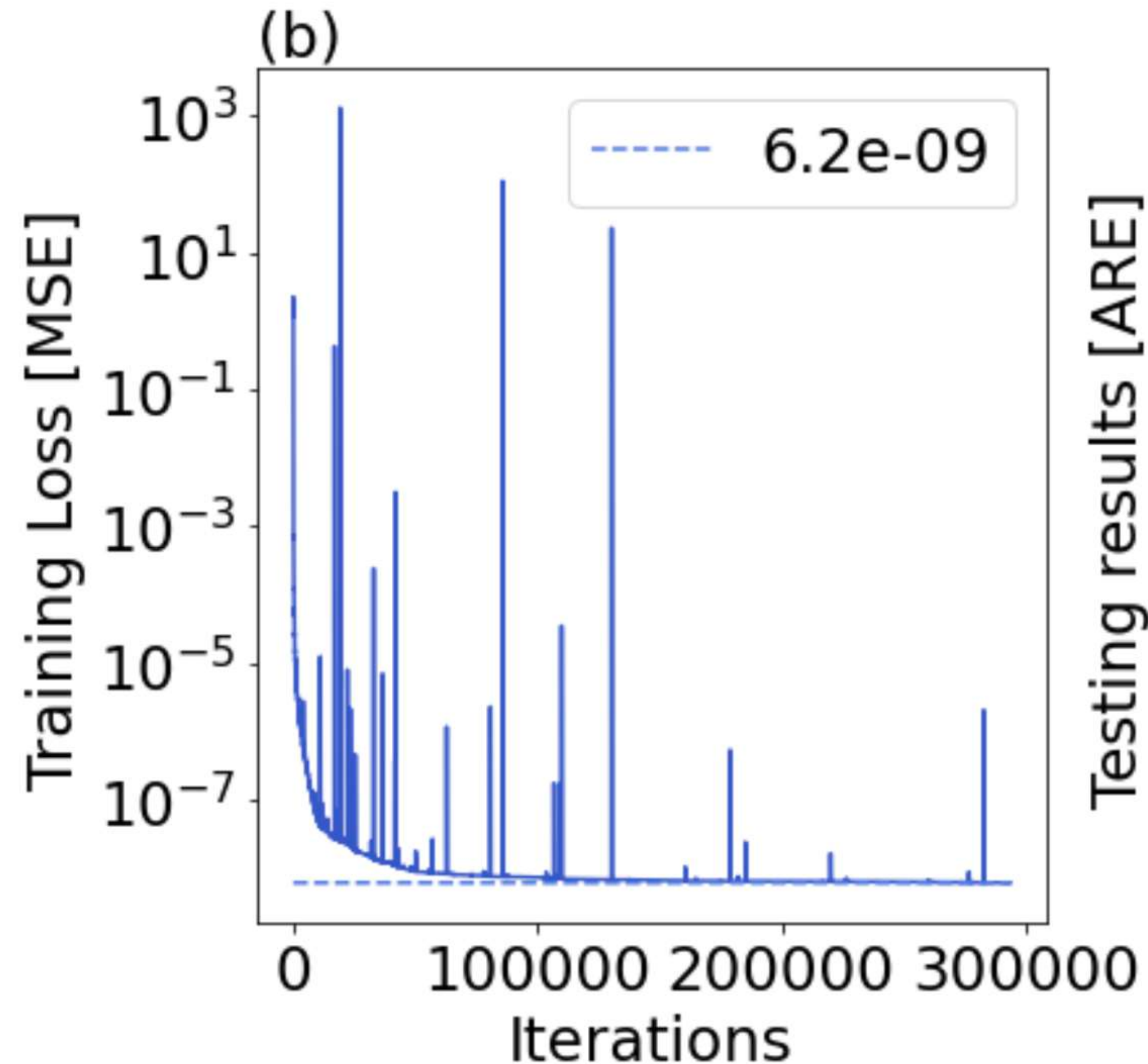
Layer	Type f_1	Type f_2
Input layer	(α, p_c)	(α, M)
Hidden layer 1	25-tanh	25-tanh
Hidden layer 2	35-relu	35-relu
Hidden layer 3	25-tanh	25-tanh
Output layer	(M, R)	R

