

LEVERAGING MACHINE LEARNING FOR GRAVITATIONAL WAVE DISCOVERIES

From Binary Black Hole Mergers to Probing High-Density Nuclear Matter

NIKOLAOS STERGIOULAS

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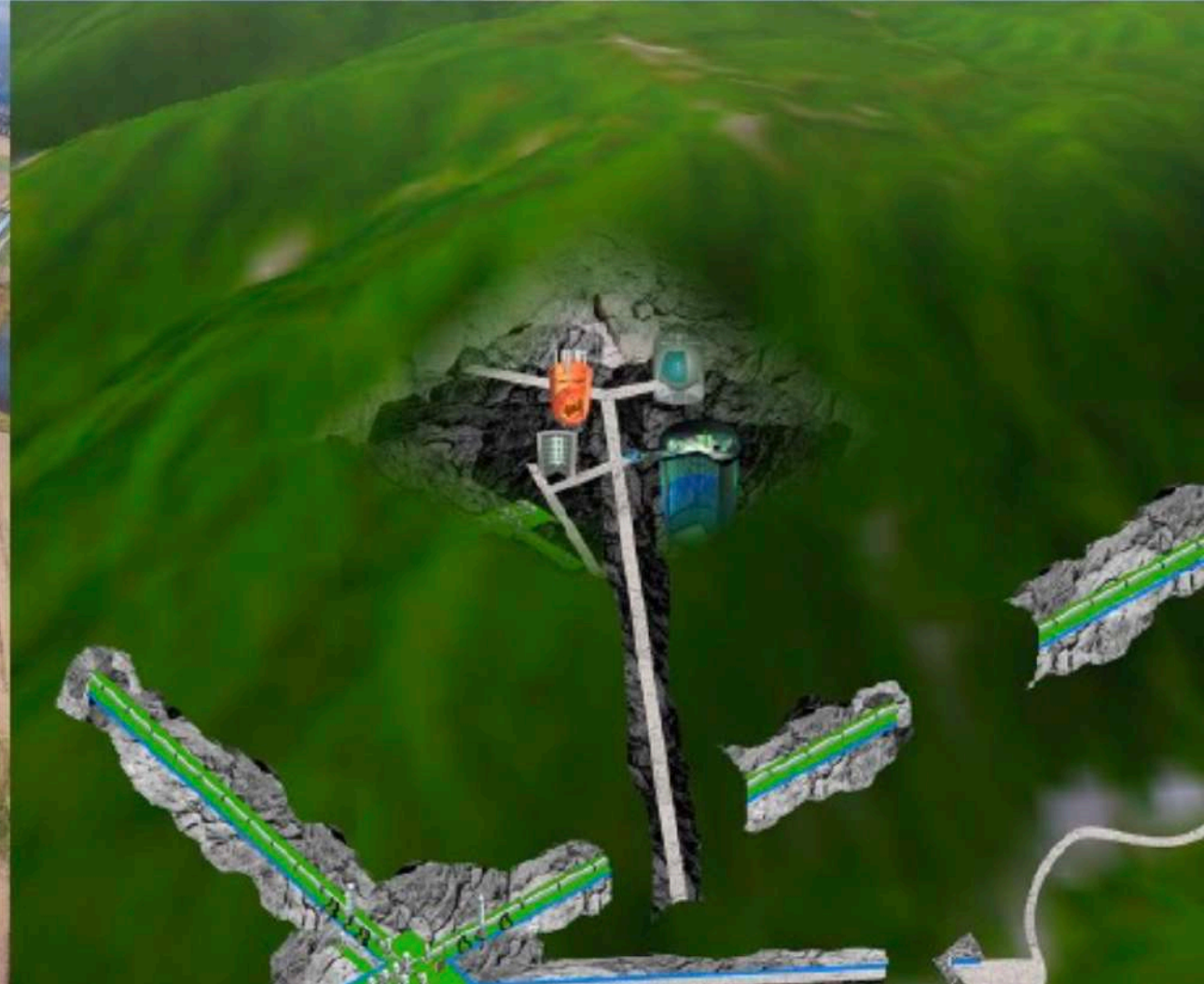


Ministry of Science
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Republic of Poland

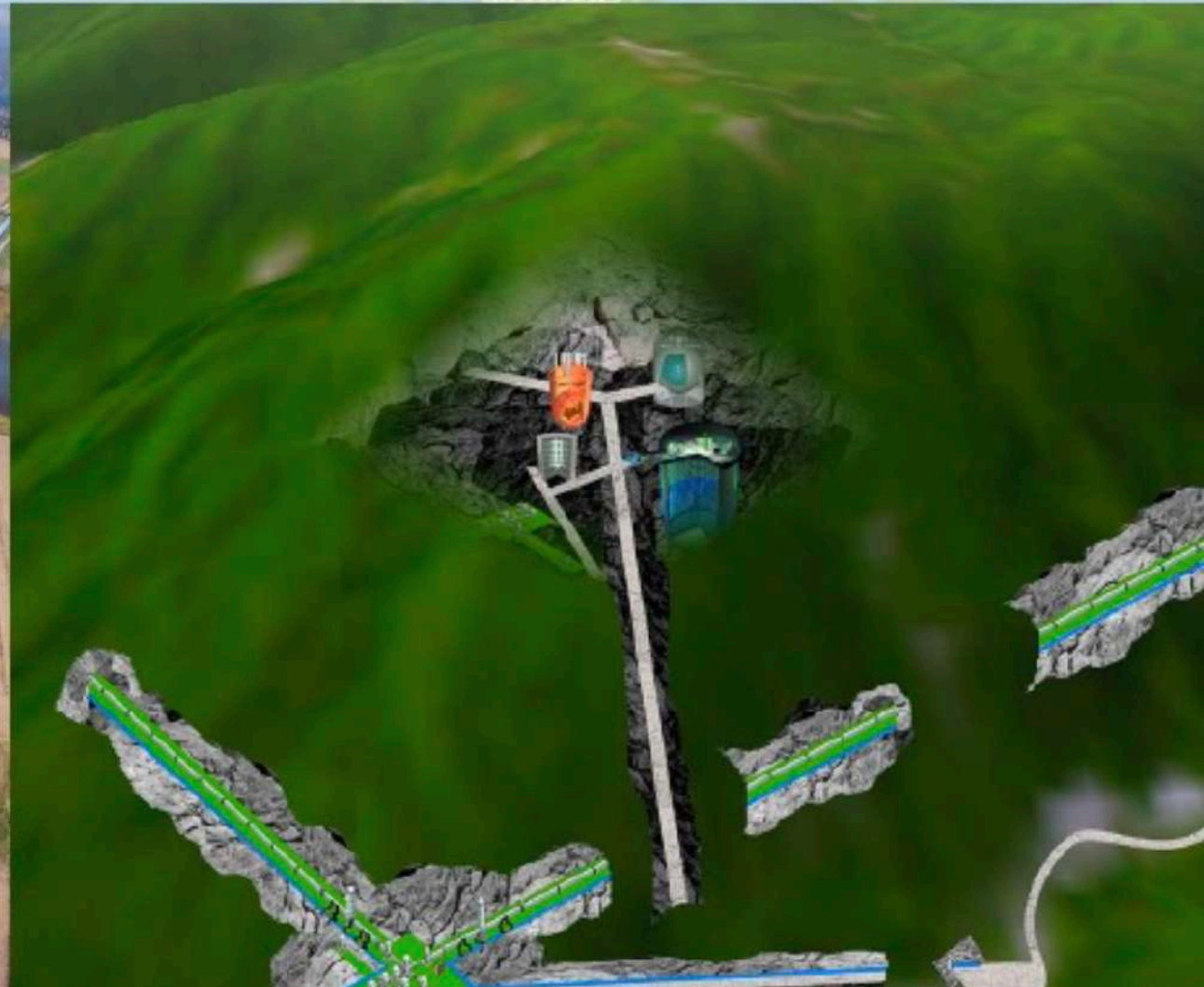
11th Conference of the Polish Society on Relativity, Wrocław, July 21, 2025

PART A. BINARY BLACK HOLE MERGERS

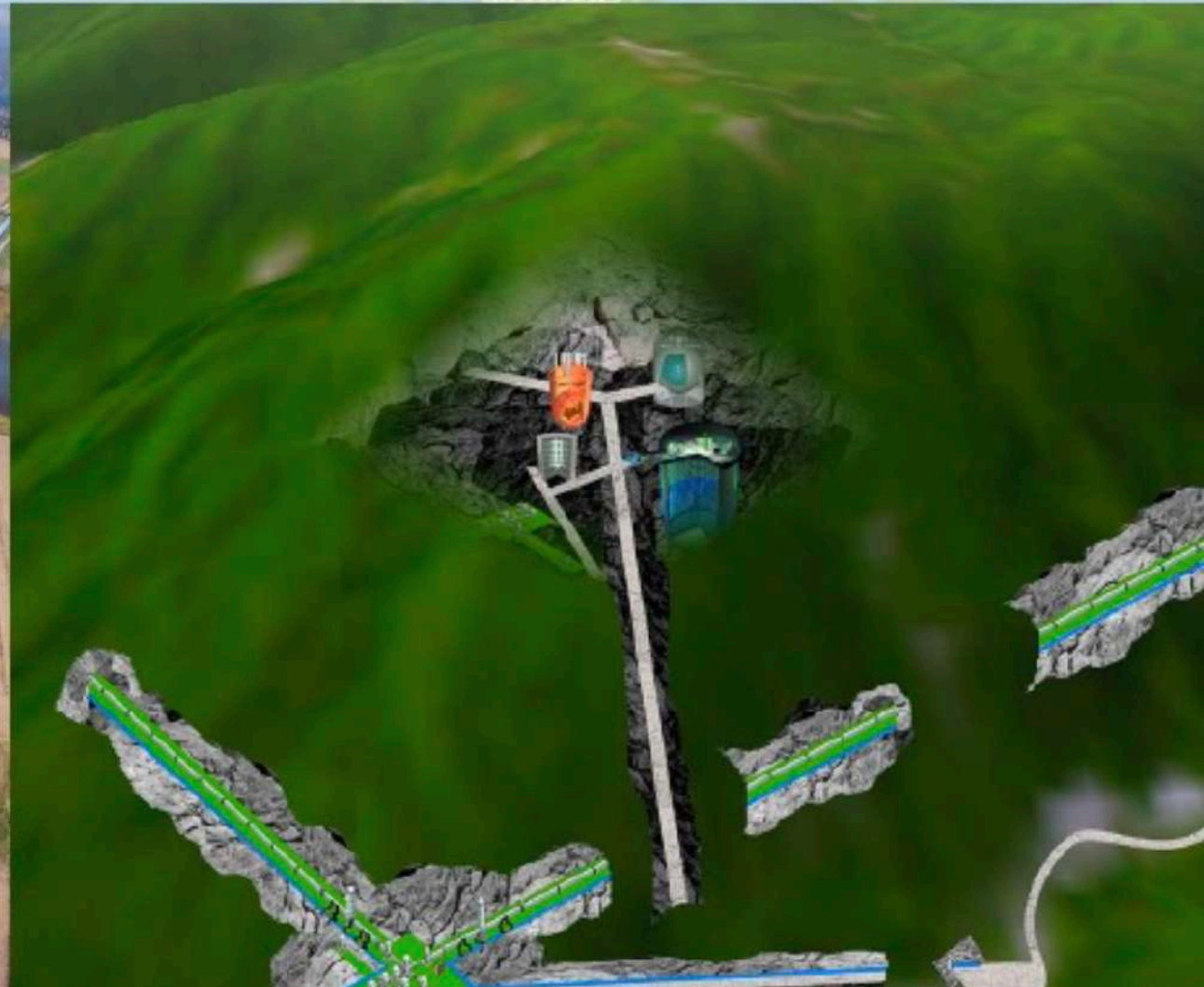
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



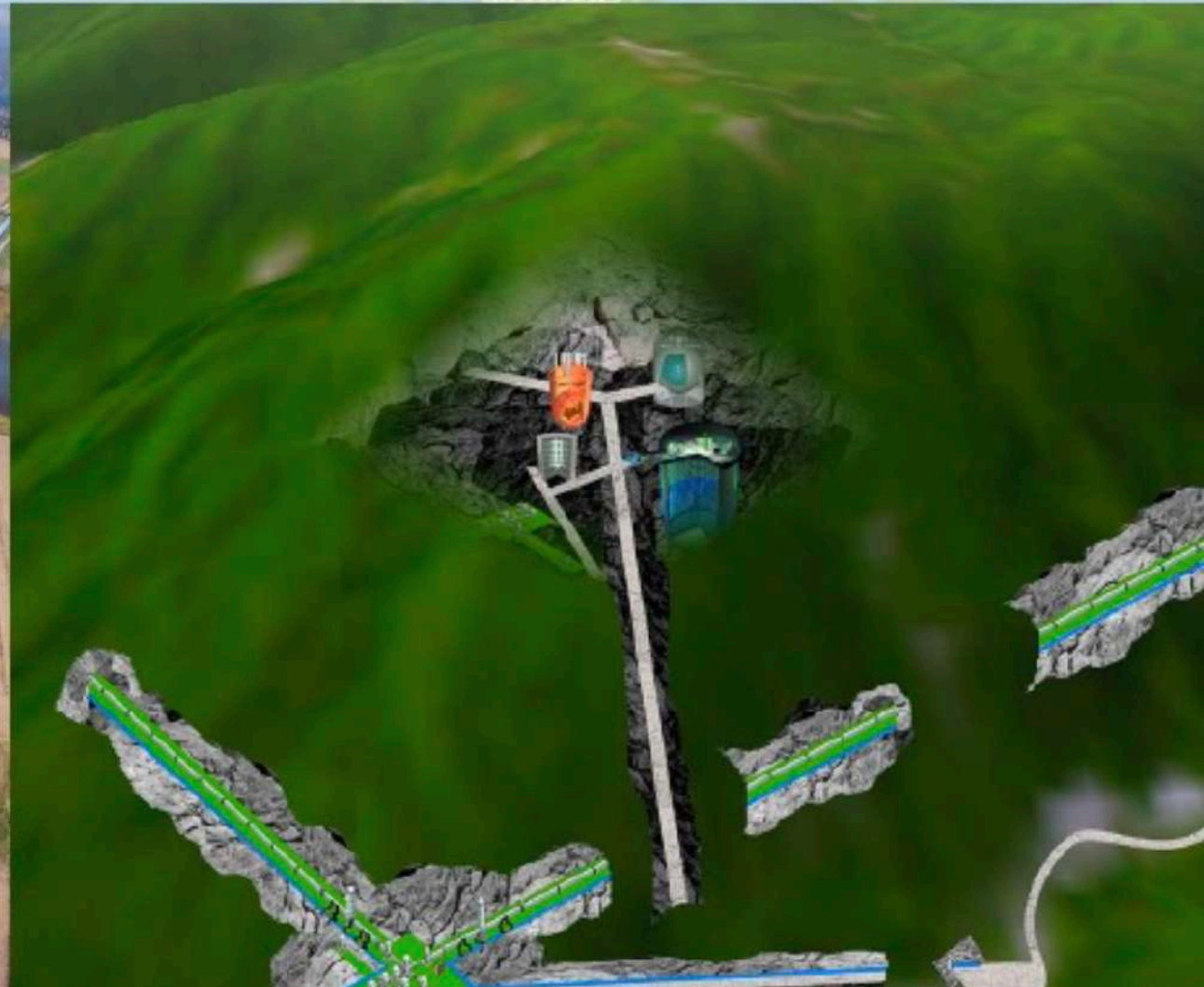
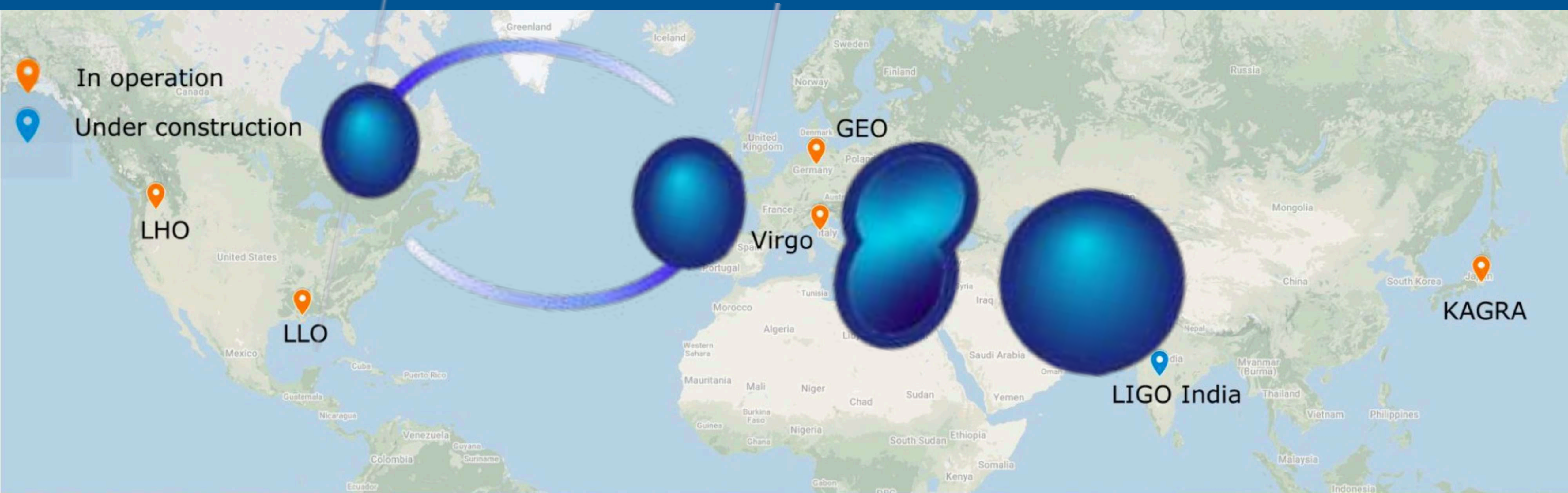
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



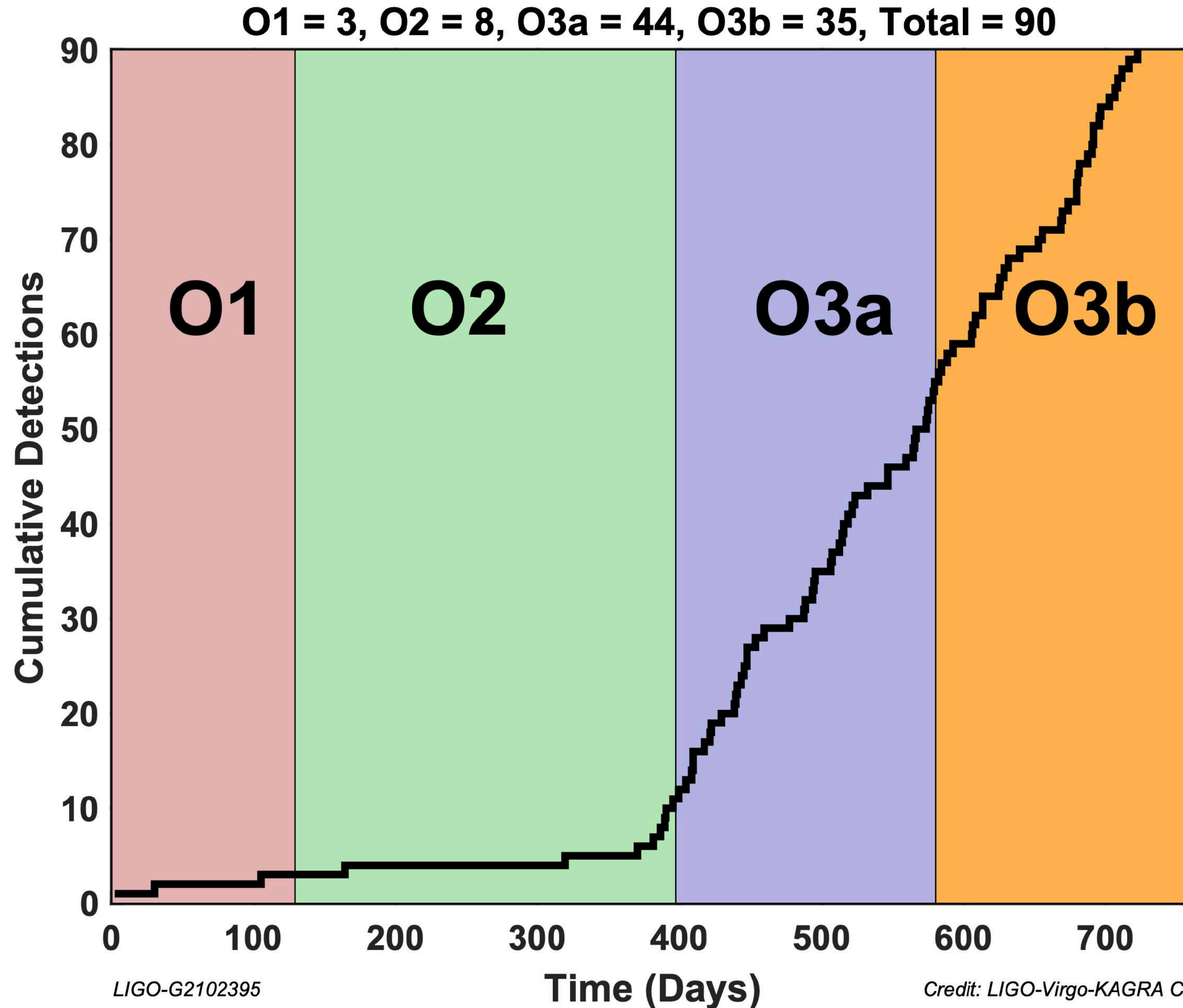
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