Training set for each EOS: 200 (p_c) x 51 (α) = 10200 equilibrium models

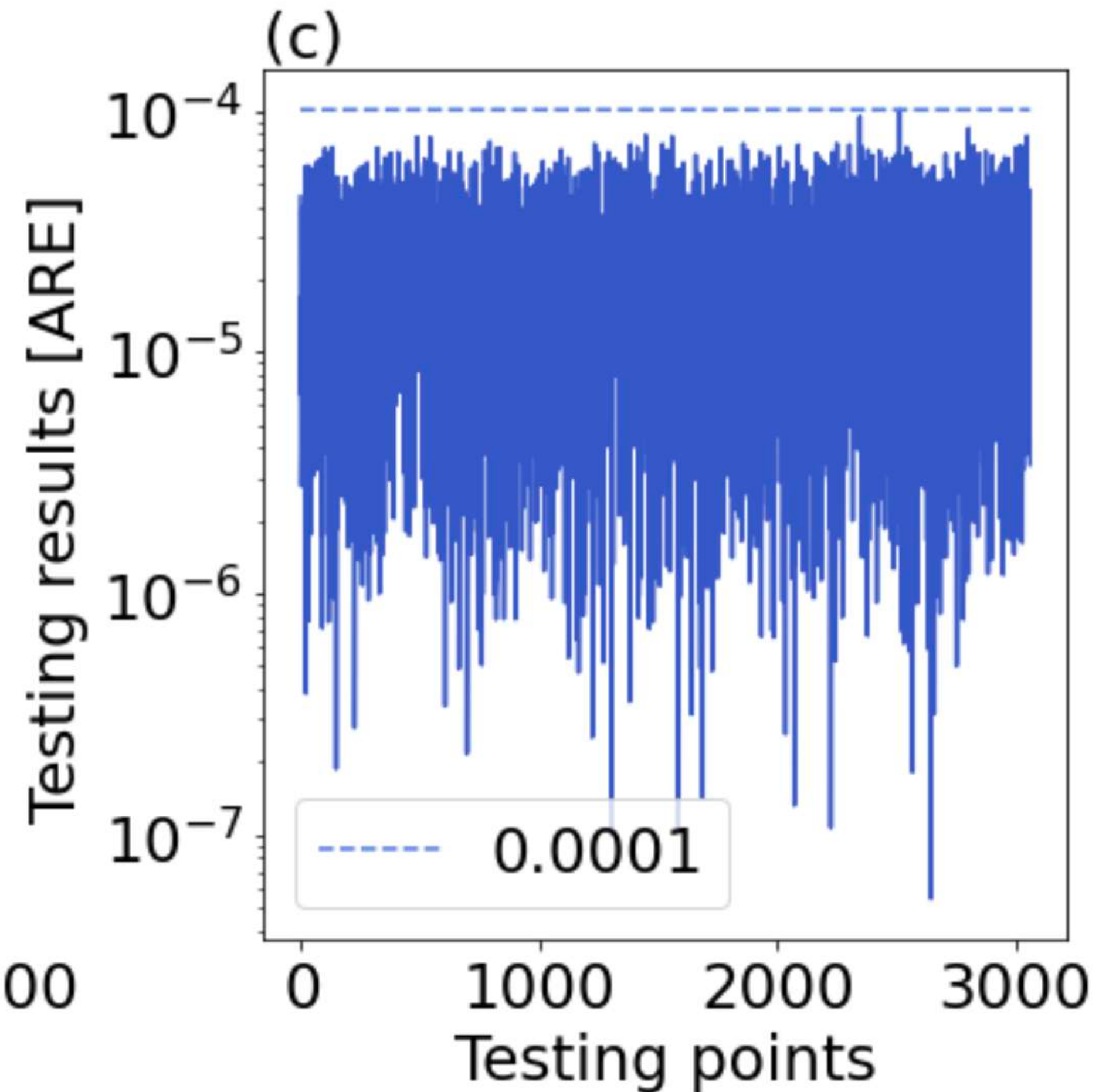