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TOTAL NUMBER OF DETECTIONS BY LVK COLLABORATION IN 2015-2020

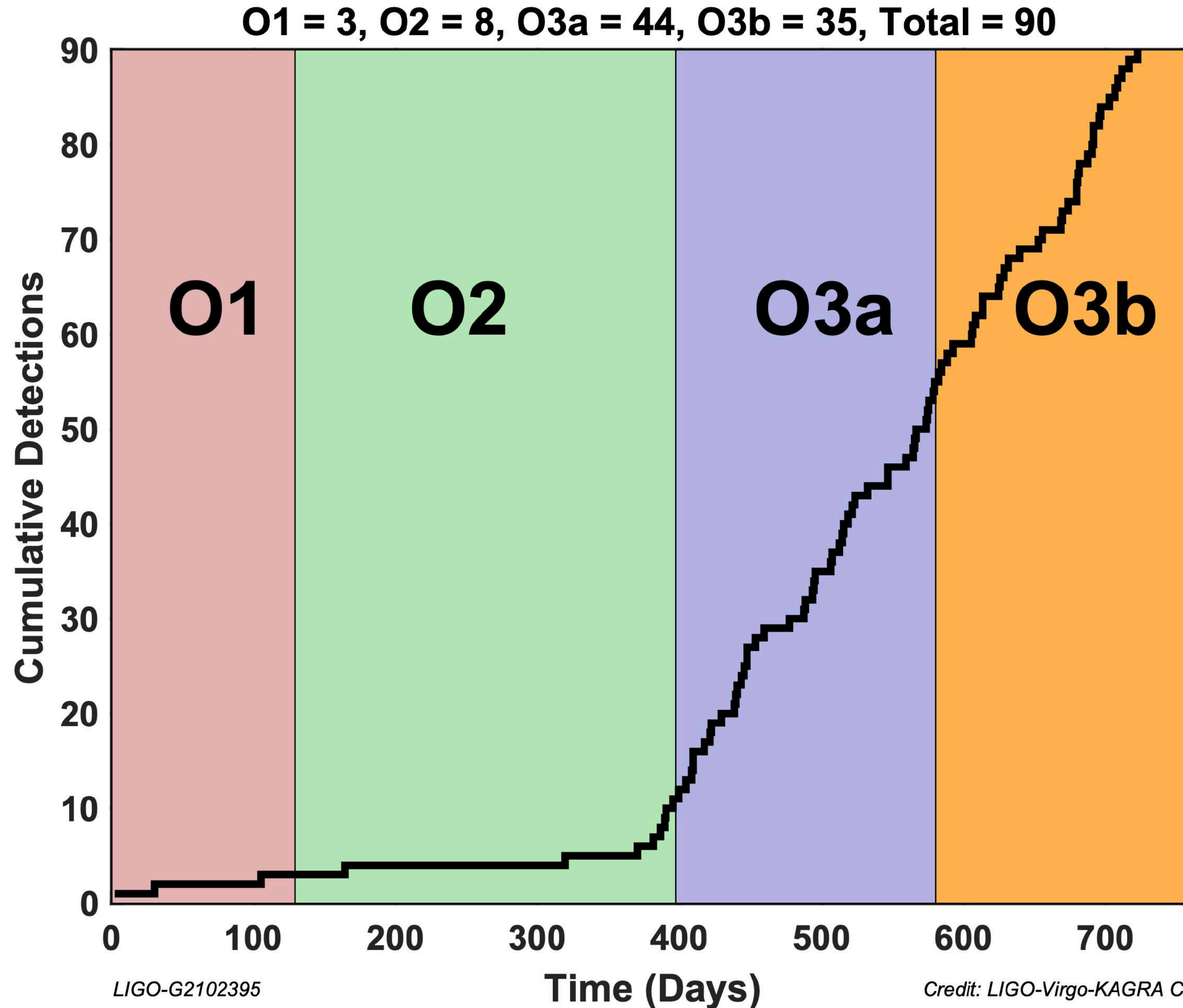


LIGO-Virgo-KAGRA (LVK):

90 published detections

+ *additional detections by
AEI Hannover and IAS
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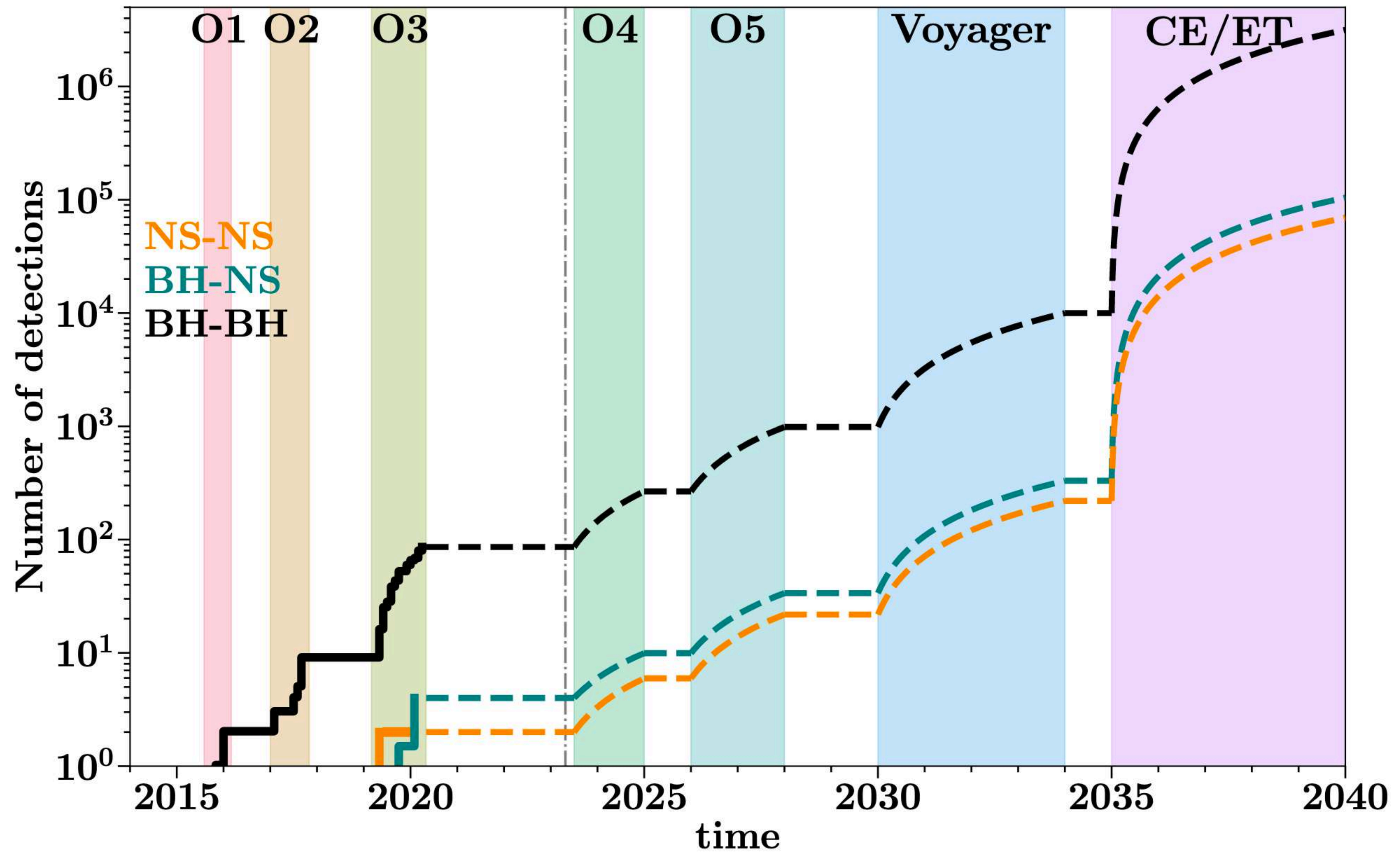
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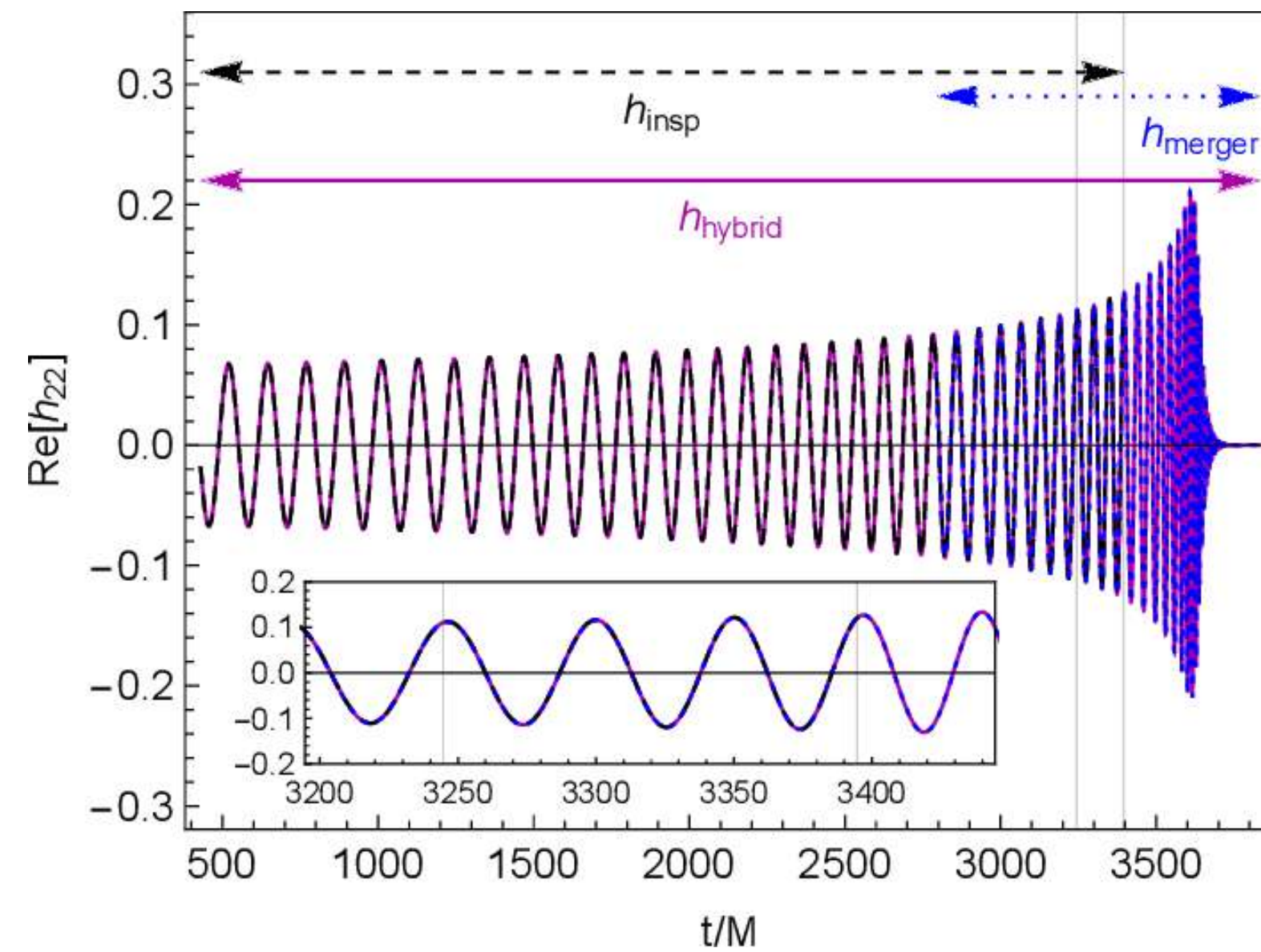
**Stay tuned for upcoming
new catalog of O4 detections
by the LVK Collaboration!**