ACCURACY OF f_1 ANN SURROGATE MODEL FOR EOS BSk20

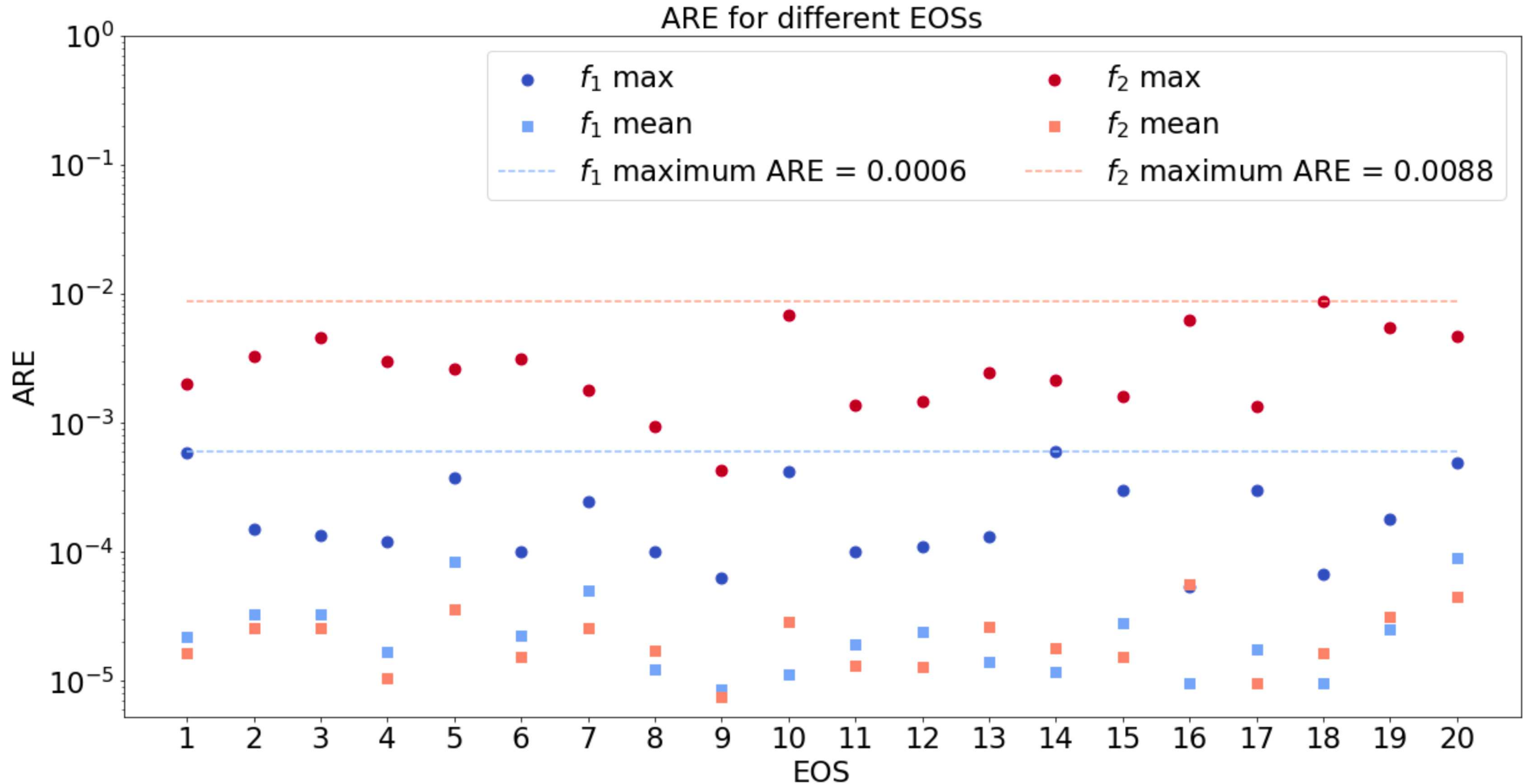
Loss function:
Mean Square Error (MSE)