EXPECTED NUMBER OF DETECTIONS

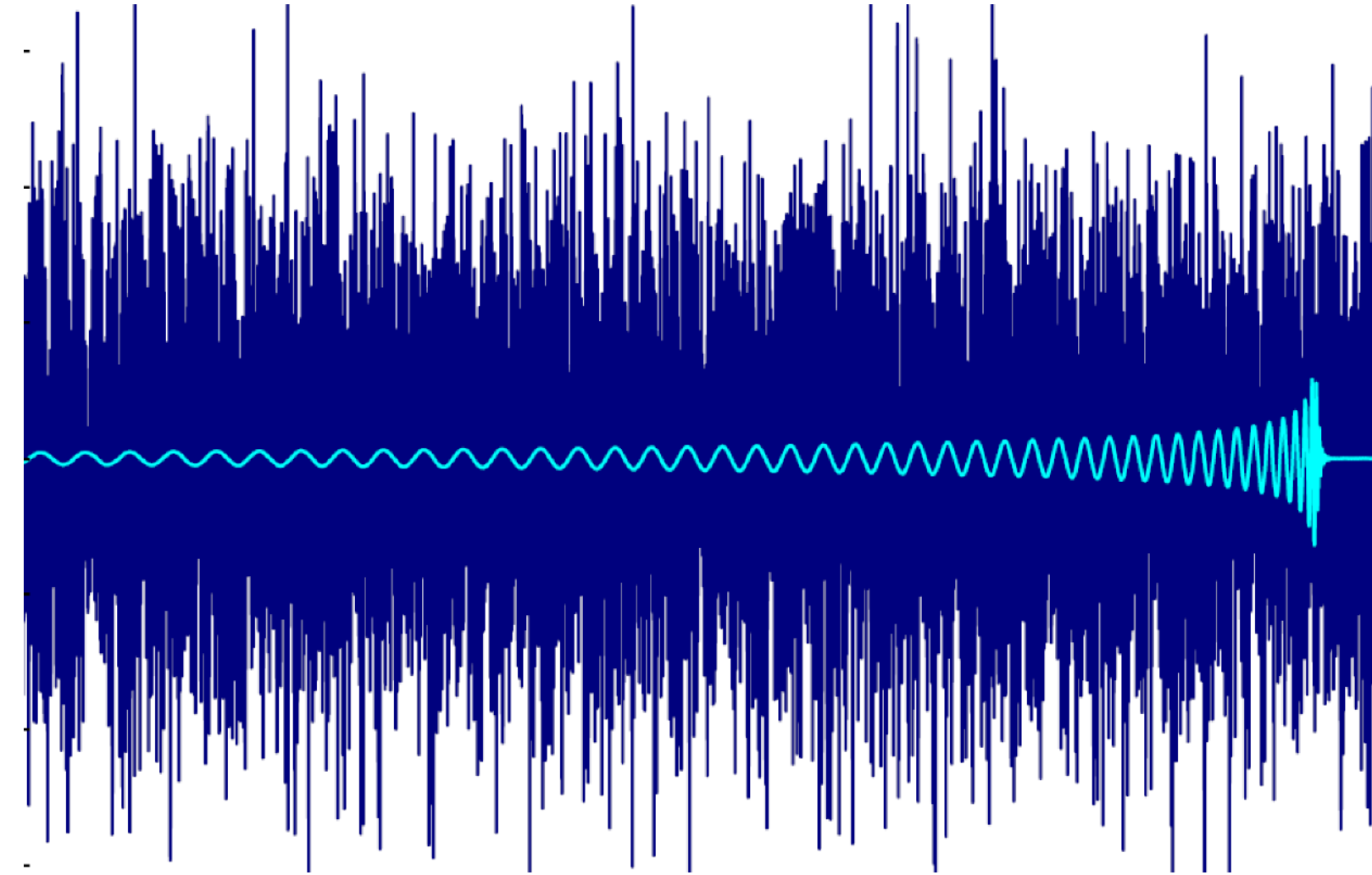


MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

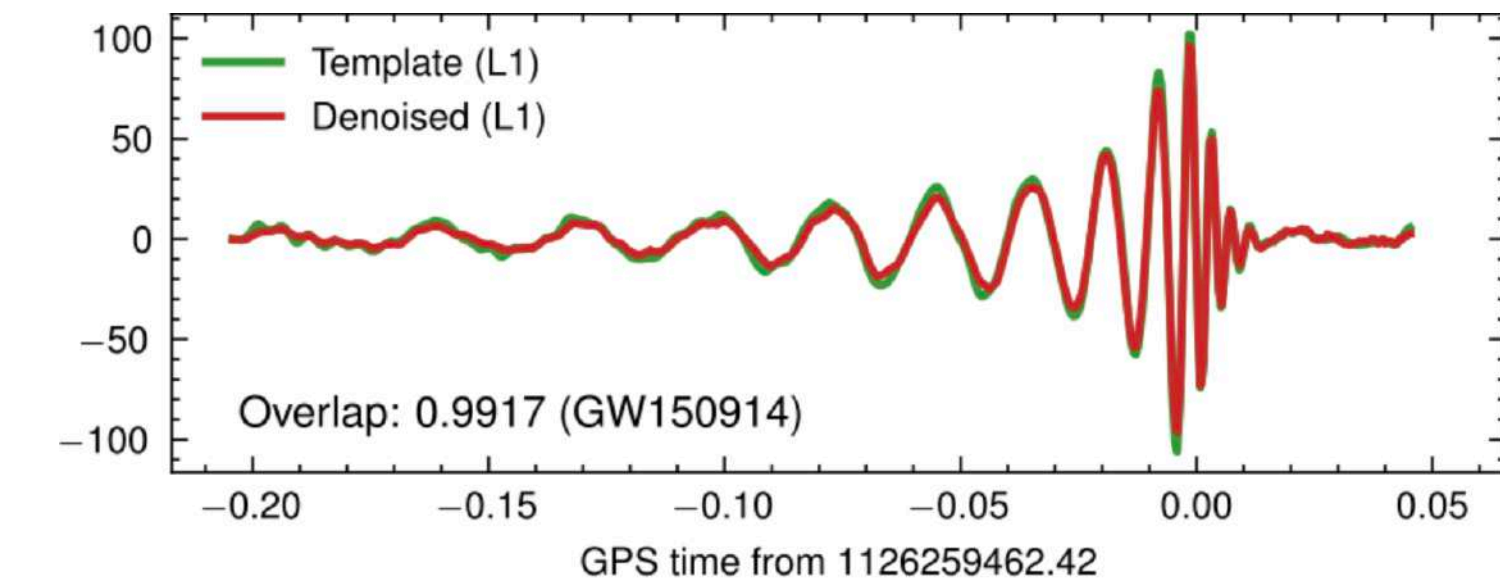
Waveform Modeling



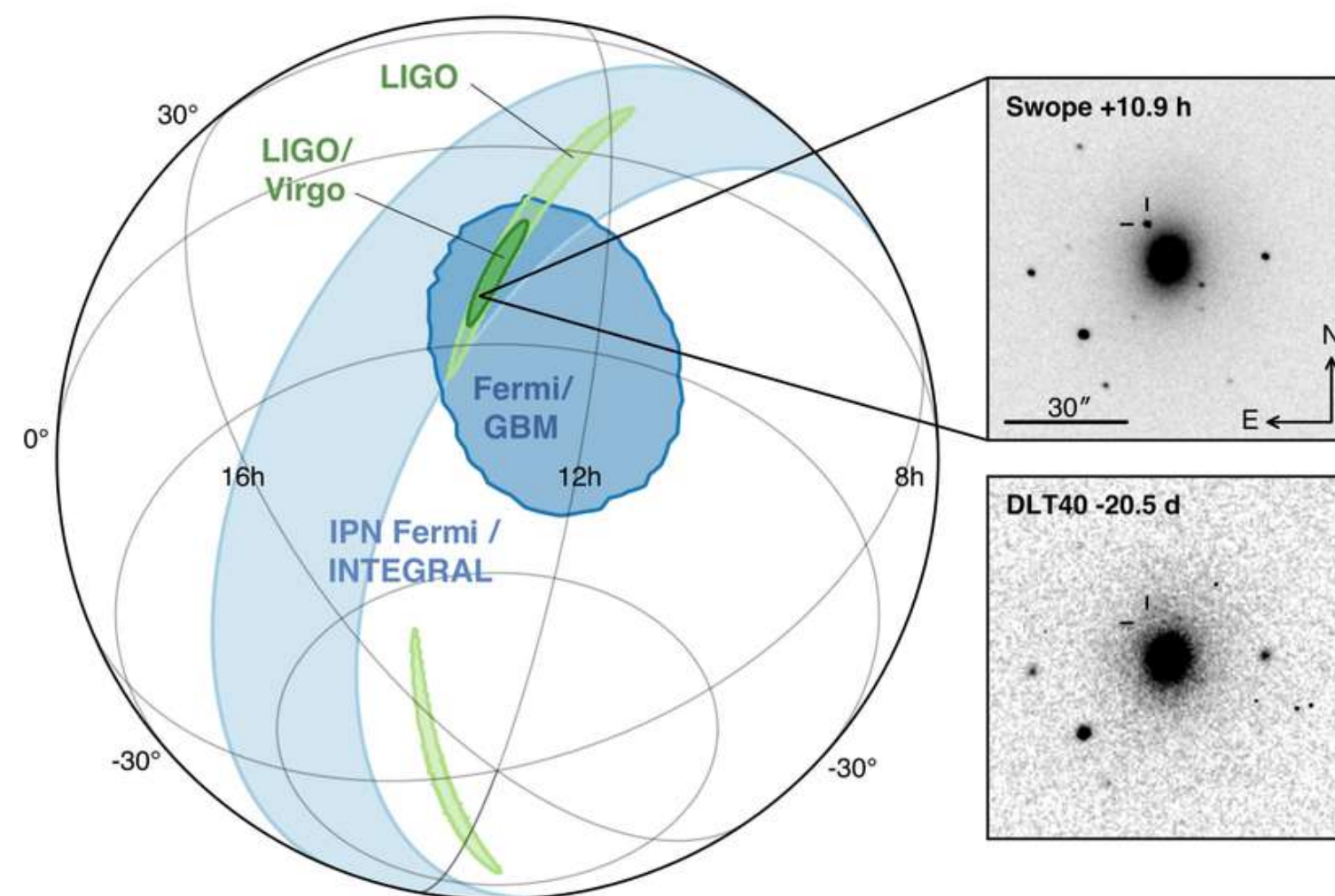
Detection



Denoising

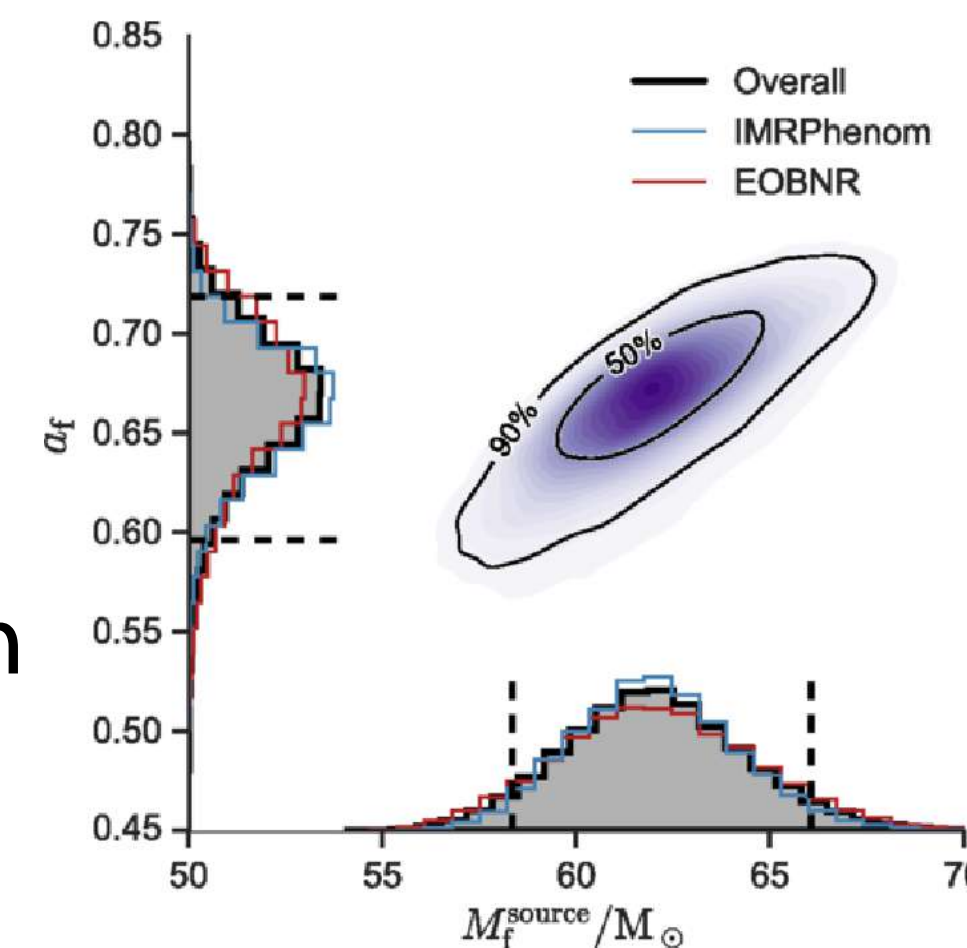


Glitch Classification

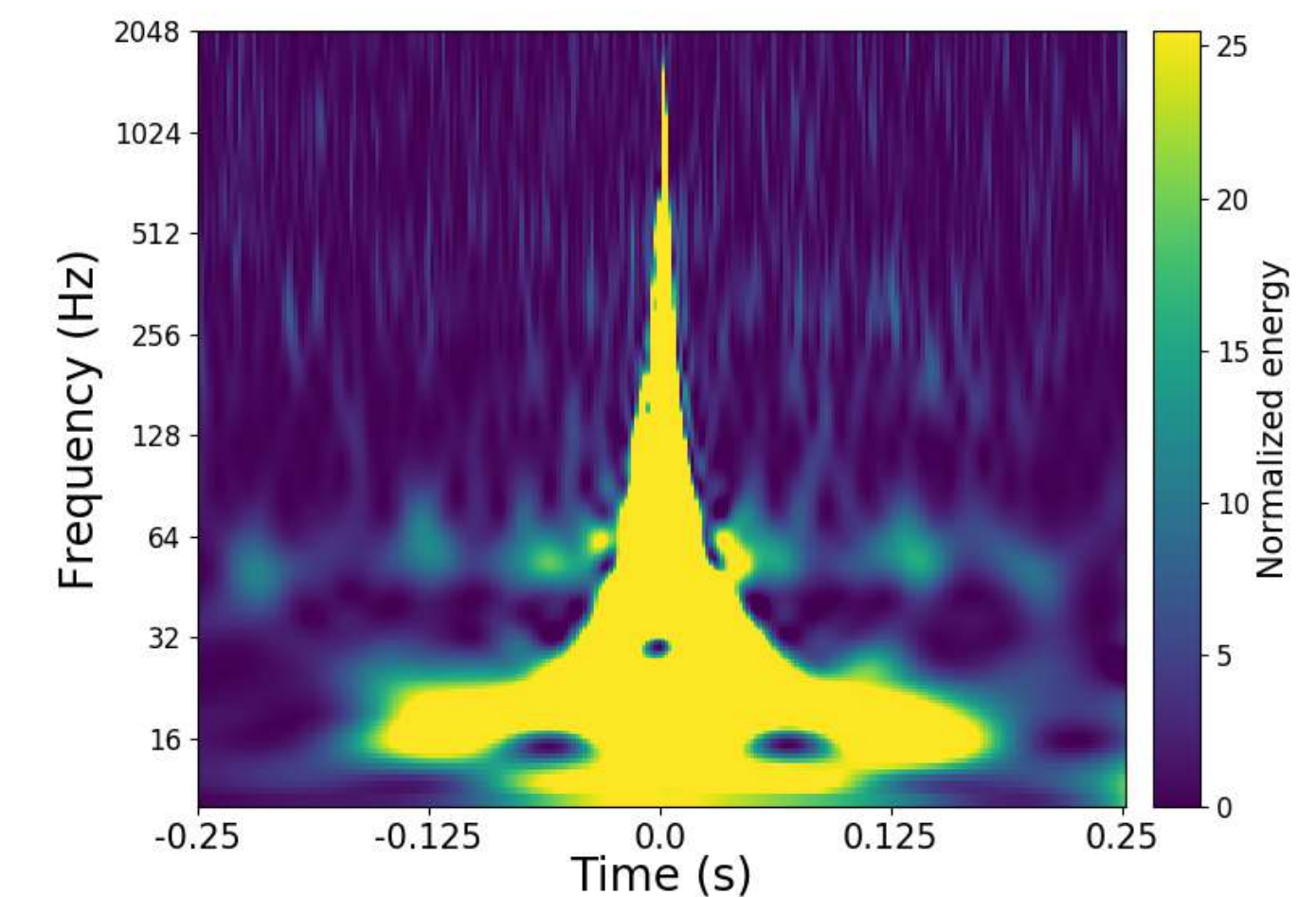


Parameter Estimation

Sky Localization



Livingston - O2a



PHYSICAL REVIEW D **108**, 024022 (2023)

Deep residual networks for gravitational wave detection

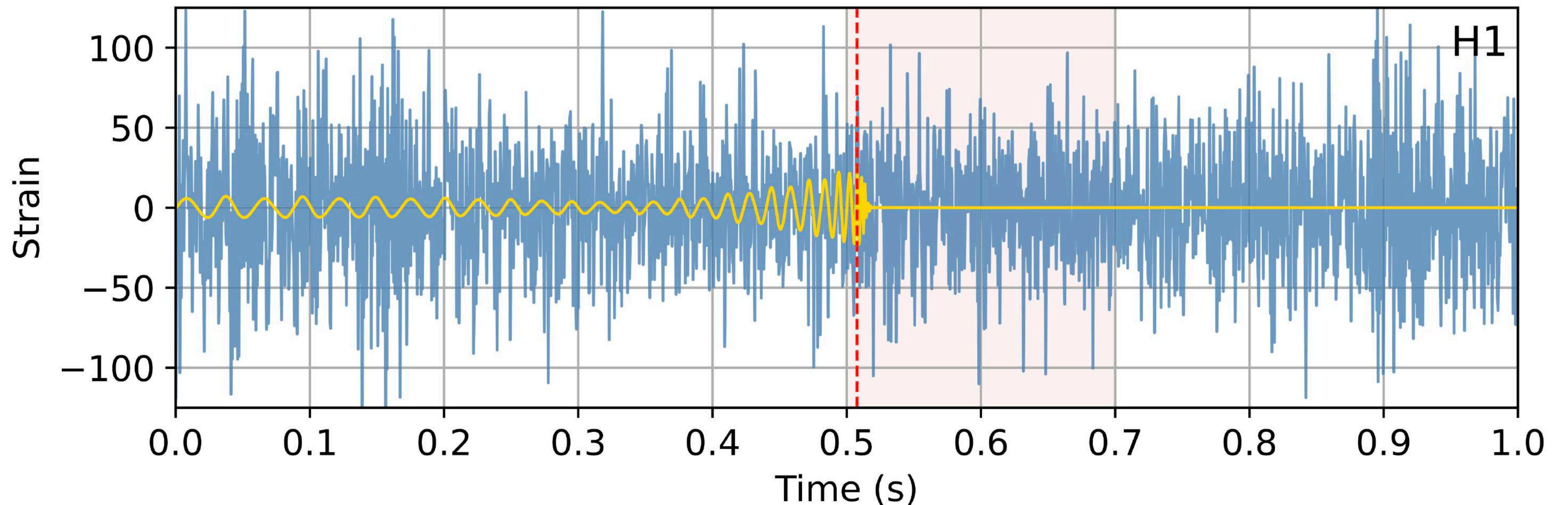
Paraskevi Nousi¹, Alexandra E. Koloniari,² Nikolaos Passalis,¹ Panagiotis Iosif,²
Nikolaos Stergioulas² and Anastasios Tefas¹

¹*Department of Informatics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece*

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(Received 17 December 2022; accepted 14 June 2023; published 11 July 2023)



Architecture:

- 54-layer Resnet-1D
- Deep Adaptive Input Normalization
- SNR-based Curriculum Learning
- 30x faster than PyCBC (using a single GPU card)



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Mass range: $7M_{\odot} \leq M \leq 50M_{\odot}$

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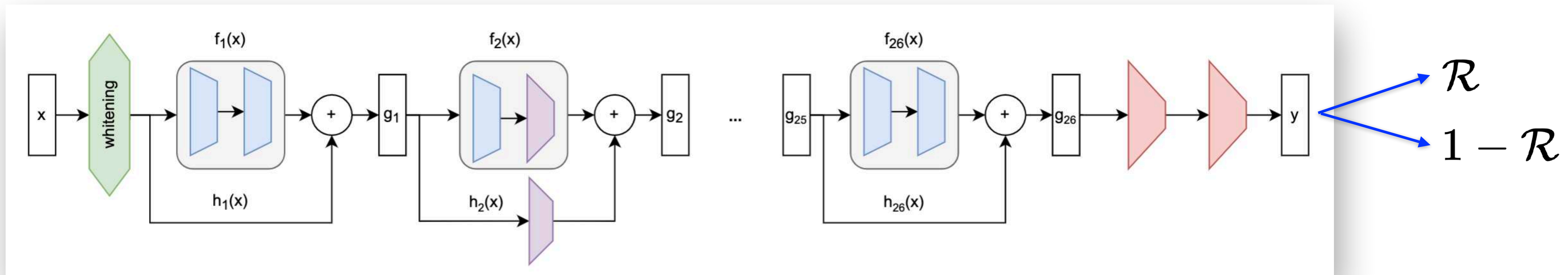
Mass range: $7M_{\odot} \leq M \leq 50M_{\odot}$

Leading algorithm (Virgo-AUTH) in the **1st ML GW search challenge** in the most demanding dataset.

<https://github.com/gwastro/ml-mock-data-challenge-1>

NETWORK ARCHITECTURE OF ARES-GW

1-D ResNet-54 (27 residual blocks with 2 convolutional layers each and skip connections)!

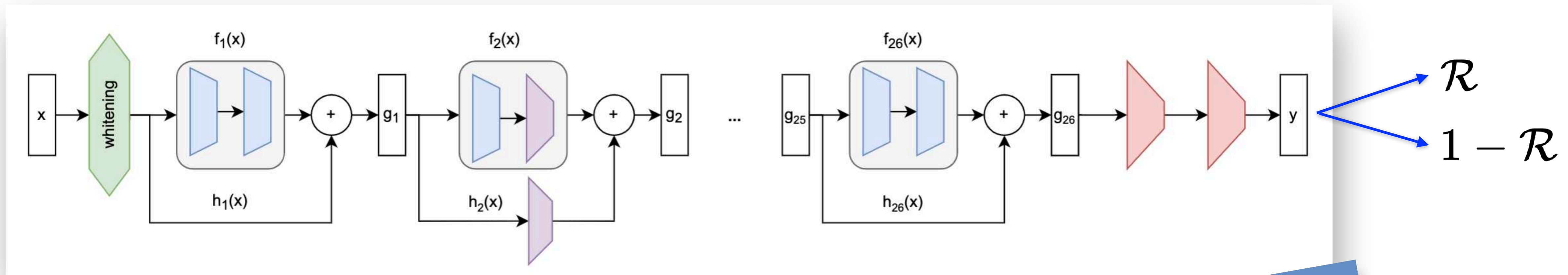


- Residual blocks with skip connections: $g(\mathbf{x}) = f(\mathbf{x}) + h(\mathbf{x})$
- $h(\mathbf{x}) = \mathbf{x}$ or a strided convolutional layer
- After each convolutional layer: batch normalization + ReLU activation
- Mini-batch size of 400 segments
- Adam optimizer for back propagation
- Objective function = regularized binary cross entropy

Residual blocks	Filters	Strided	Input D
4	8		2×2048
1	16	✓	8×2048
2	16		16×1024
1	32	✓	16×1024
2	32		32×512
1	64	✓	32×512
2	64		64×256
1	64	✓	64×256
2	64		64×128
1	64	✓	64×128
2	64		64×64
5	32		64×64
3	16		32×64

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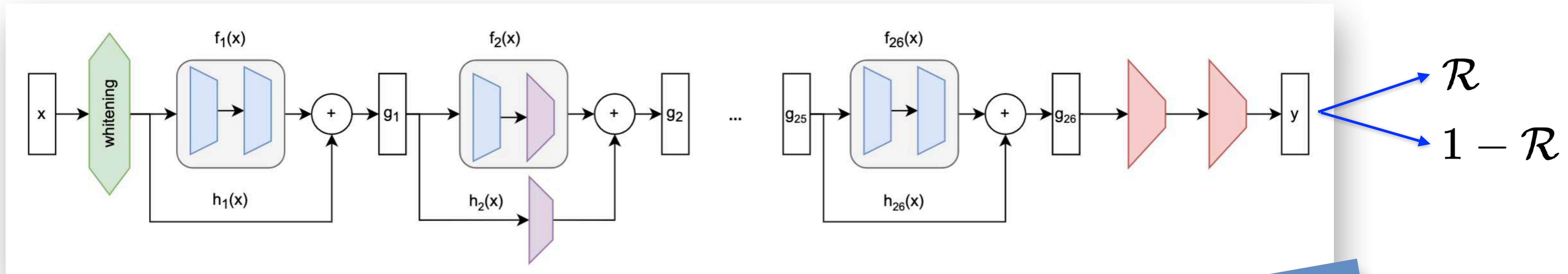
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Gradient problem solved!
-> much deeper networks

			Input D
			2×2048
		✓	8×2048
	16		16×1024
	32	✓	16×1024
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2	32		32×512
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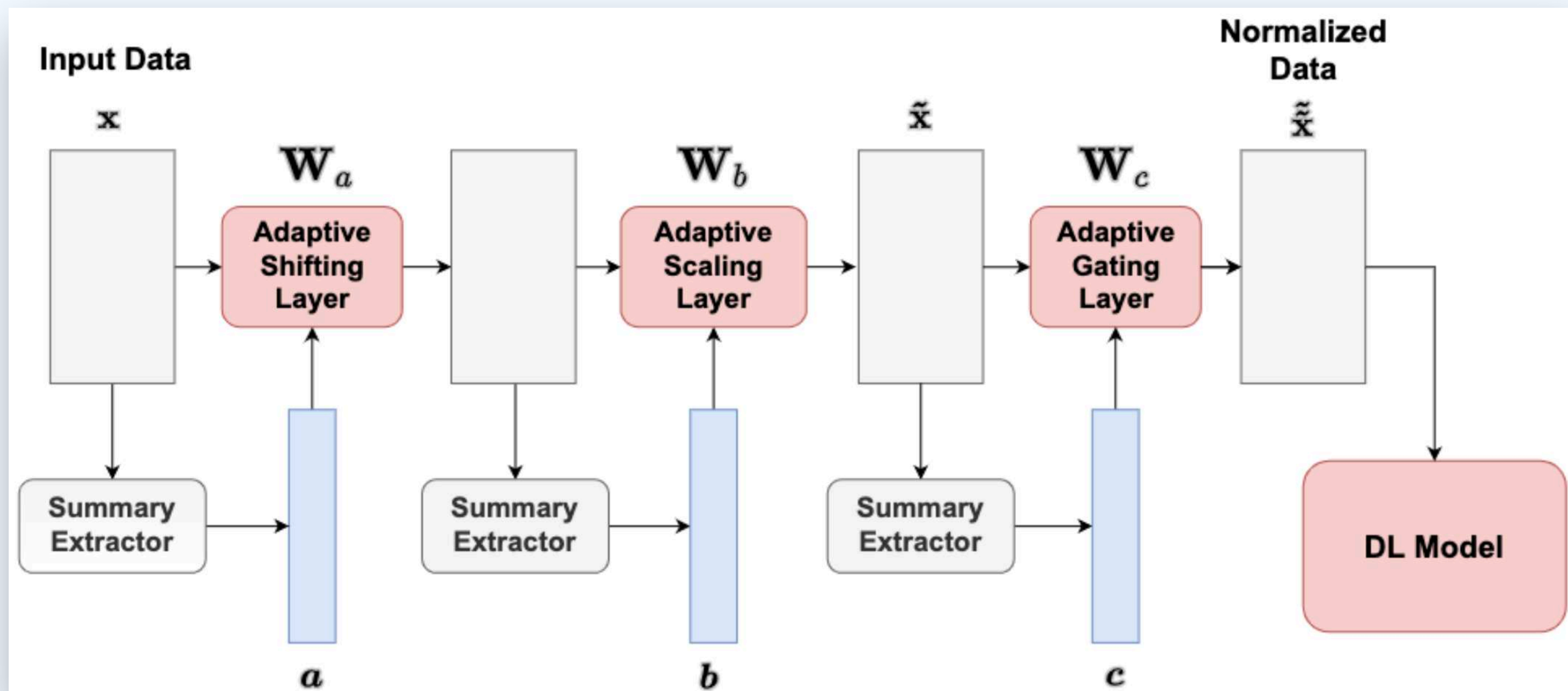
1-D ResNet-54 now used by most
ML GW detection codes

		Input D
		2×2048
		8×2048
1	16	✓
2	32	
3	64	
4	64	✓
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		64×64
		64×64
		32×64

ADAPTIVE INPUT NORMALIZATION

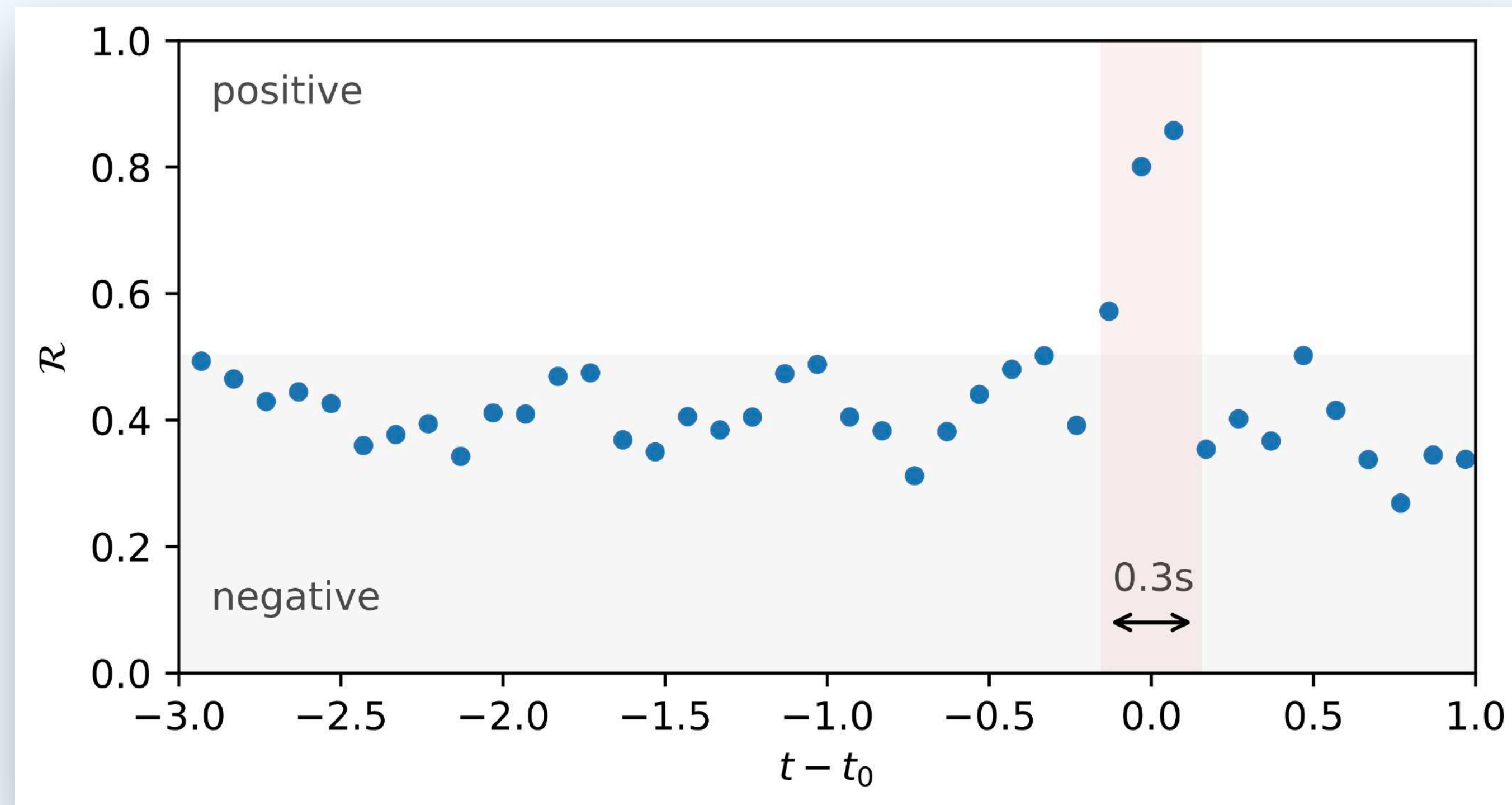
Deep Adaptive Input Normalization (DAIN) (Passalis et al. 2019)

Is applied during training - weights $\mathbf{W}_a$, $\mathbf{W}_b$, $\mathbf{W}_c$ are learnable and adapt to input data!



RANKING STATISTIC

Neural Network Ranking Statistic $\mathcal{R}$ is reported every 0.1 s of input data

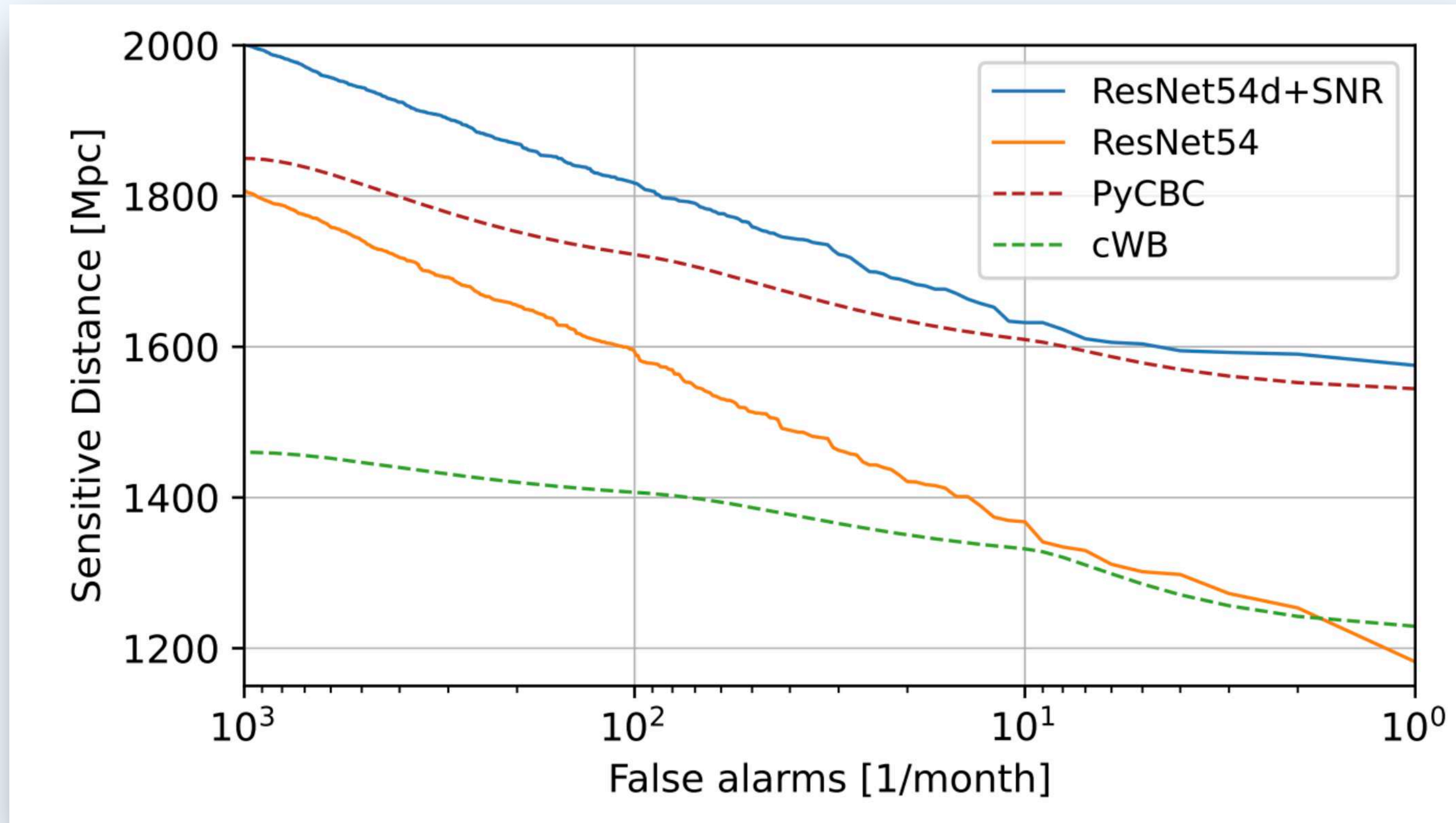


Logarithmic Ranking Statistic

$$\mathcal{R}_s = -\log_{10}(1 - \mathcal{R} + 10^{-16})$$

ARESGW

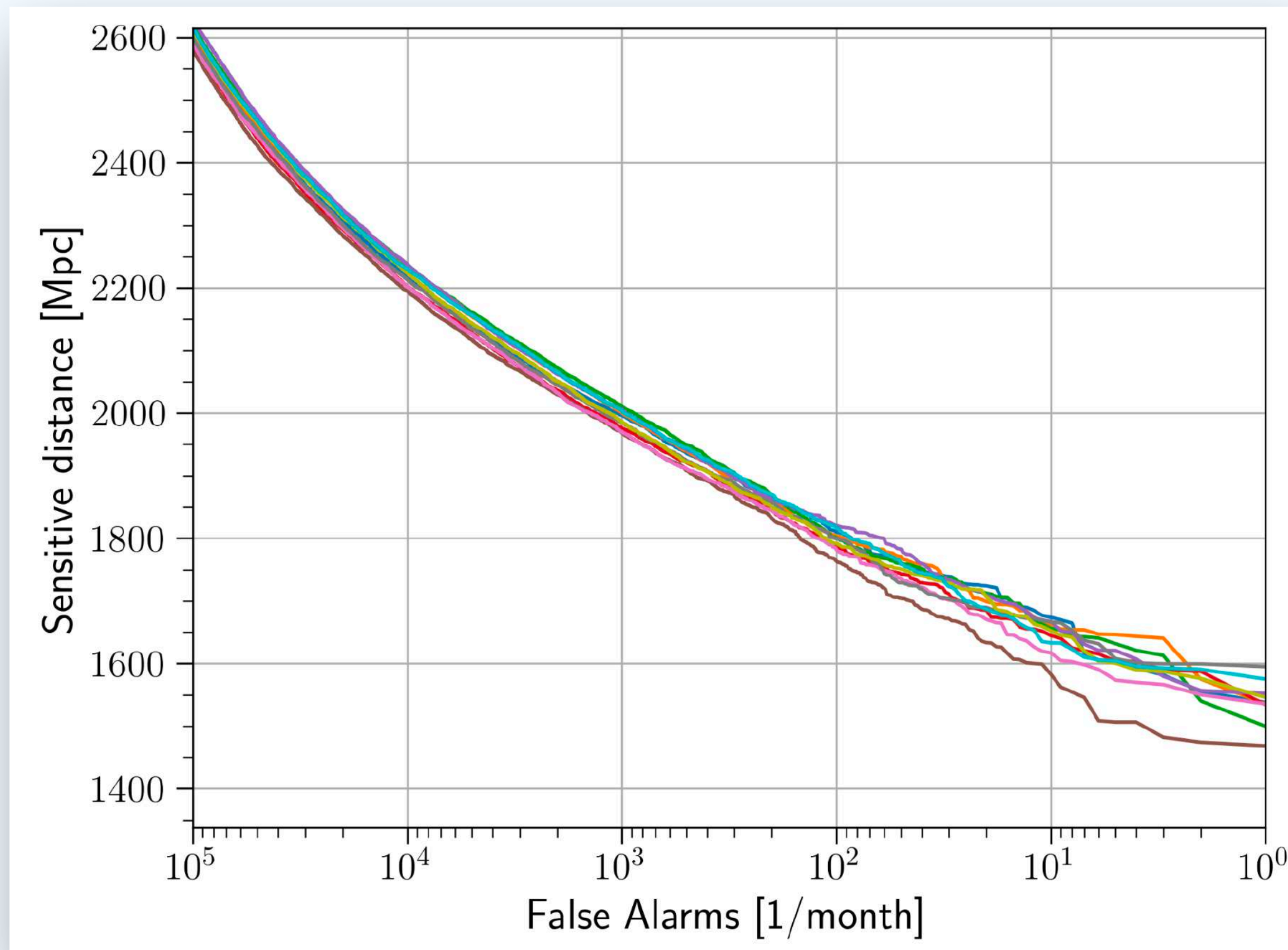
AresGW is the first ML code to exceed **the sensitivity of (non-optimized for this mass range) classical algorithms**



ROBUSTNESS OF SENSITIVITY METRICS FOR ML DETECTION CODES

Variance with respect to different noise realizations and different injections:

Sensitive distance $\sim 4\%$

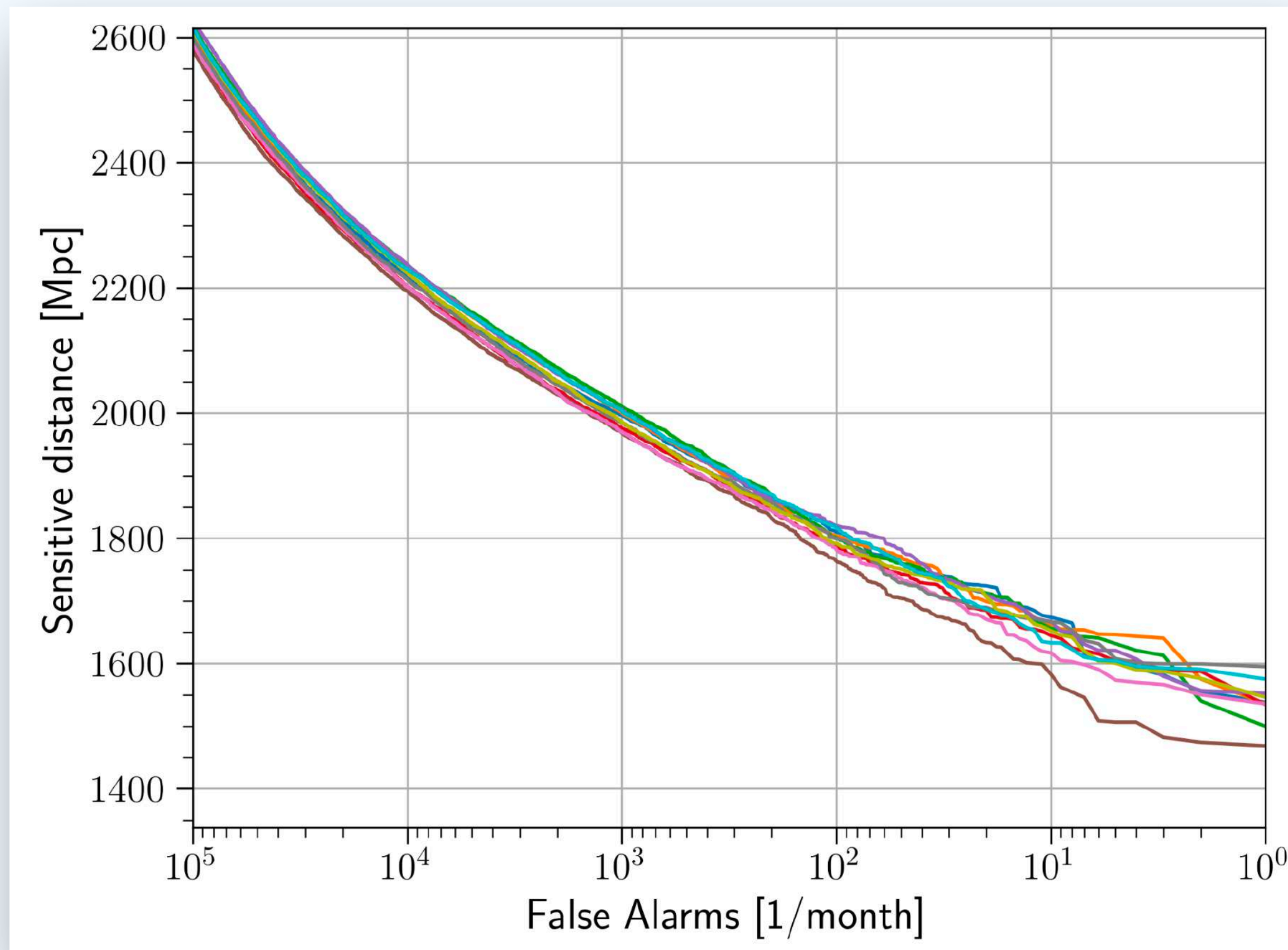


Koloniari, Paschalidis, Lazaridis, Stergioulas, in preparation (2025)

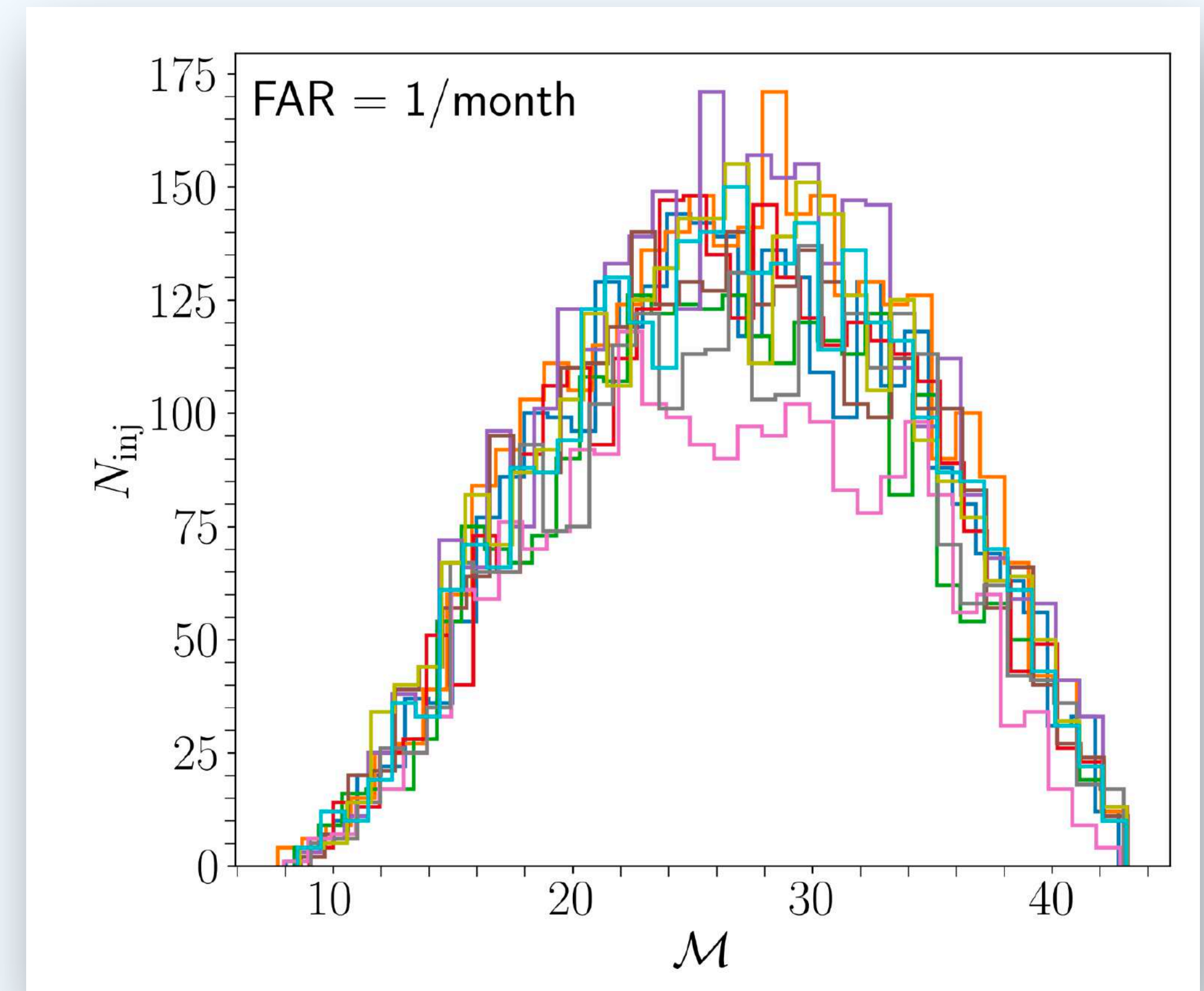
ROBUSTNESS OF SENSITIVITY METRICS FOR ML DETECTION CODES

Variance with respect to different noise realizations and different injections:

Sensitive distance $\sim 4\%$



Number of injections $\sim 19\%$



ARESGW ON GITHUB

<https://github.com/vivinousi/gw-detection-deep-learning>

The screenshot displays the GitHub repository page for `vivinousi/gw-detection-deep-learning`. The repository is public and has 22 stars, 2 forks, and 7 watchers. The main content area shows the repository structure with a table of files and folders, their commit history, and the README content.

File/Folder	Commit Message	Commit Time
doc	readme update	2 years ago
modules	training code initial commit	2 years ago
trained_models	training code initial commit	2 years ago
utils	training code initial commit	2 years ago
LICENSE	Initial commit	2 years ago
README.md	readme update	2 years ago
run_on_test.sh	training code initial commit	2 years ago
test.py	training code initial commit	2 years ago
test_challenge_model.py	training code initial commit	2 years ago
train.py	readme update	2 years ago

The README content is as follows:

AResGW: Augmentation and RESidual networks for Gravitational Wave detection

Gravitational wave detection in real noise timeseries using deep residual neural networks.

This repository contains the method submitted by our team, Virgo-AUTH, to the [MLGWSC](#) competition. Our method contains the following components:



PAPER

New gravitational wave discoveries enabled by machine learning

OPEN ACCESS

Alexandra E Koloniari^{1,*} , Evdokia C Koursoumpa¹ , Paraskevi Nousi² , Paraskevas Lampropoulos¹ , Nikolaos Passalis³ , Anastasios Tefas⁴  and Nikolaos Stergioulas¹ 

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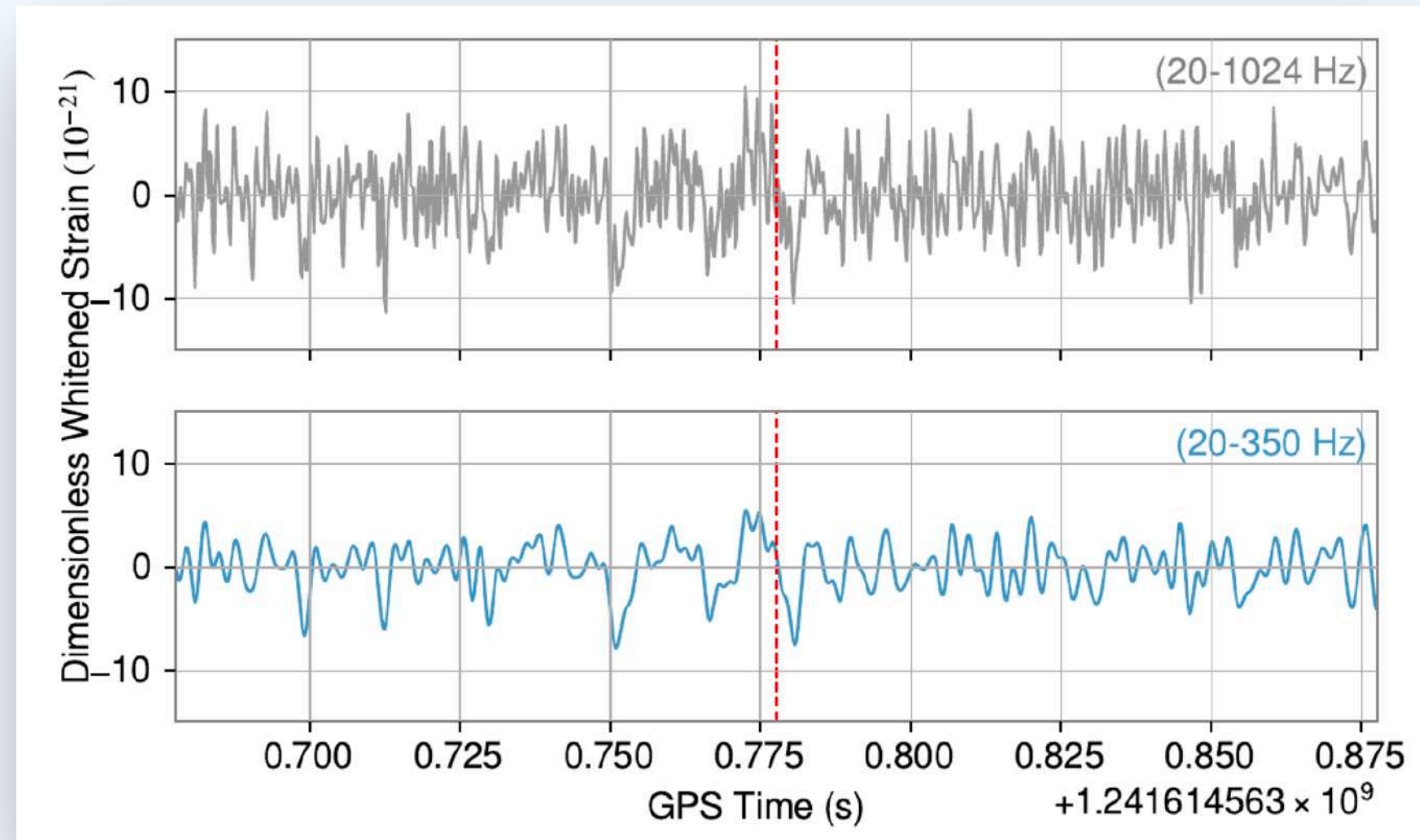
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E-mail: akolonia@auth.gr

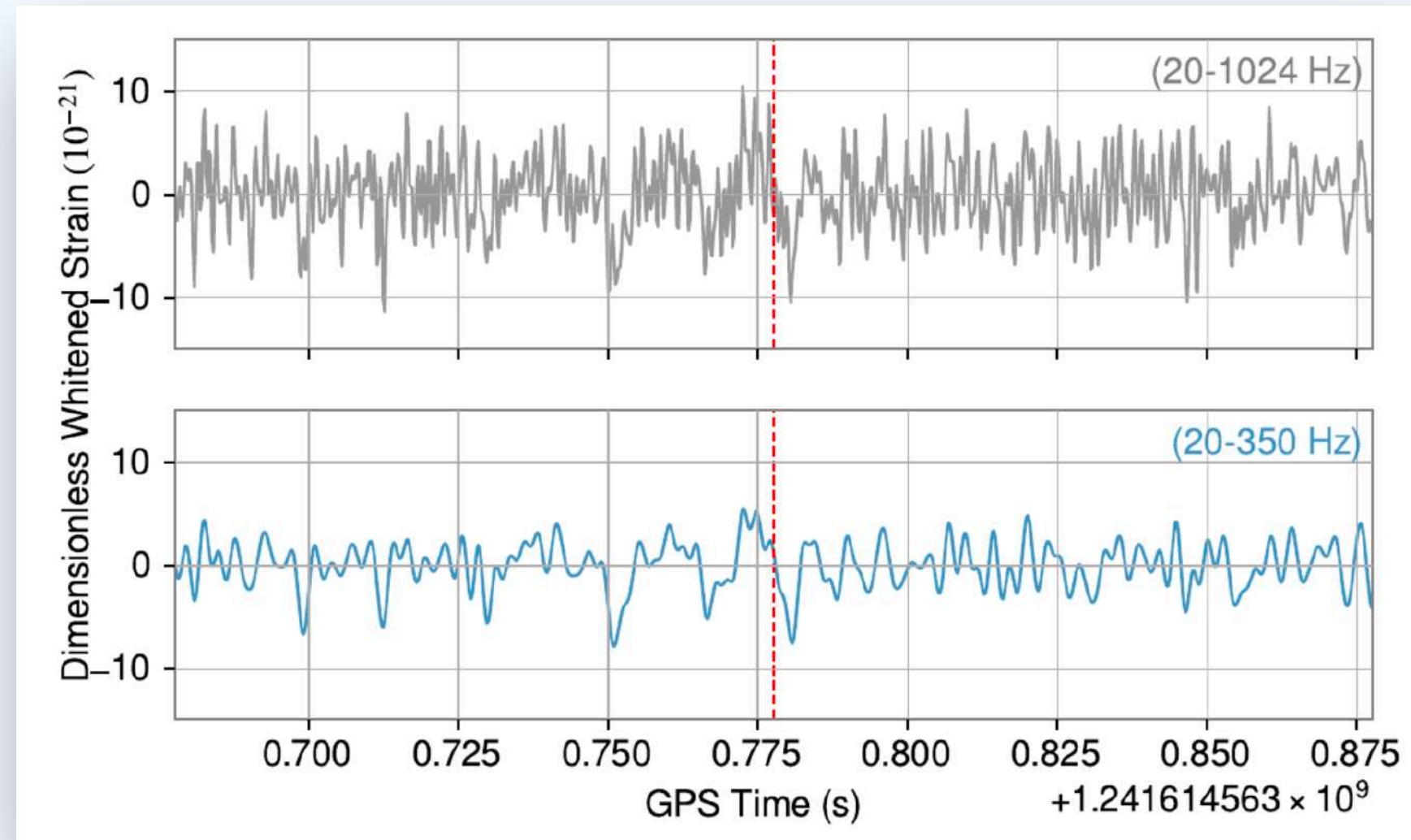
MAIN ENHANCEMENTS:

1) Training on low-pass filtered data

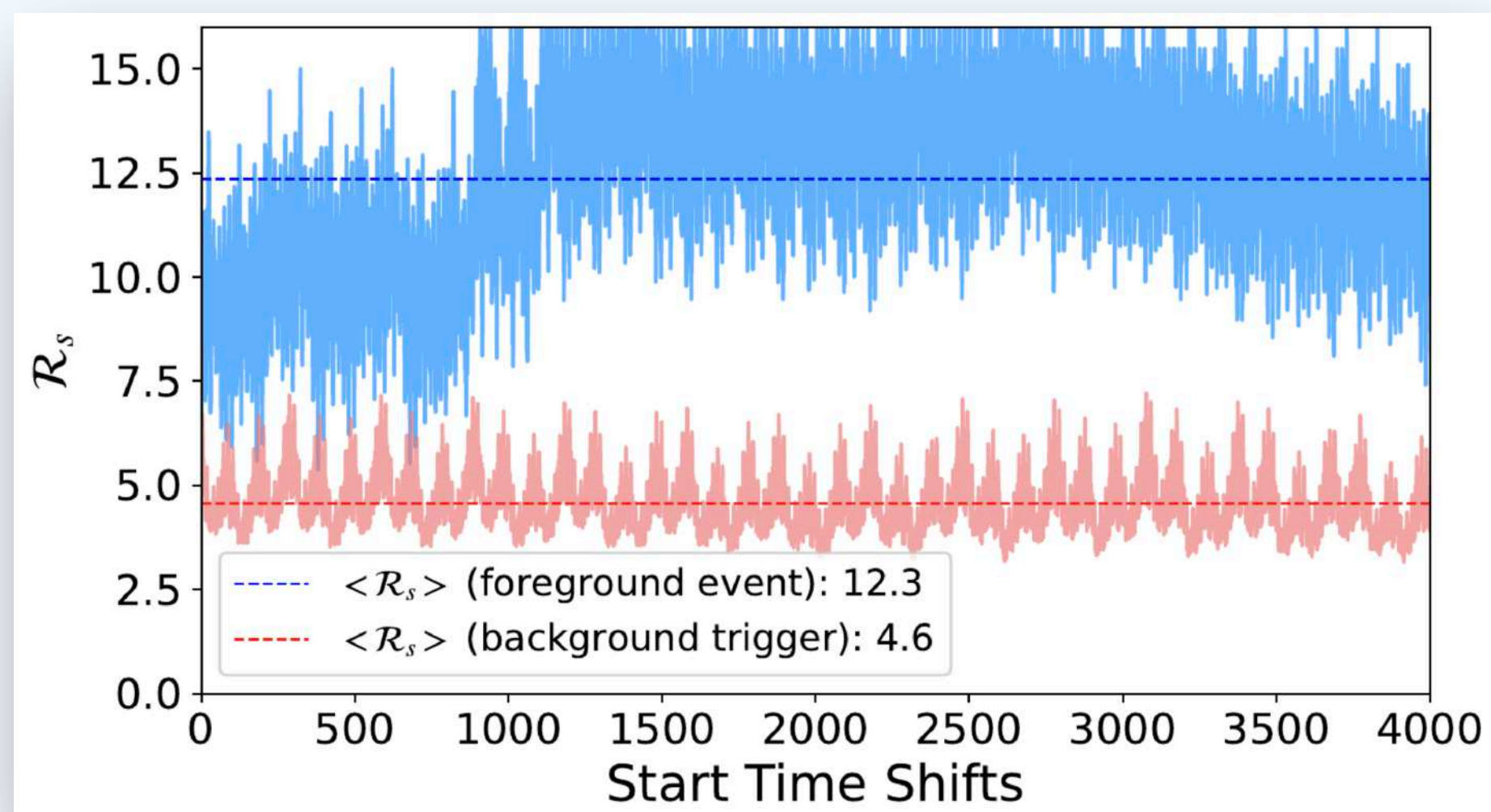


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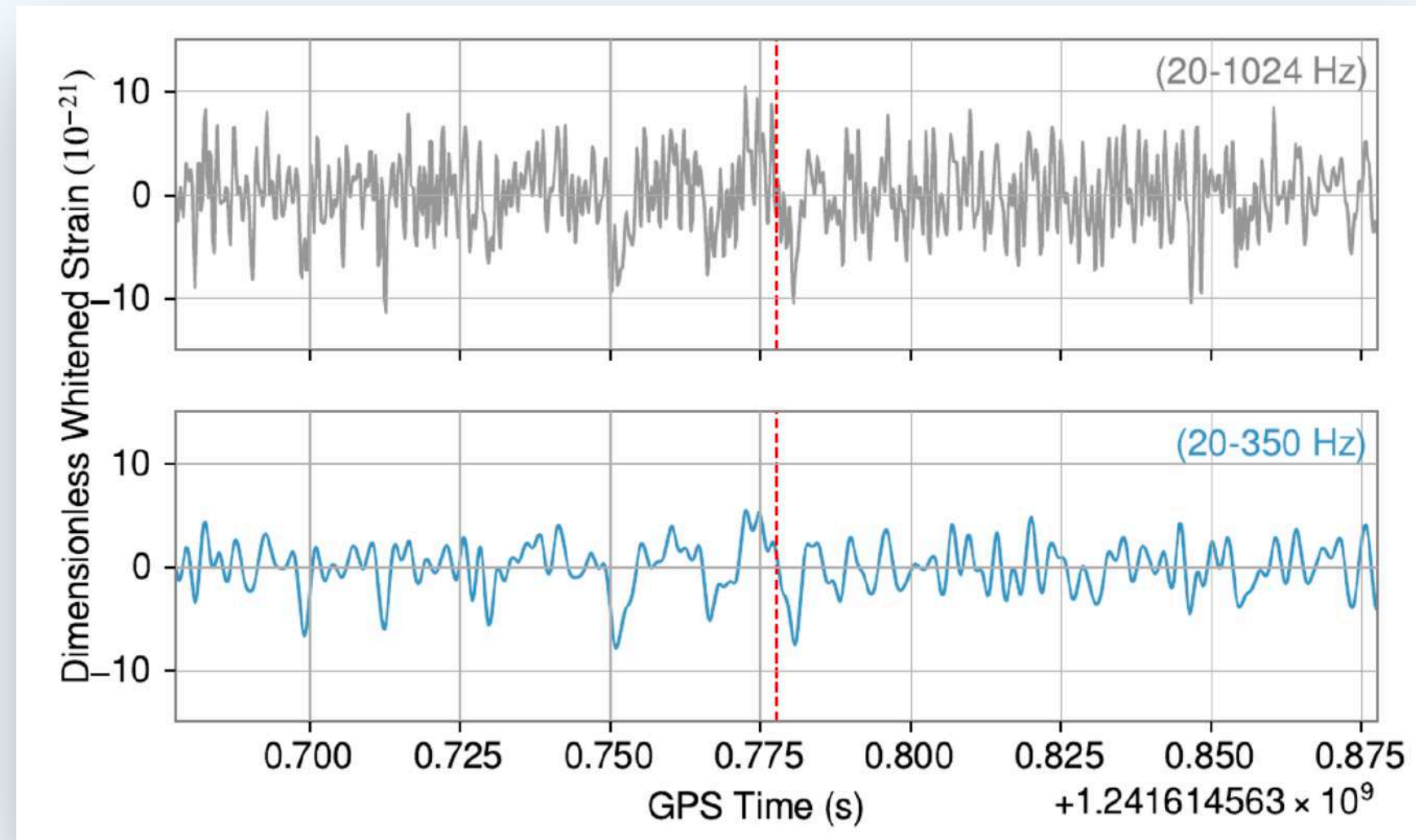


2) Ensemble-averaged ranking statistic

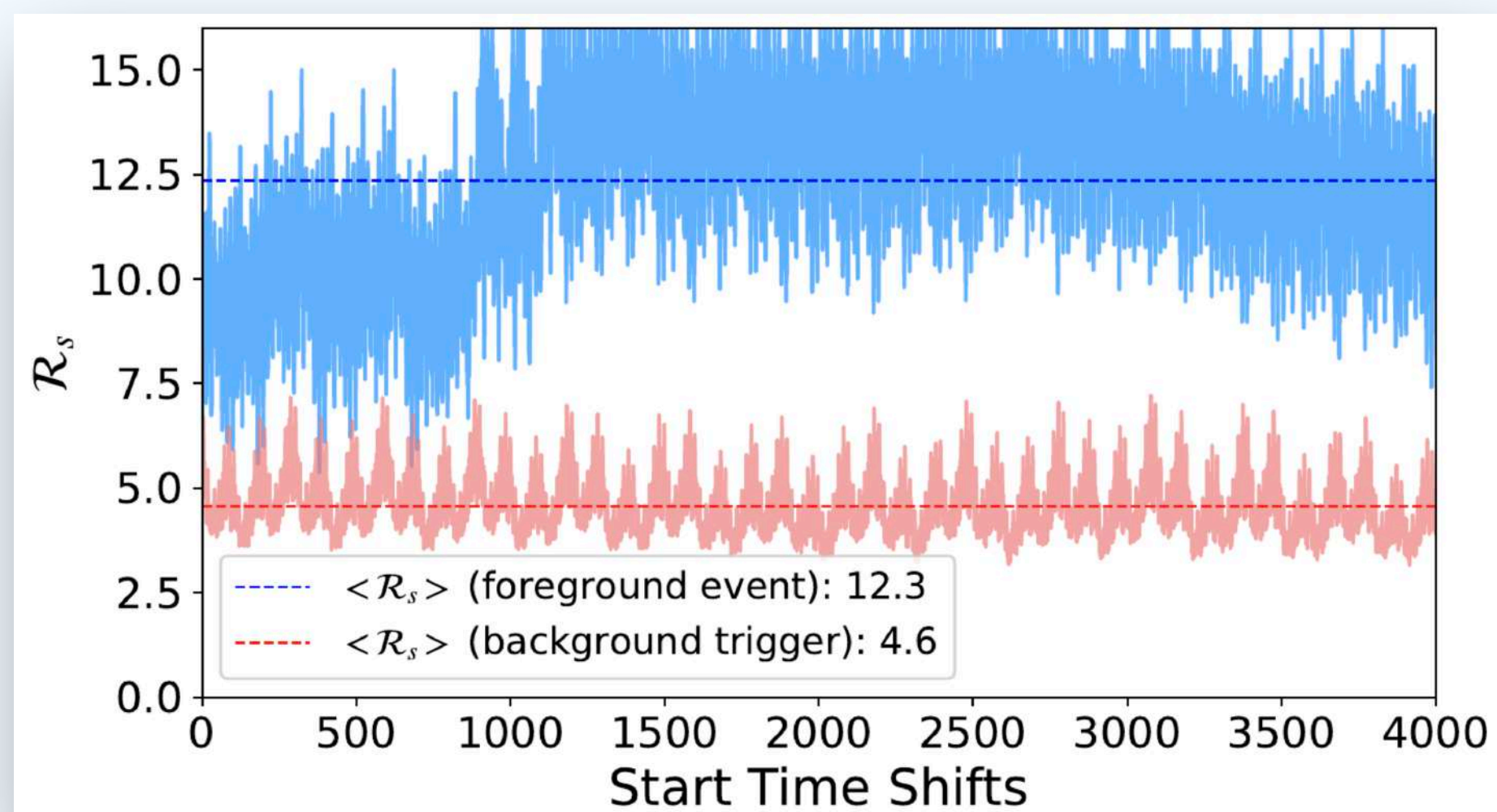


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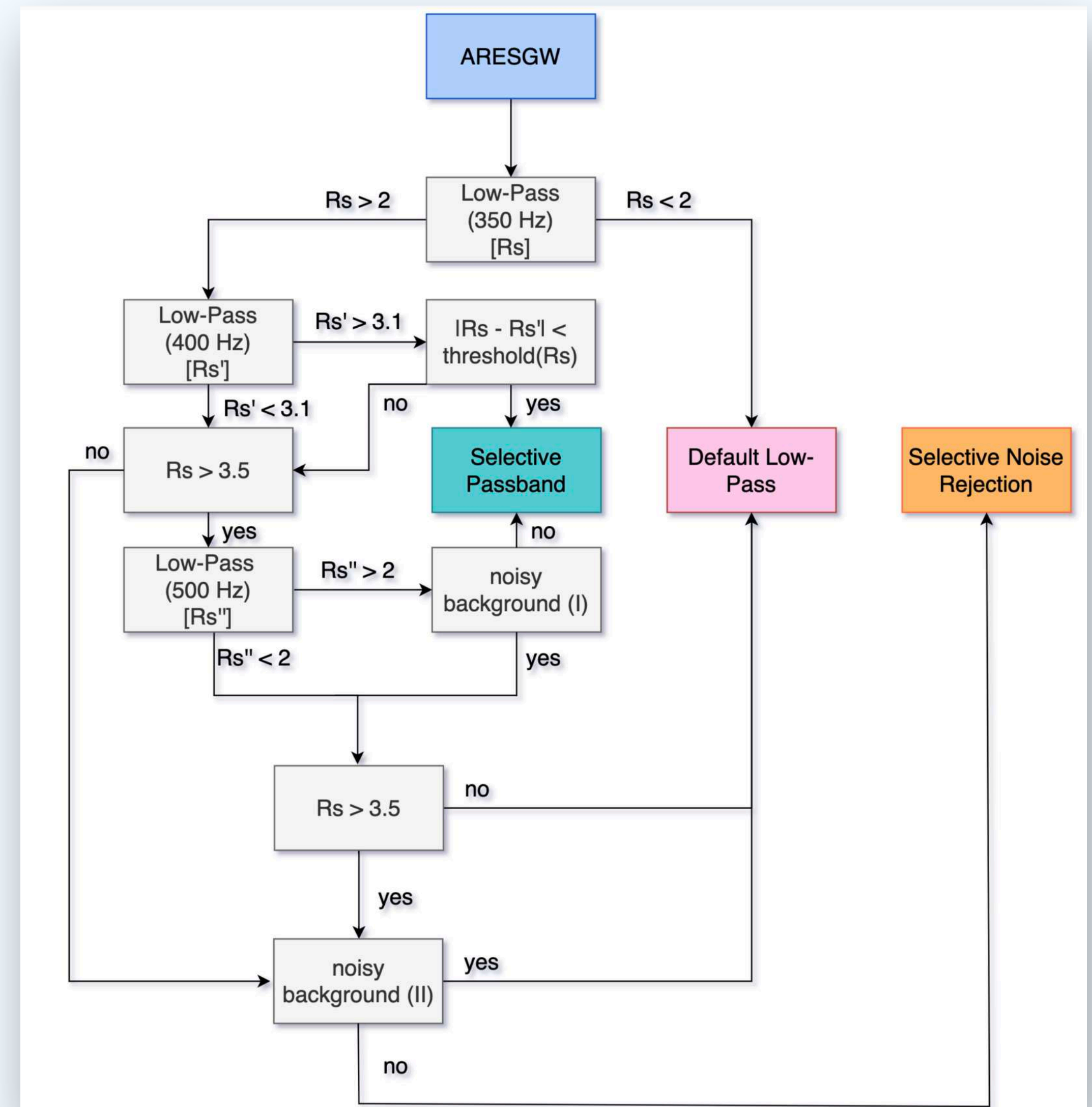
1) Training on low-pass filtered data



2) Ensemble-averaged ranking statistic



3) Application of **noise filters** to **reduce background FAR**.



ASTROPHYSICAL PROBABILITY

p_astro is calculated as

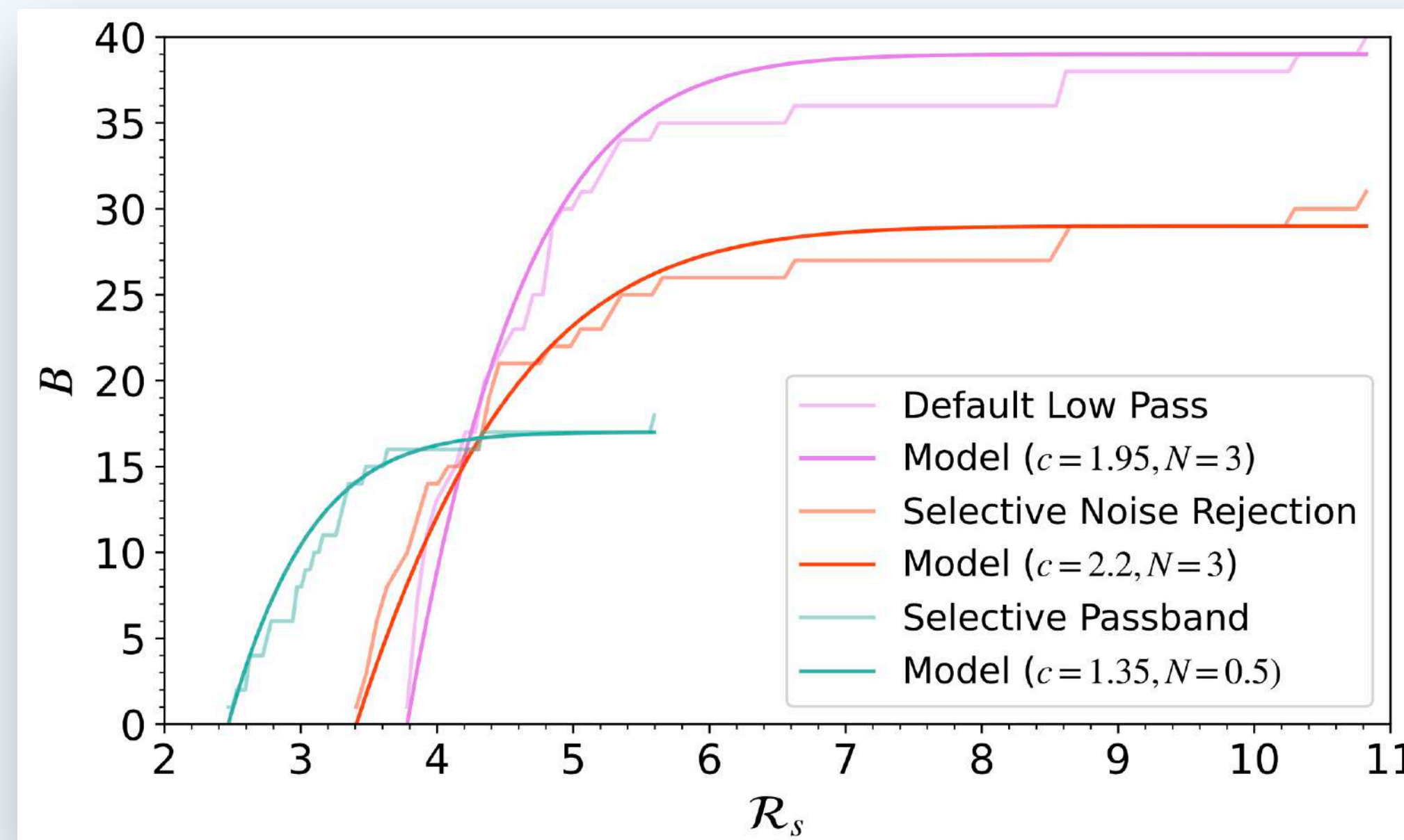
$$p_{\text{astro}} = \frac{f(\mathcal{R}_s)}{b(\mathcal{R}_s) + f(\mathcal{R}_s)}$$

where the **background** and **foreground differential rates** are

$$b(\mathcal{R}_s) = \frac{dB}{d\mathcal{R}_s} \quad f(\mathcal{R}_s) = \frac{dF}{d\mathcal{R}_s}$$

The cumulative distribution of the **O3 background** is modeled **analytically** as

$$\hat{B}(x) = \frac{\left(1 + \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right)\right)^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}{2^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}$$

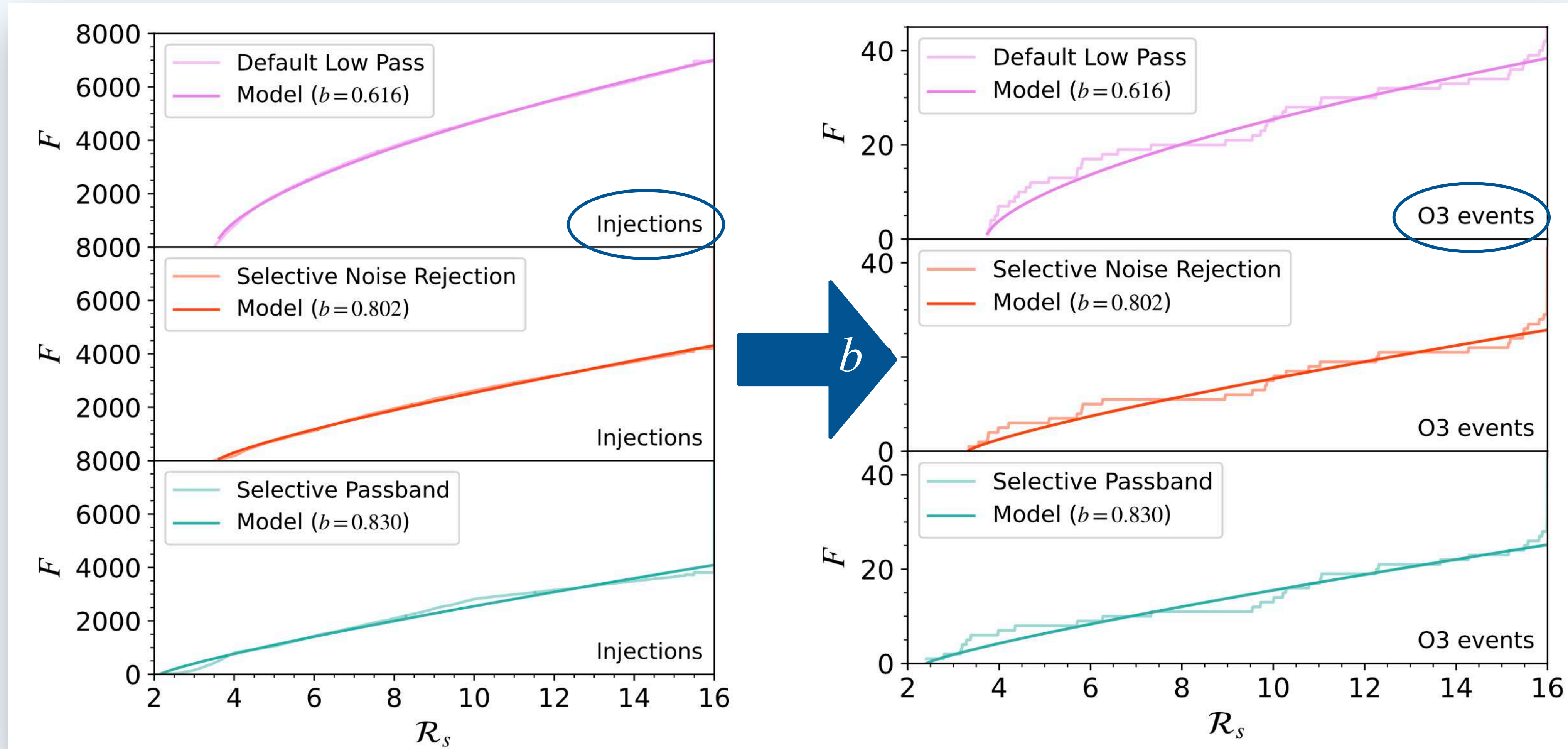


ASTROPHYSICAL PROBABILITY

Analytic model of **cumulative foreground** distribution:

$$F(x) = a(x - x_{\min})^b$$

Coefficient **b** determined through **injections** in O3 noise:



NEW GW DETECTIONS WITH AresGW IN O3 DATA

AresGW detects **42 out of 51** known O3 events (*most sensitive pipeline in this mass range*)

We found **8 new gravitational wave candidates** with $p_{\text{astro}} > 50\%$ (3 $p_{\text{astro}} > 99\%$).