Accuracy test:
Absolute Relative Error $\text{ARE}_i = \frac{1}{m} \sum_{j=1}^m \left| \frac{Y_i^j - Y_{i,\text{true}}^j}{Y_{i,\text{true}}^j} \right|$



ACCURACY OF ANN SURROGATE MODELS FOR ALL EOS



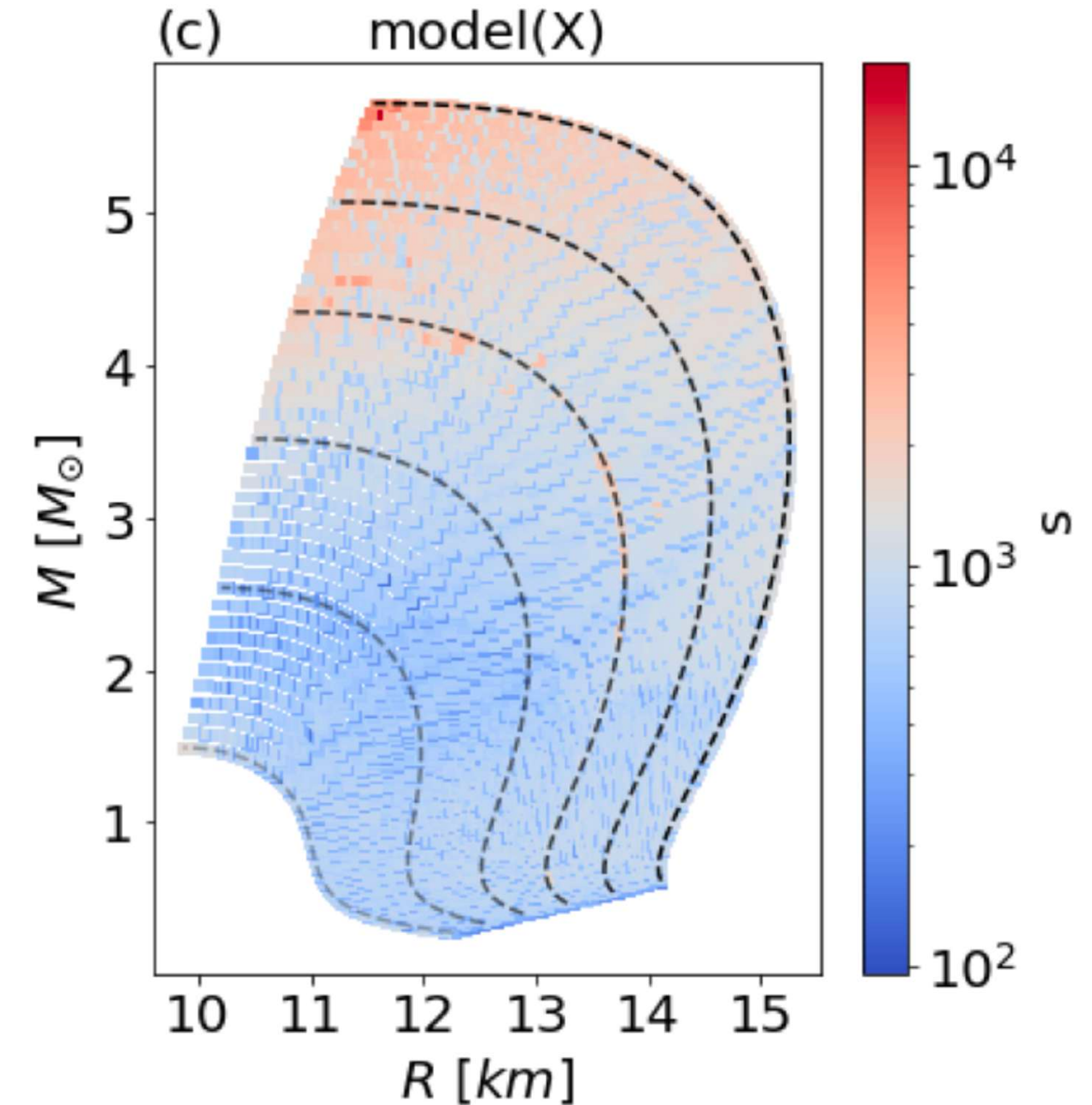
SPEED-UP ACHIEVED WITH THE ANN SURROGATE MODELS