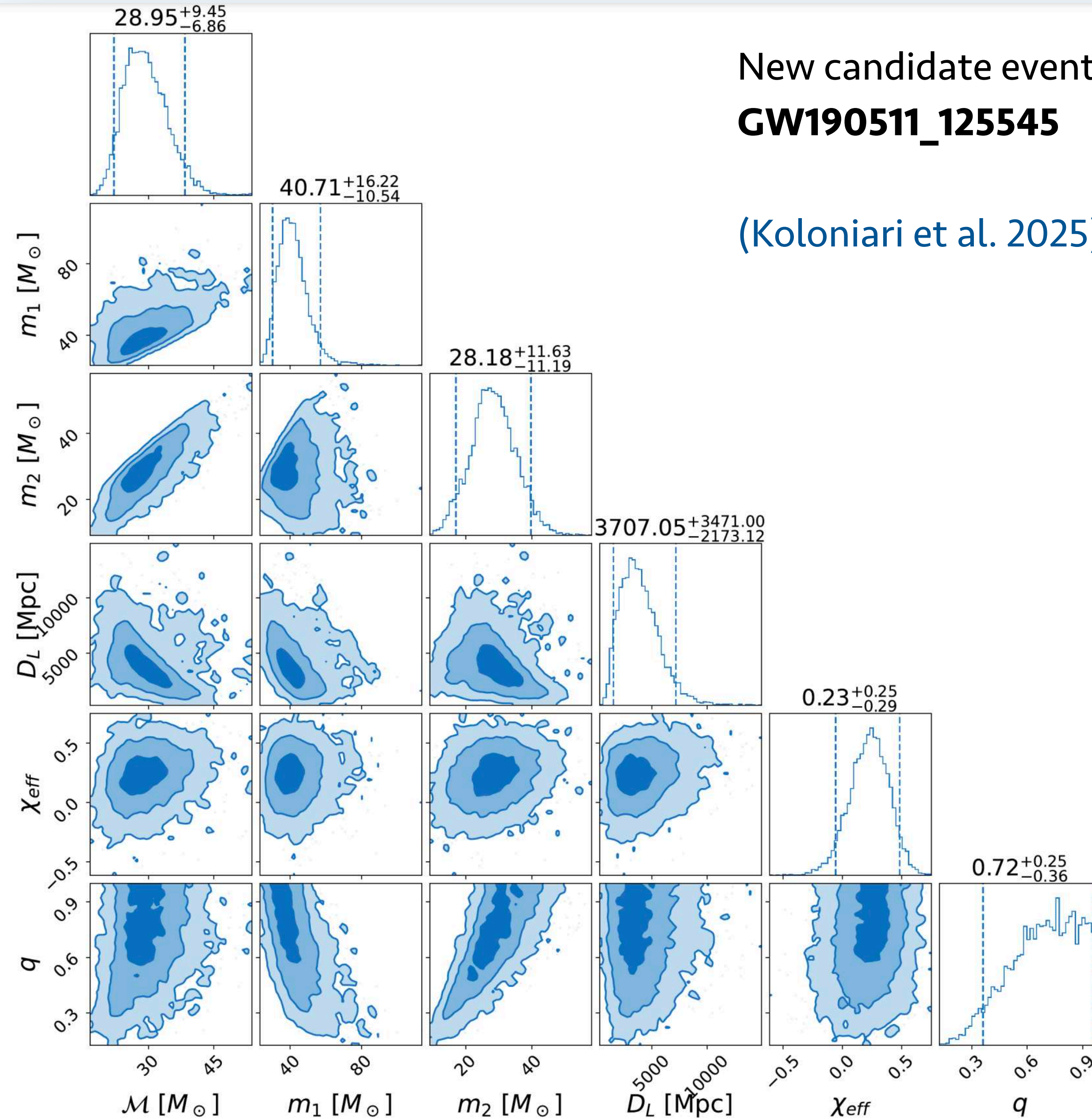
TABLE VII: New candidate events identified by AresGW.

#	Event Name	GPS Time (s)	p_{astro}	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay (s)	χ_L^2	χ_H^2	Class
1	GW190511_125545	1241614563.77	1.00	0.27	9.54	0.0027	1.16	1.46	Selective Passband
2	GW190614_134749	1244555287.93	0.99	4.6	5.80	0.0012	0.65	0.80	Selective Passband
3	GW190607_083827	1243931925.99	0.99	6.5	8.95	0.0056	0.90	0.48	Selective Noise Rejection
4	GW190904_104631	1251629209.01	0.72	14	4.35	0.0002	0.38	0.71	Selective Passband
5	GW190523_085933	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
6	GW200208_211609	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

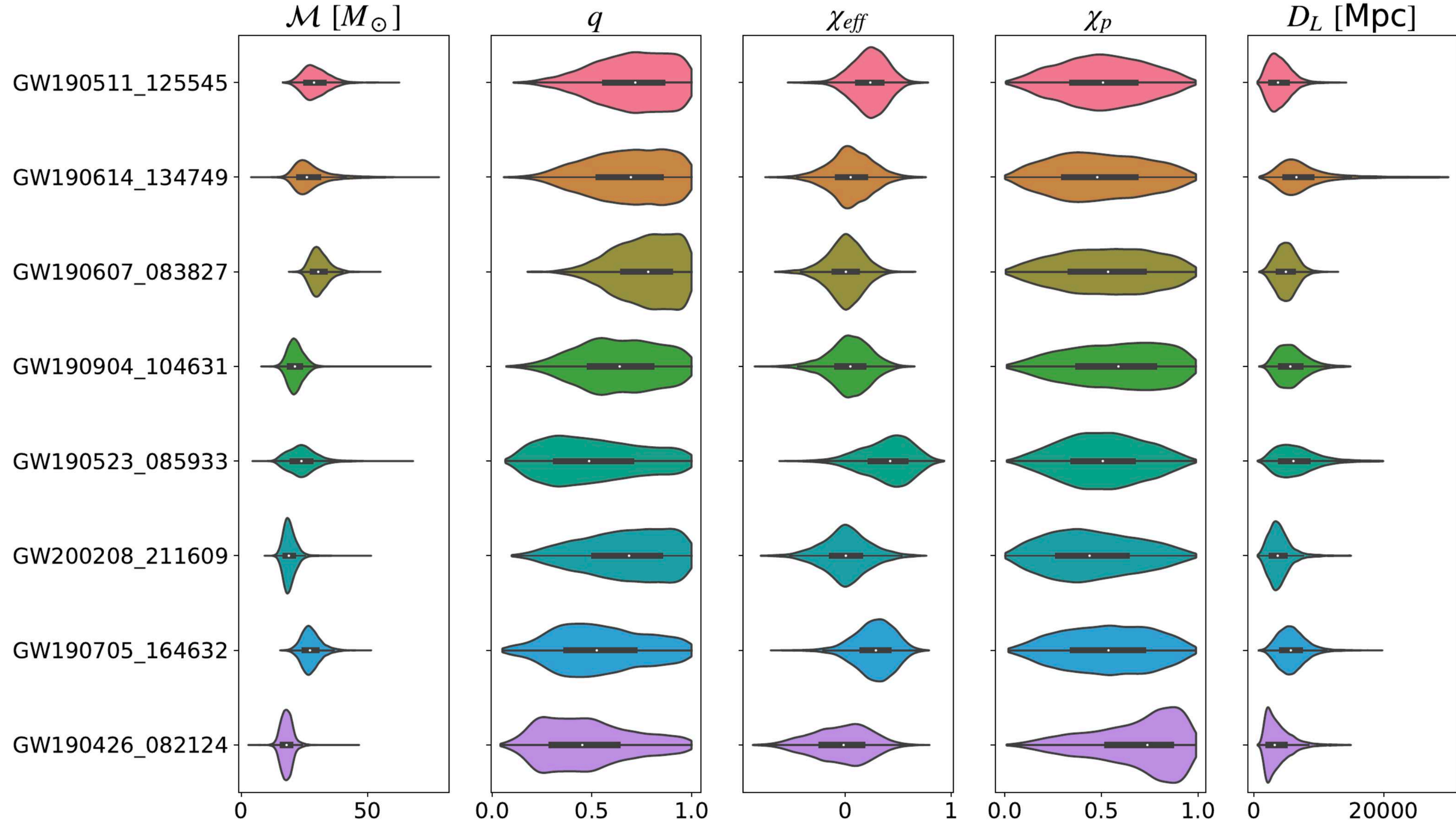
PARAMETER ESTIMATION USING BILBY

New candidate event
GW190511_125545

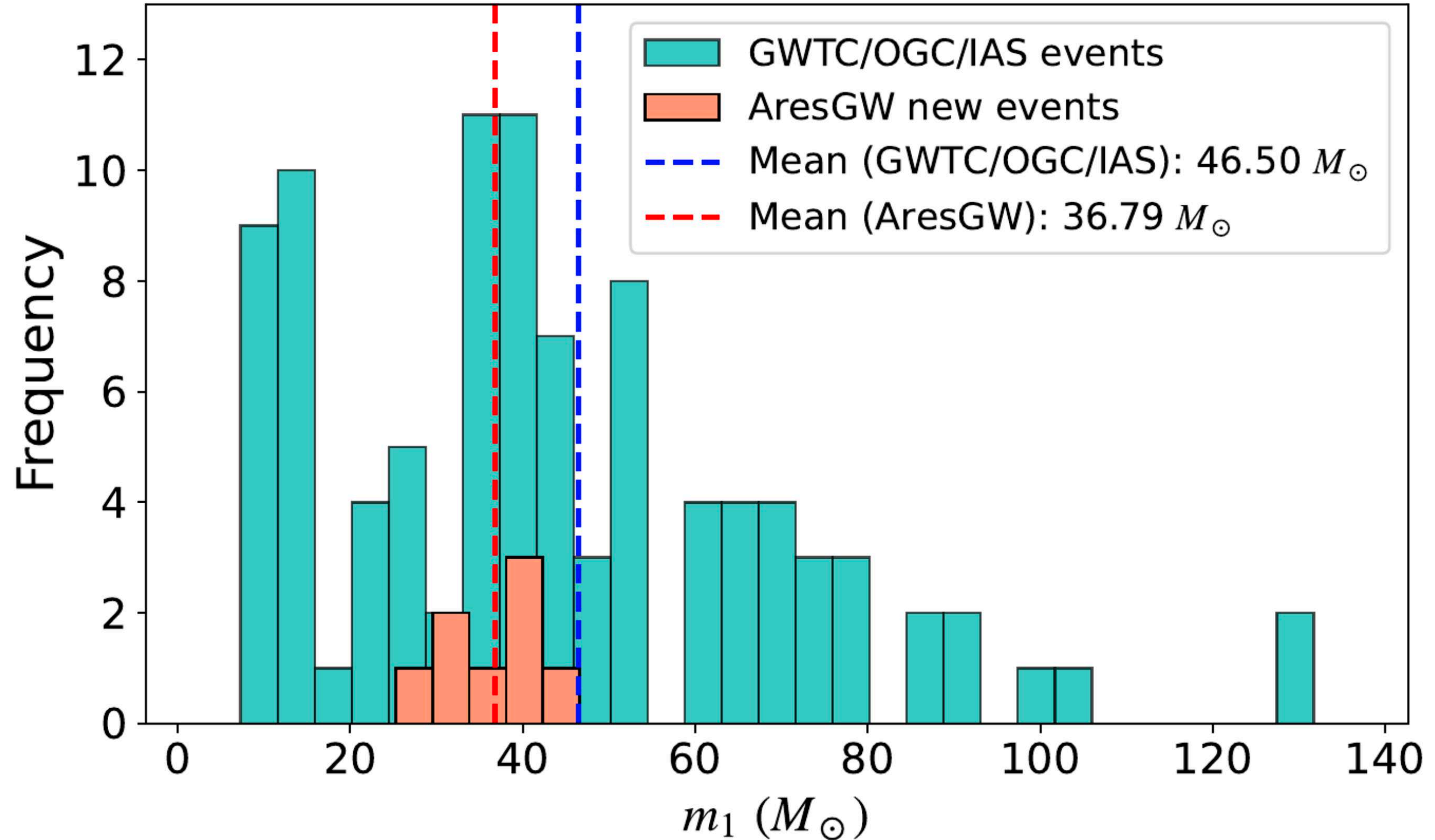
(Koloniari et al. 2025)



PARAMETER ESTIMATION USING BILBY



PARAMETER ESTIMATION USING BILBY



RECONSTRUCTED WAVEFORMS FOR NEW EVENTS

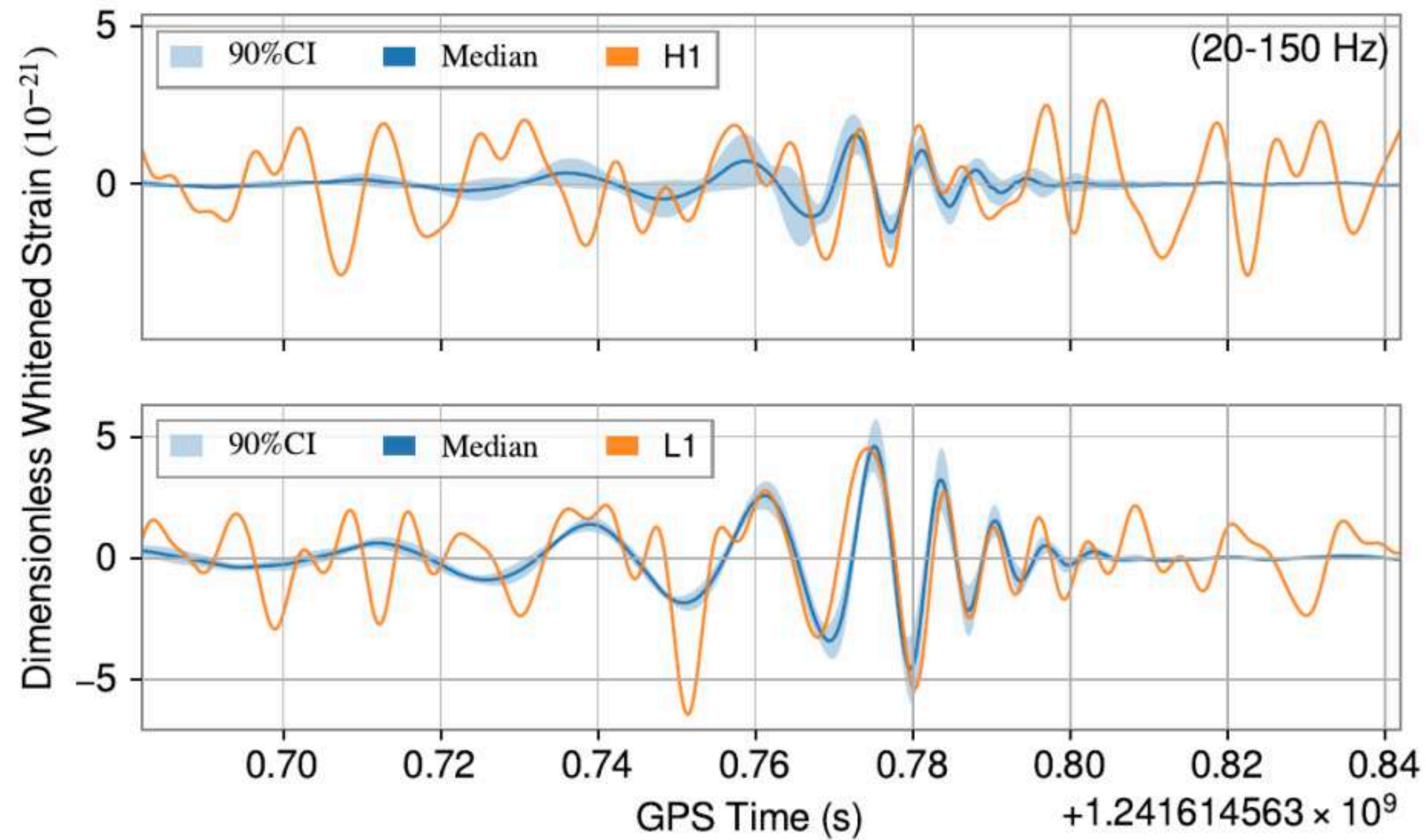


FIG. 35: Whitened, bandpassed strain data and reconstructed waveform for the new event GW190511_125545 identified by AresGW.

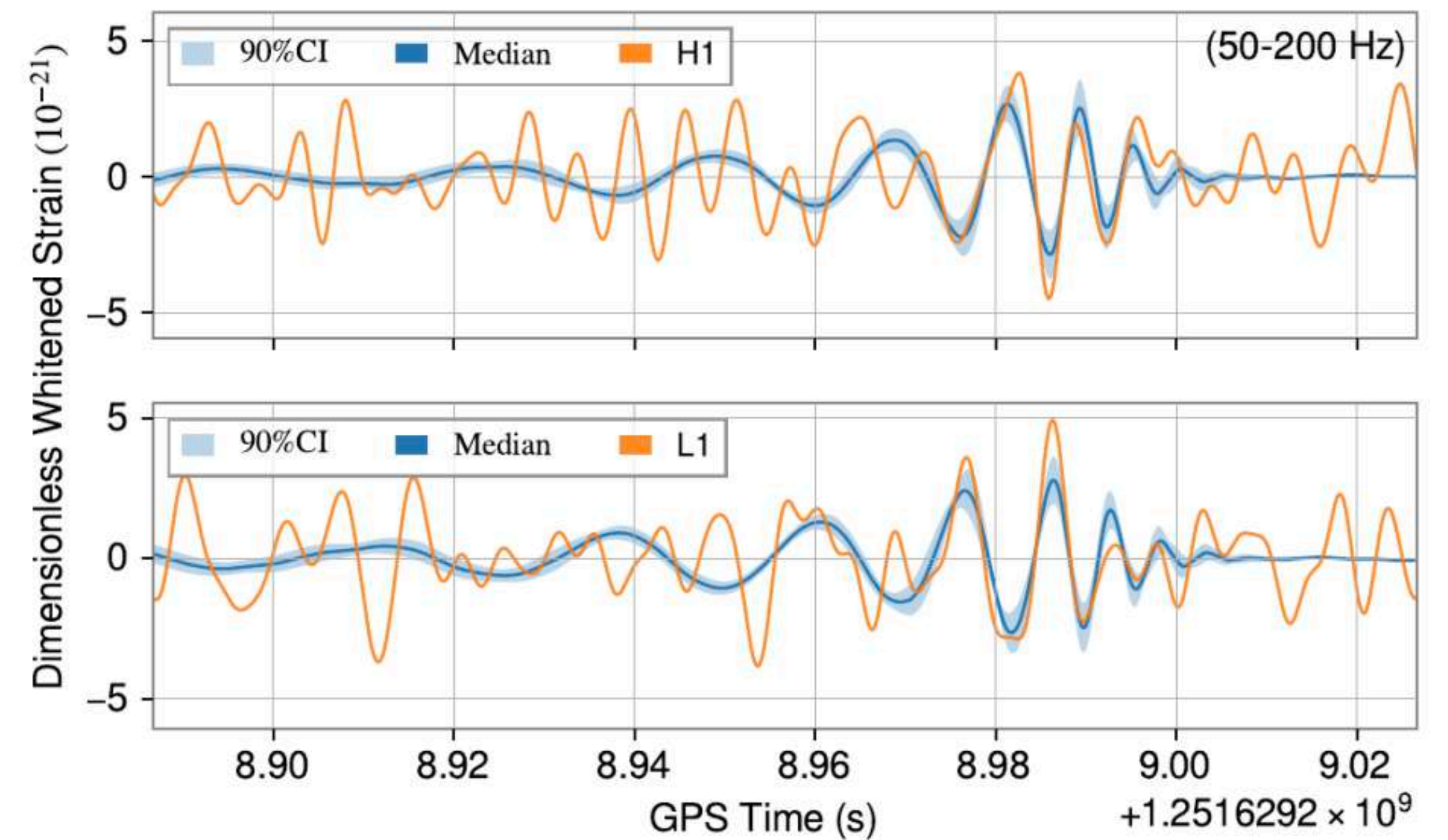
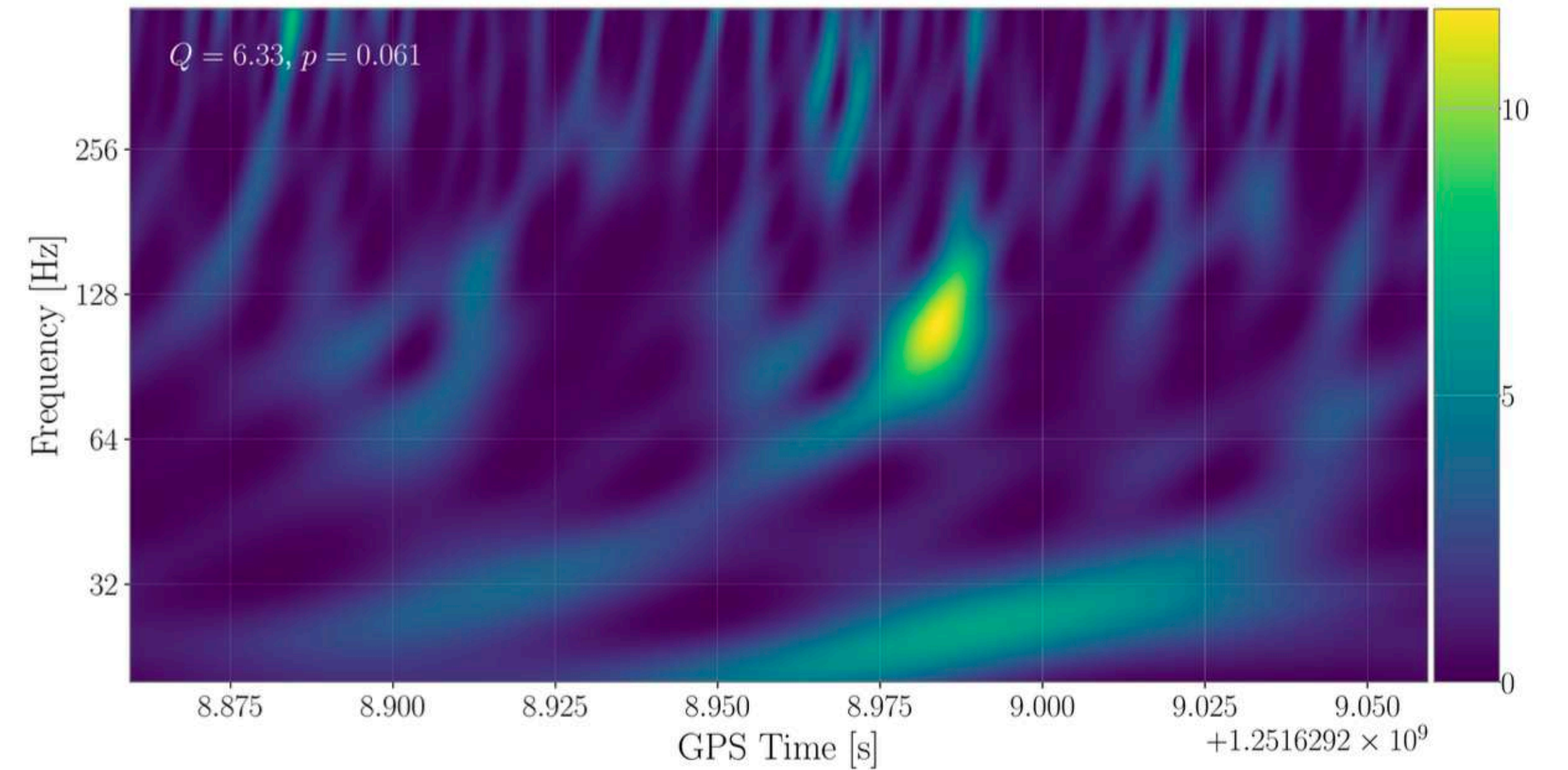
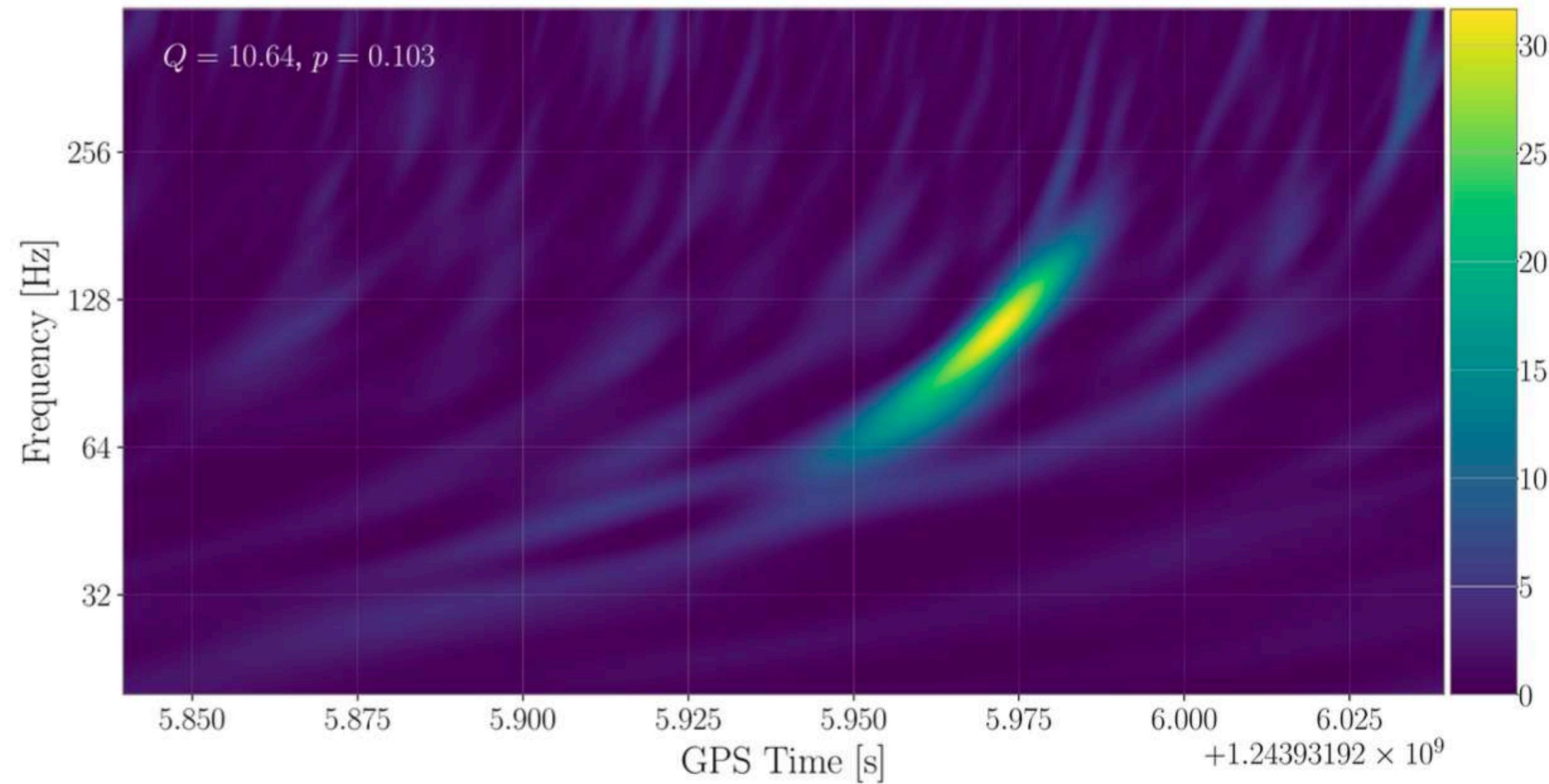
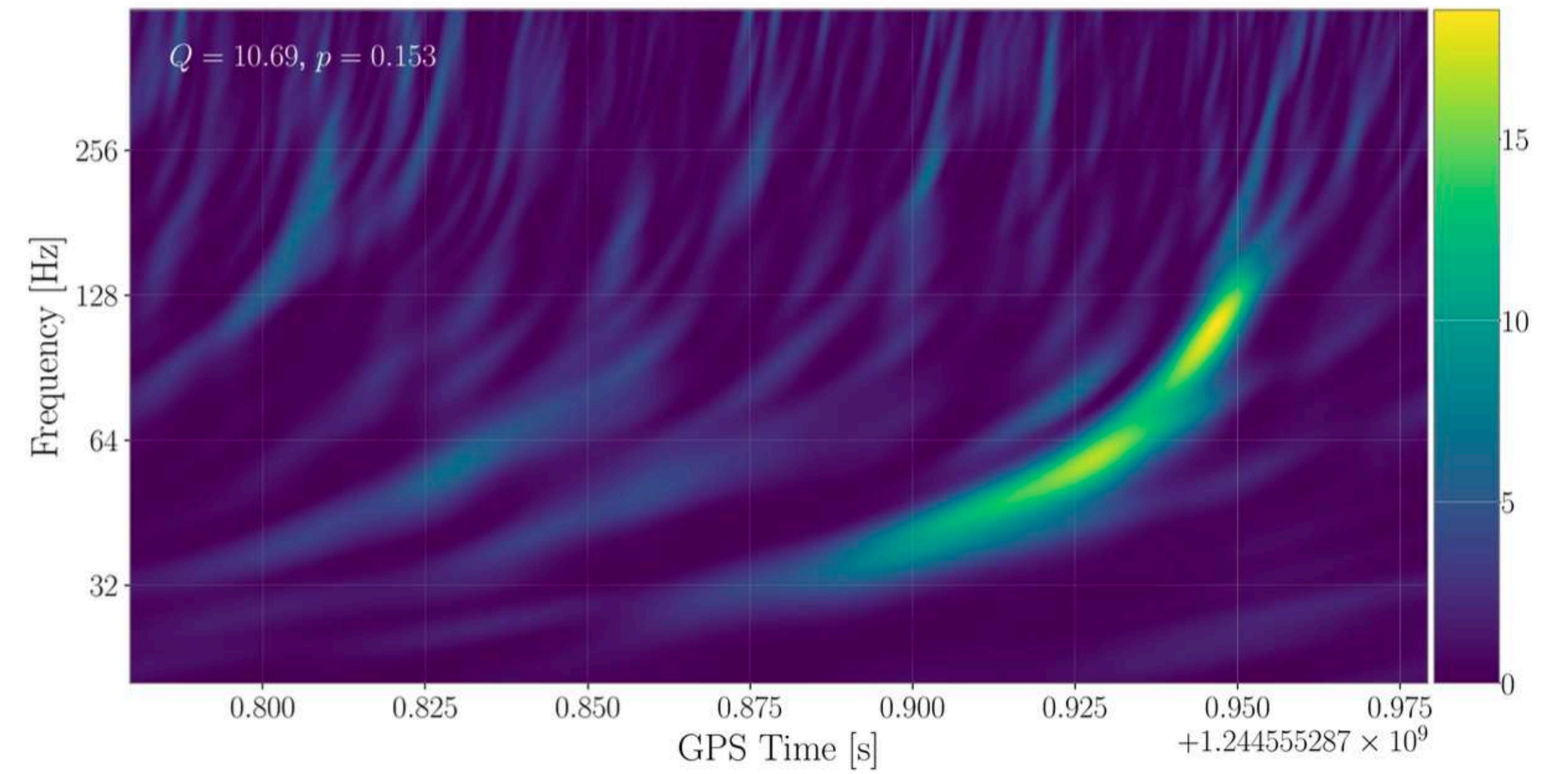
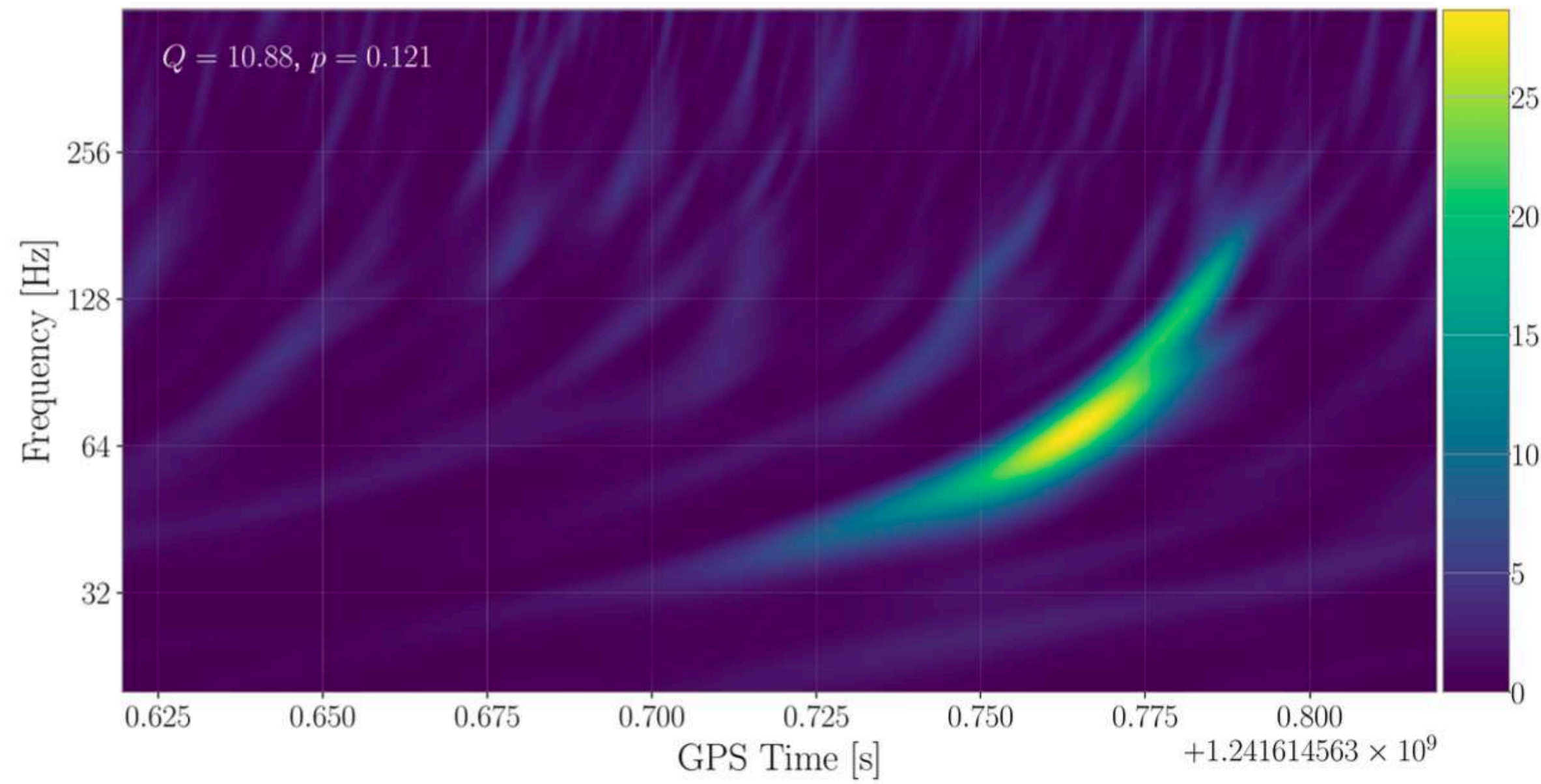