Speed-up of ANN surrogate model compared to original numerical code

$$s = \frac{\Delta t_{\text{ANN}}}{\Delta t_{\text{num}}}$$

Numerical code	(Mean)	(Min)	(Max)
run time:	1003.5 ms	147.96 ms	18122.4 ms
Output method	Speed Up (Mean)	Speed Up (Minimum)	Speed Up (Maximum)
model.predict(X)	25.12	0.97	464.56
model(X)	921.9	95.6	18102.1
model.predict($\mathbf{X}$)	31295.5	4614.5	565157.2

The achieved speed-up allows for millions of MCMC calls in a Bayesian inference computation with minimal overhead.



RECOVERY OF INJECTED α VALUES

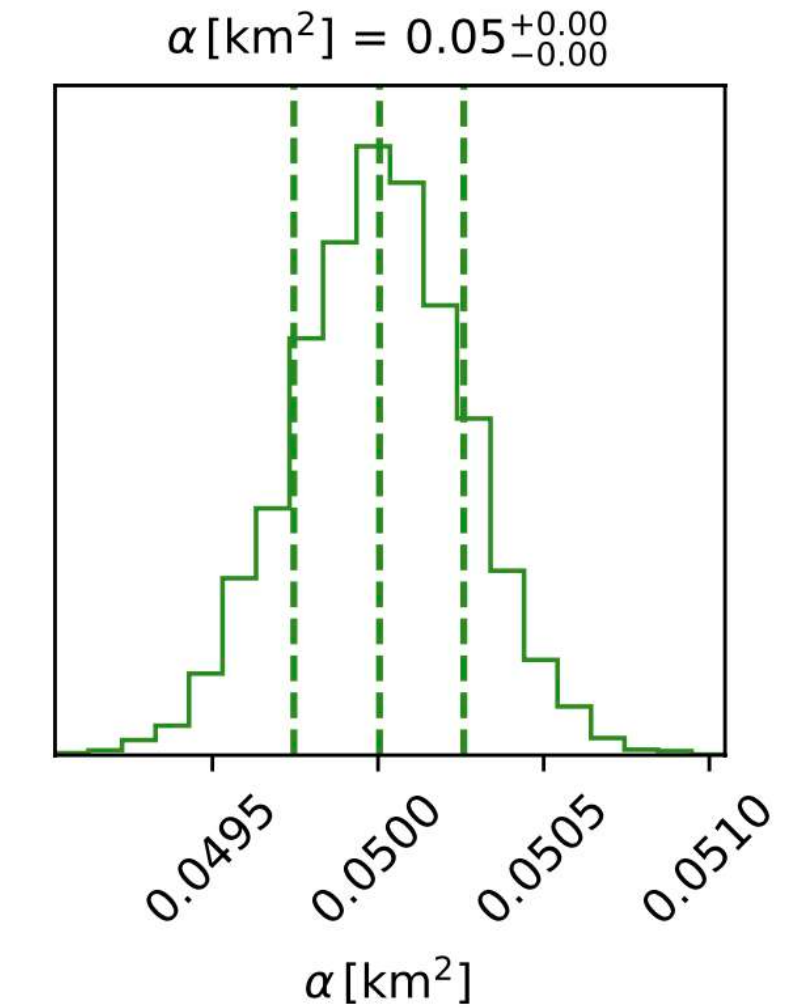
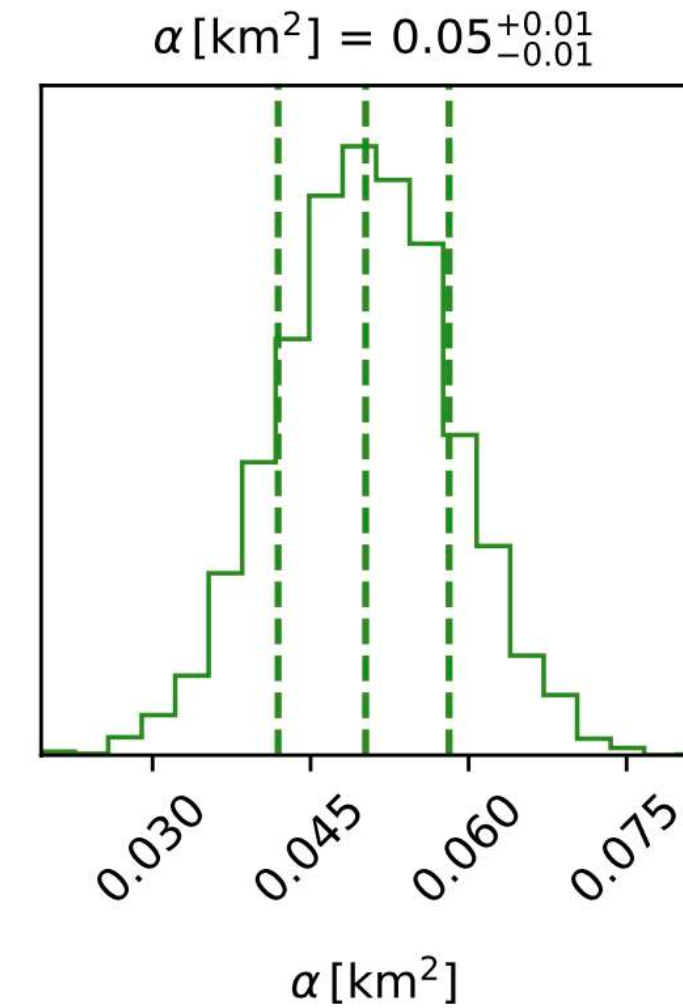
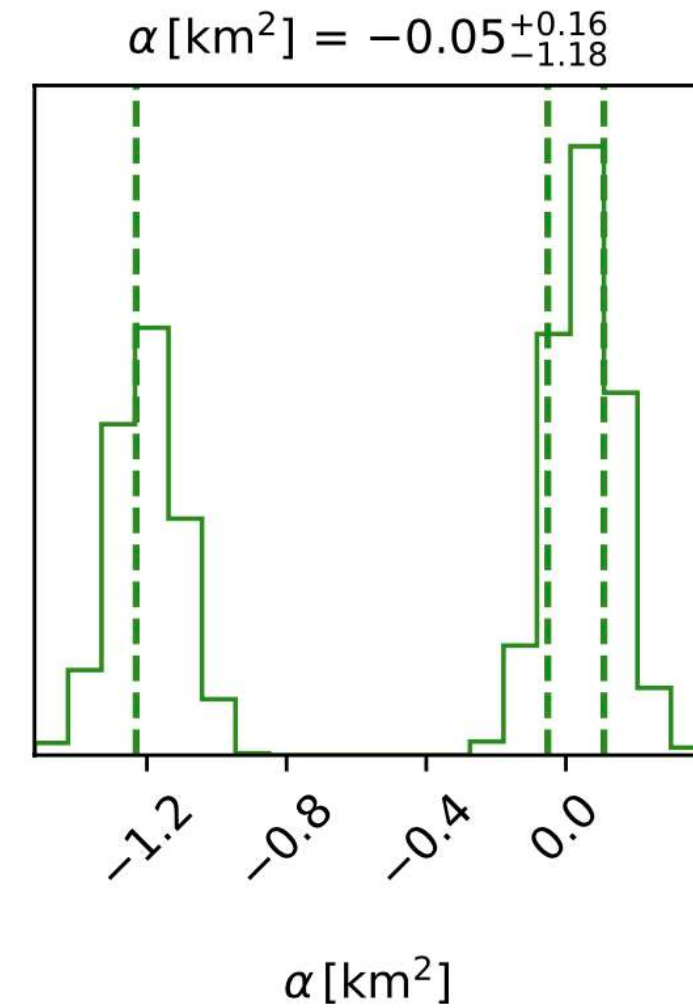
Hierarchical Bayesian Inference using astrophysical constraints for a set of 20 EOS:

A+

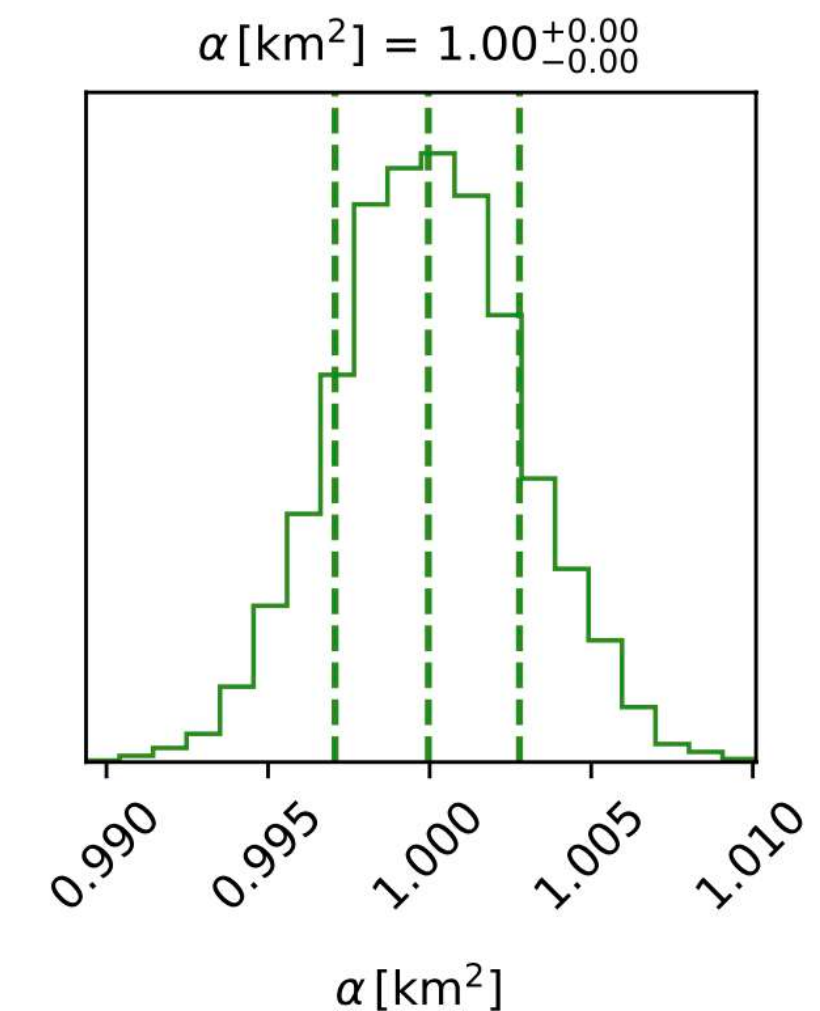
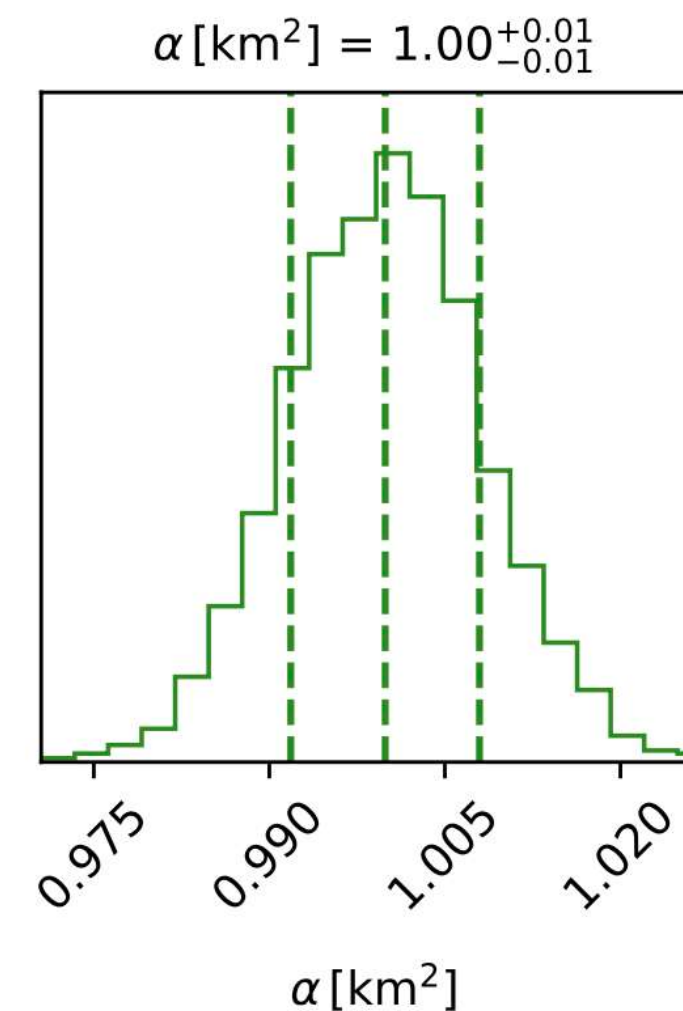
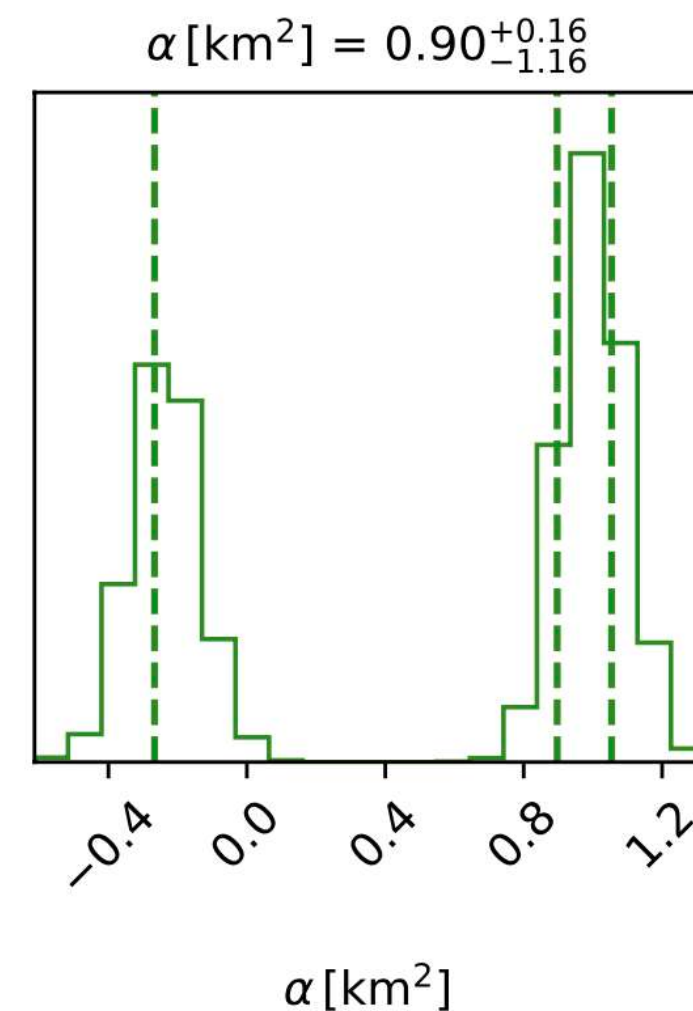
Voyager

3G

$$\alpha = 0.05 \text{ km}^2$$



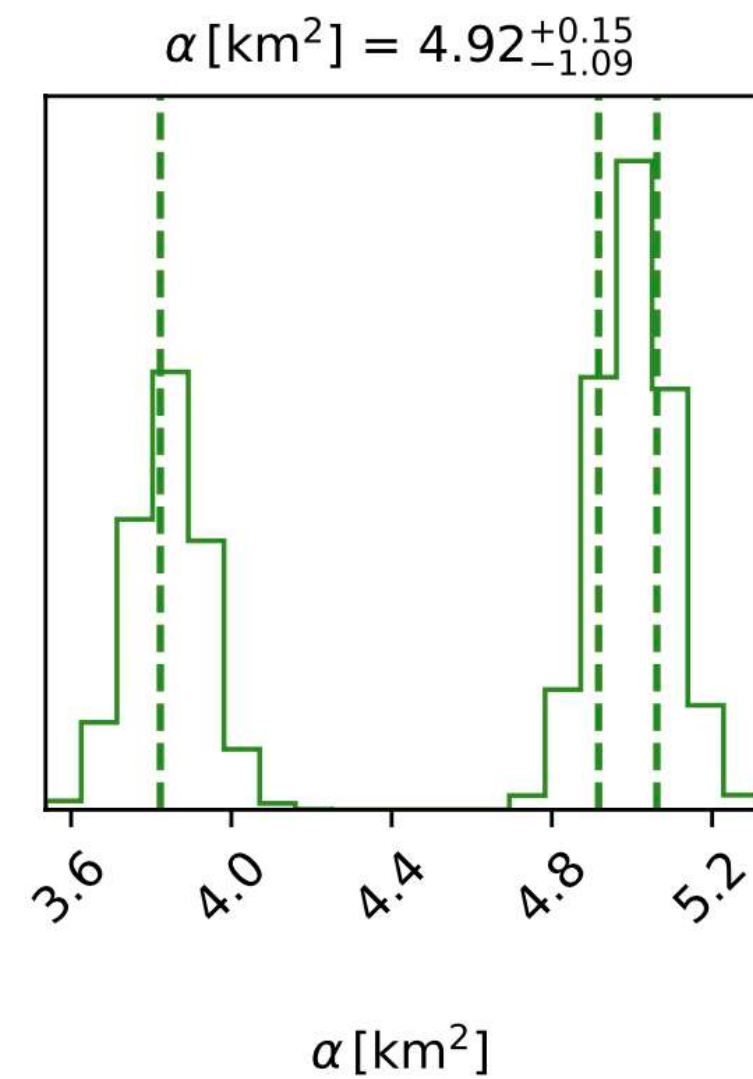
$$\alpha = 1.0 \text{ km}^2$$



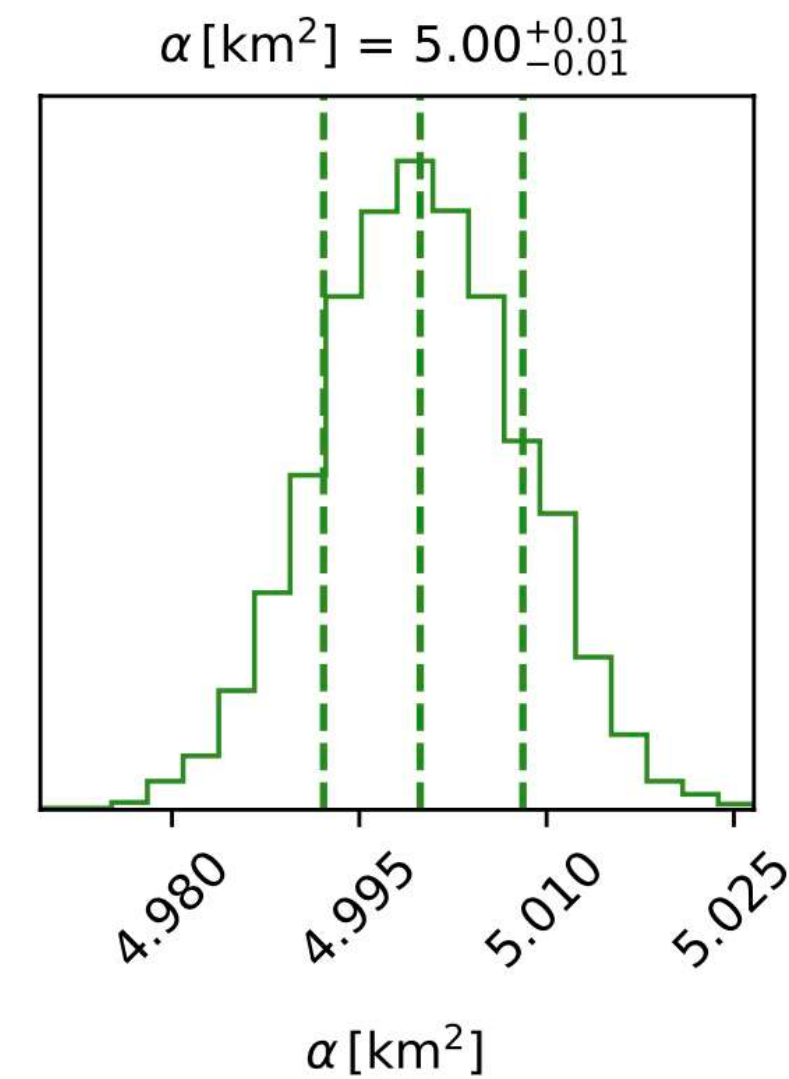
RECOVERY OF INJECTED α VALUES

$$\alpha = 5.0 \text{ km}^2$$

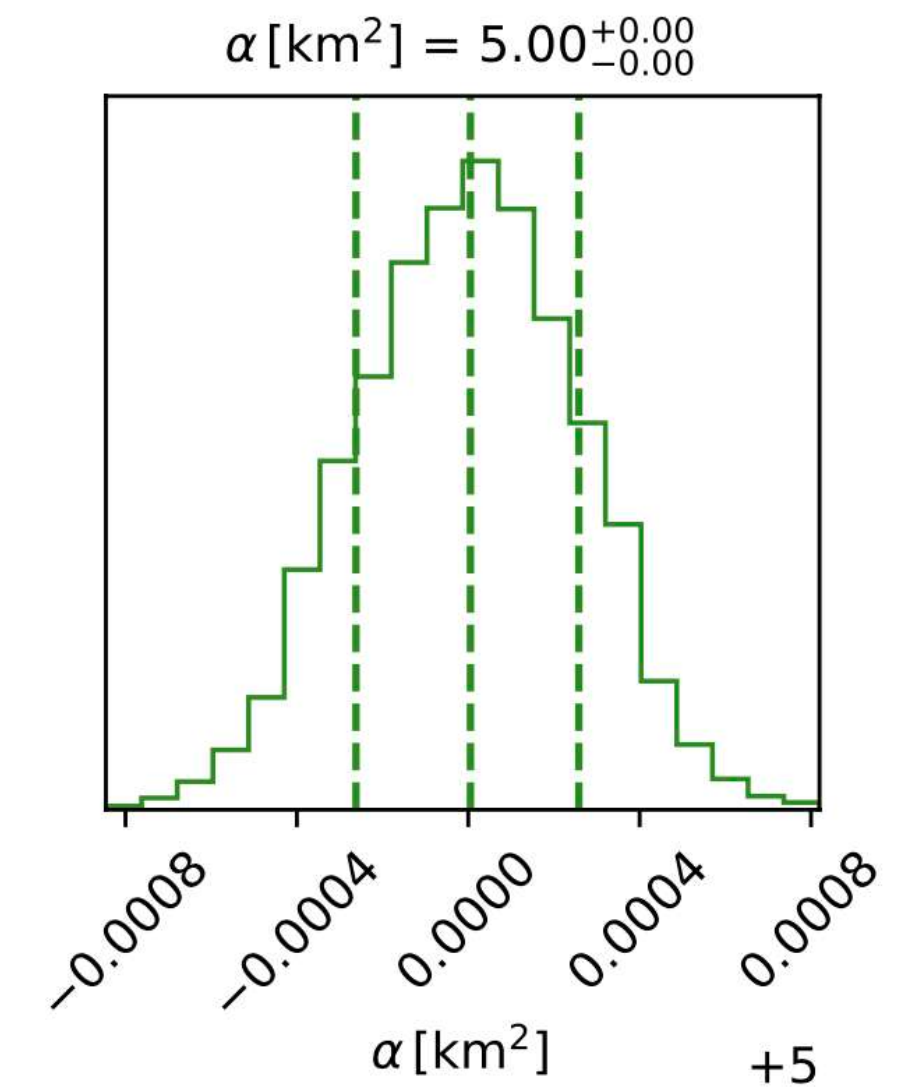
A+



Voyager



3G



A+ : for an injection of $\alpha = 5 \text{ km}^2$, the GR value of $\alpha = 0$ is excluded at the 3σ level.

Voyager/3G : even departures from GR at the $\alpha = 0.05 \text{ km}^2$ level are accurately recovered.

THANK YOU FOR YOUR ATTENTION