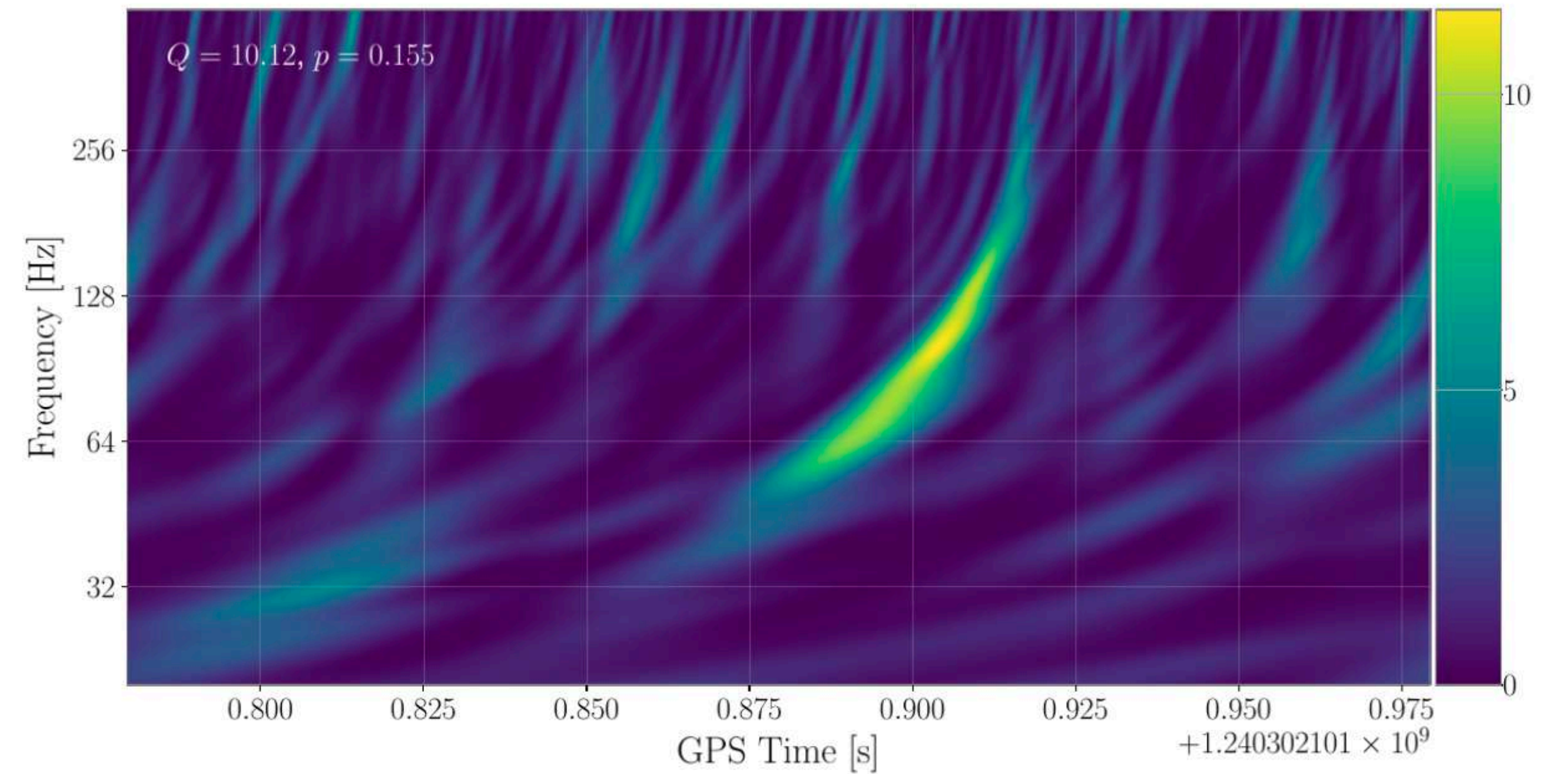
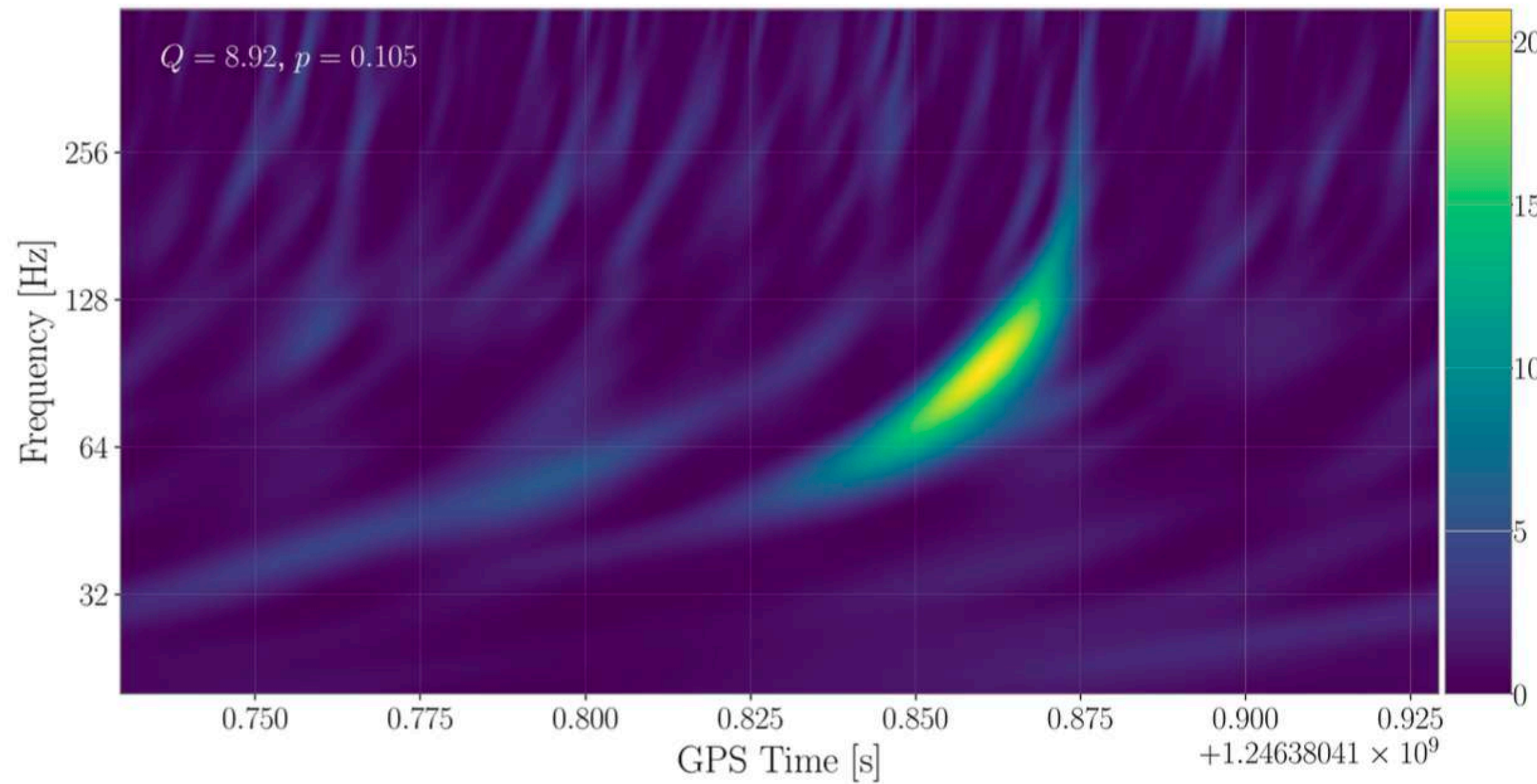
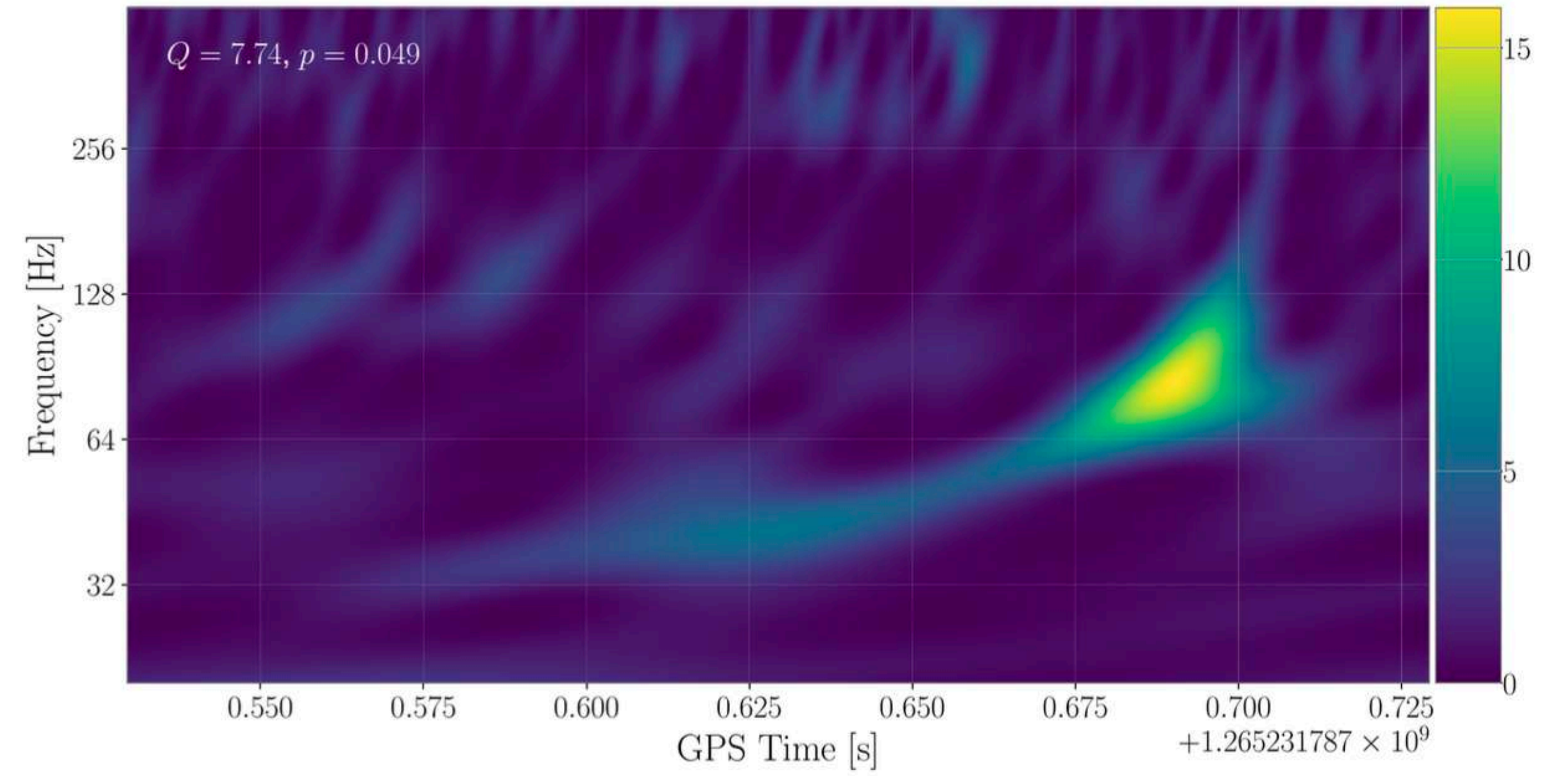
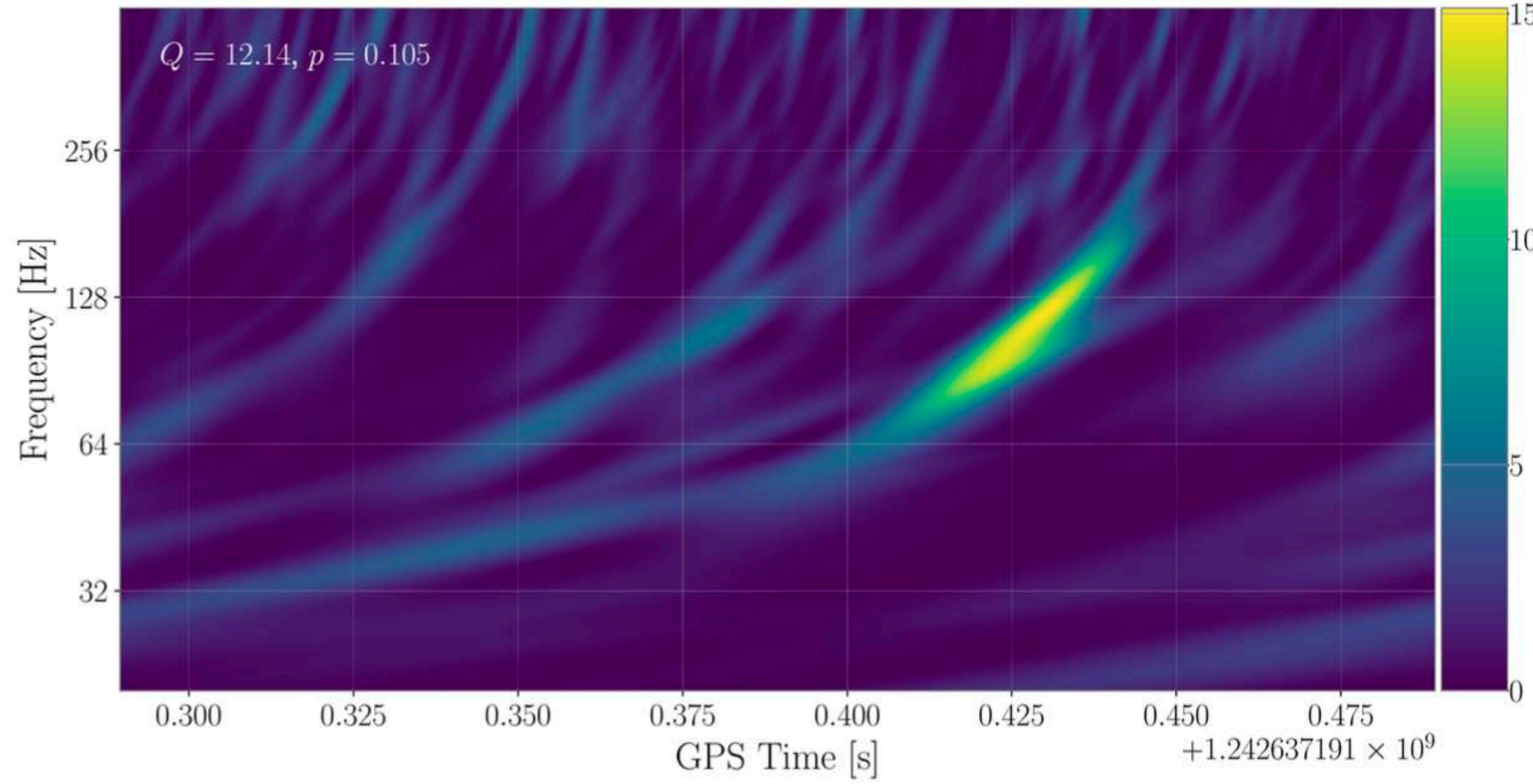
FIG. 38: Same as Fig. 35, but for the new event GW190904_104631.

Koloniari, Koursoumpa, Nousi, Lampropoulos, Passalis, Tefas, Stergioulas (2025)

ARESGW NEW CANDIDATE EVENTS



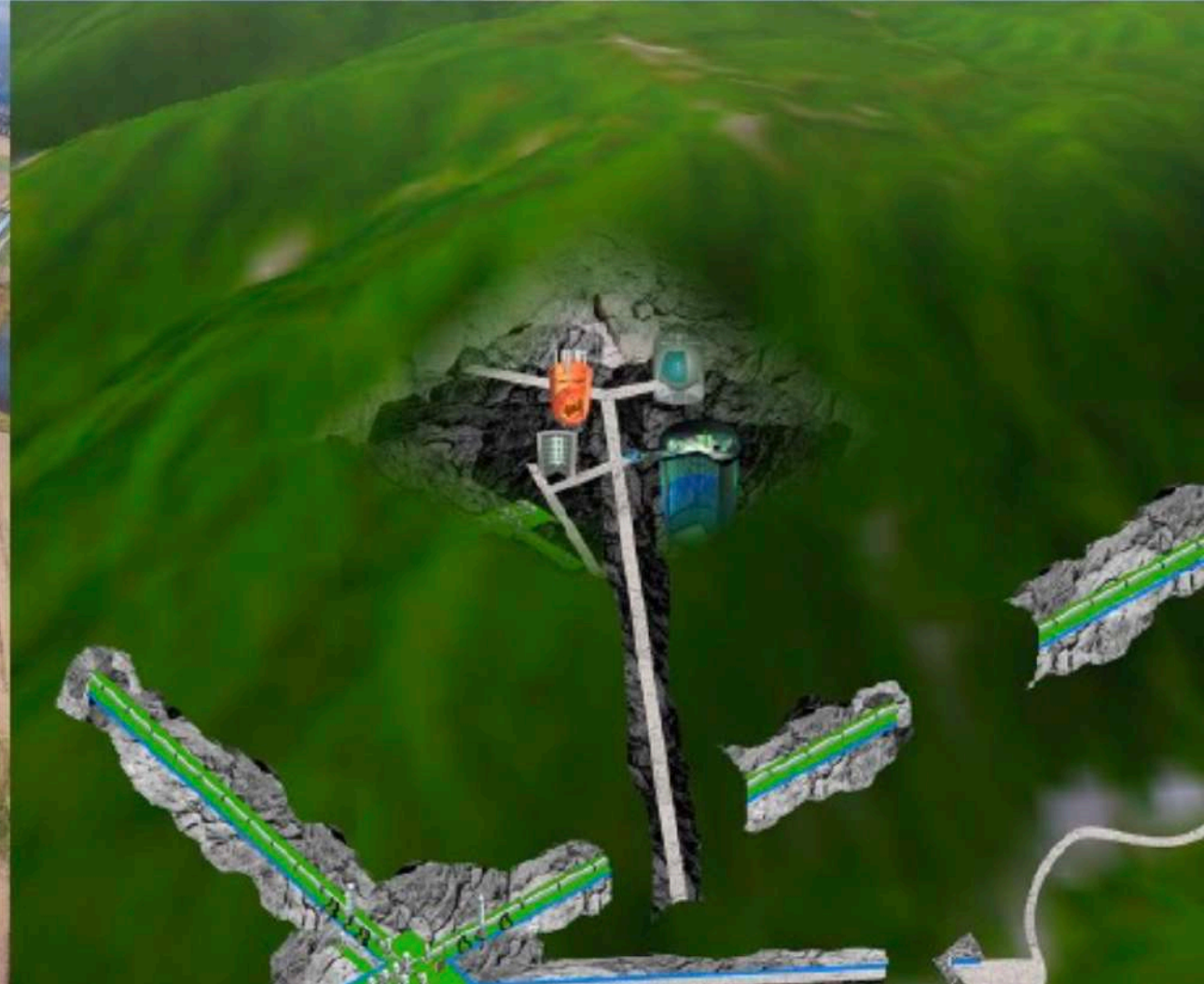
ARESGW NEW CANDIDATE EVENTS



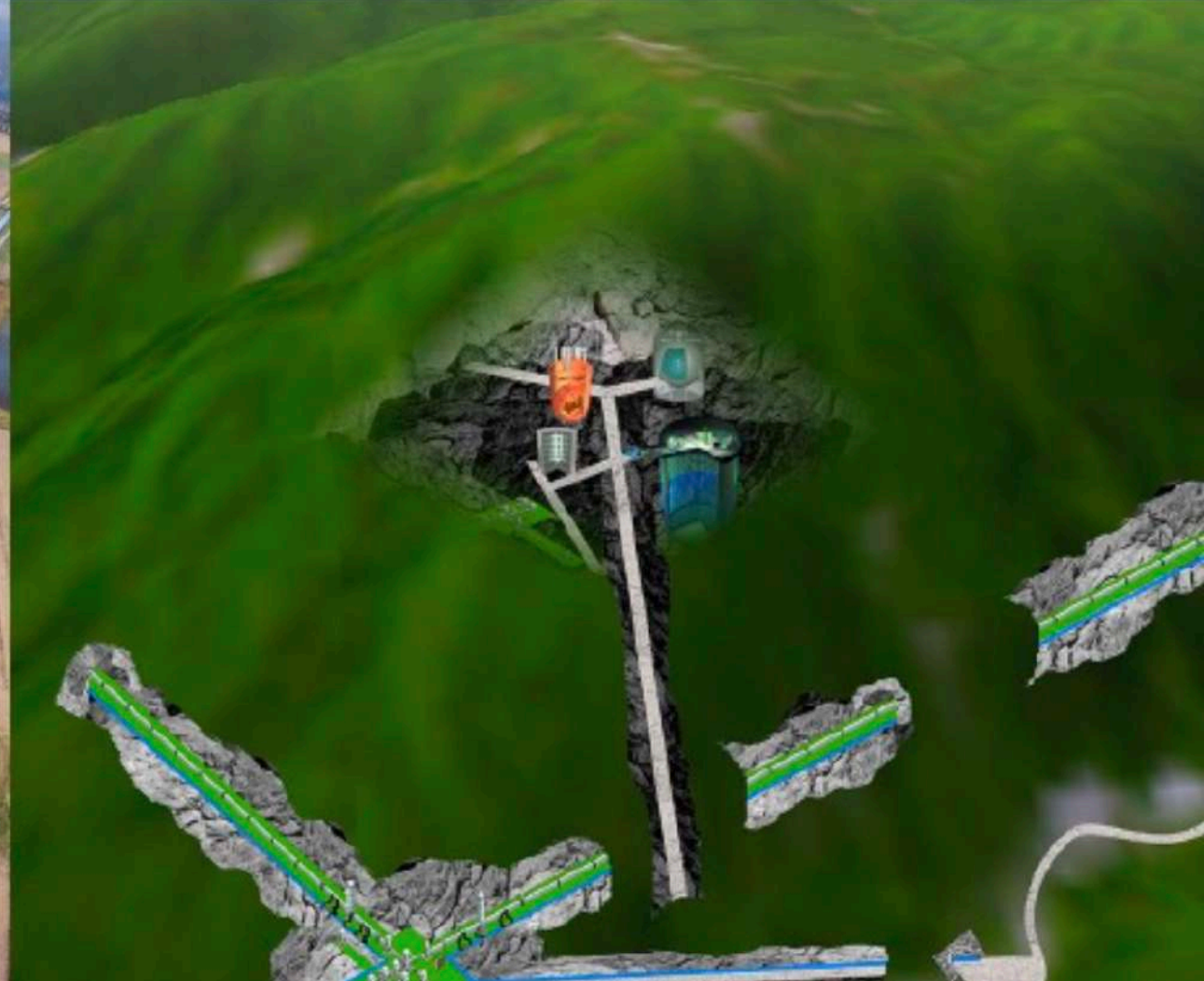
PART B.

BINARY NEUTRON STAR POST-MERGER PHASE

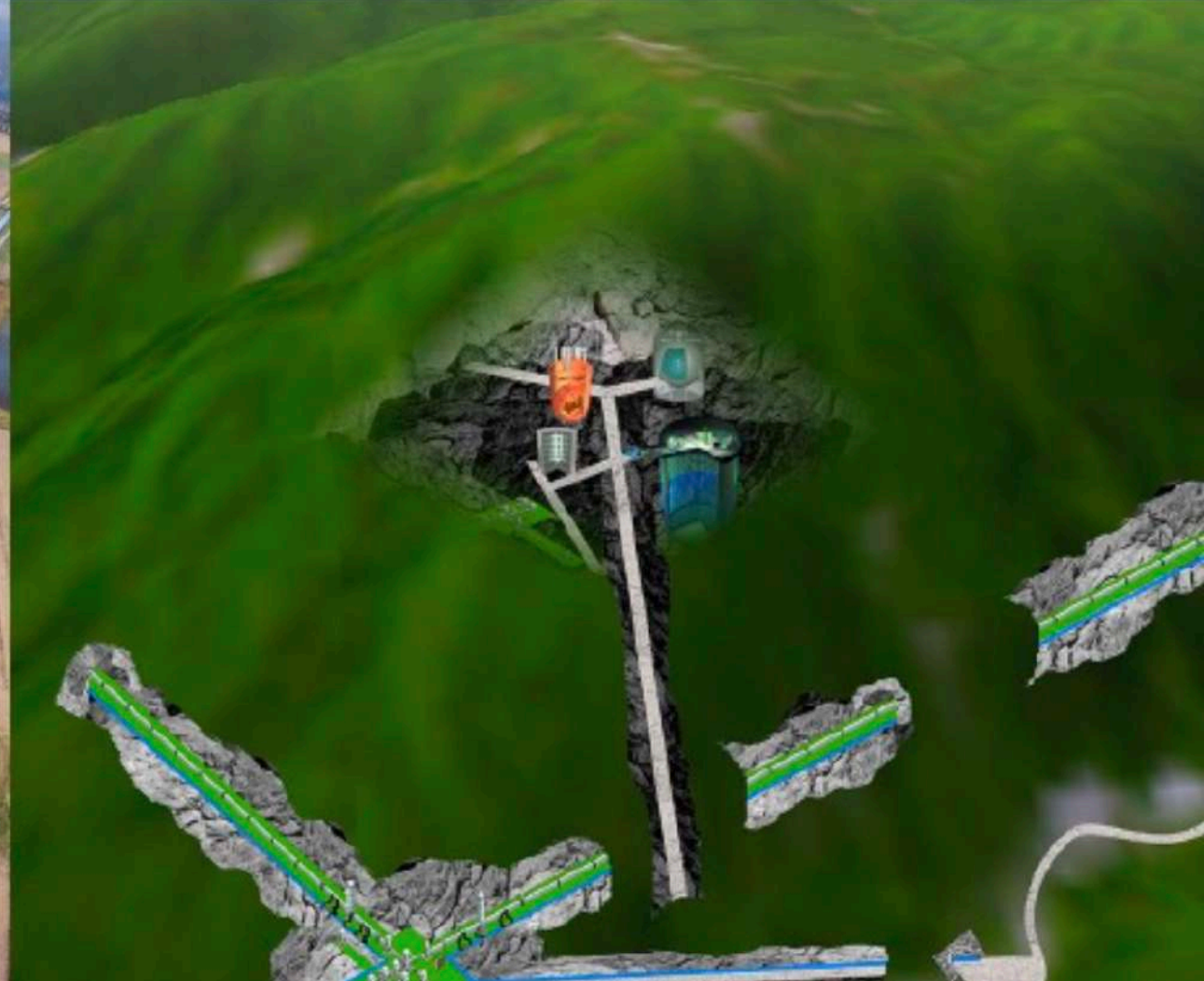
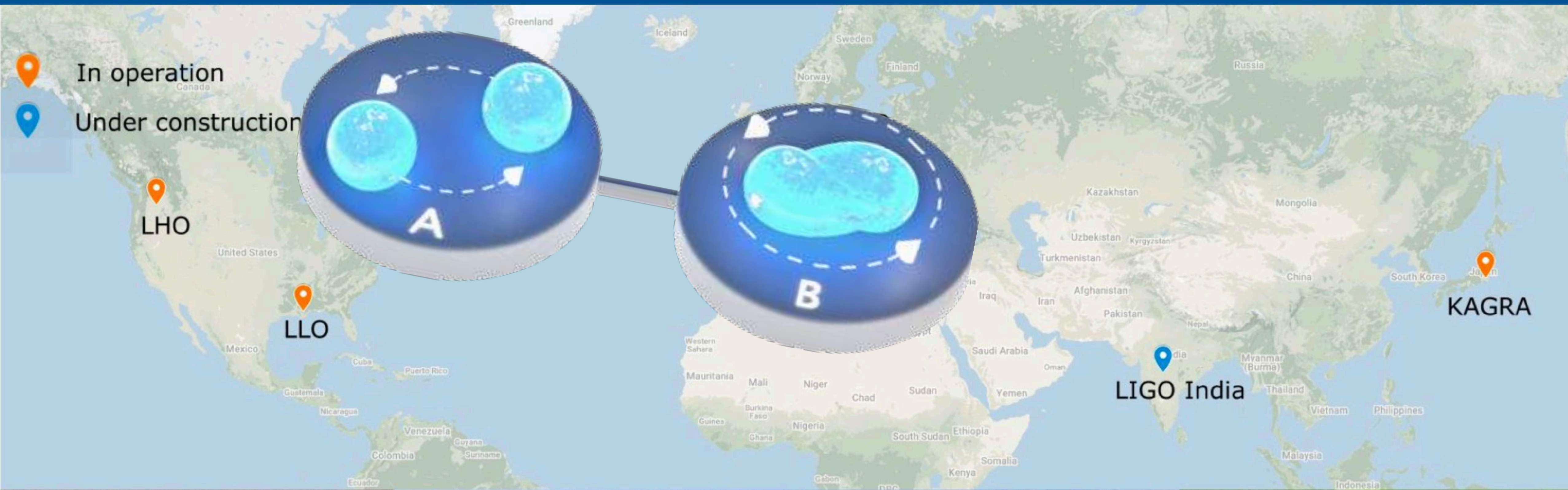
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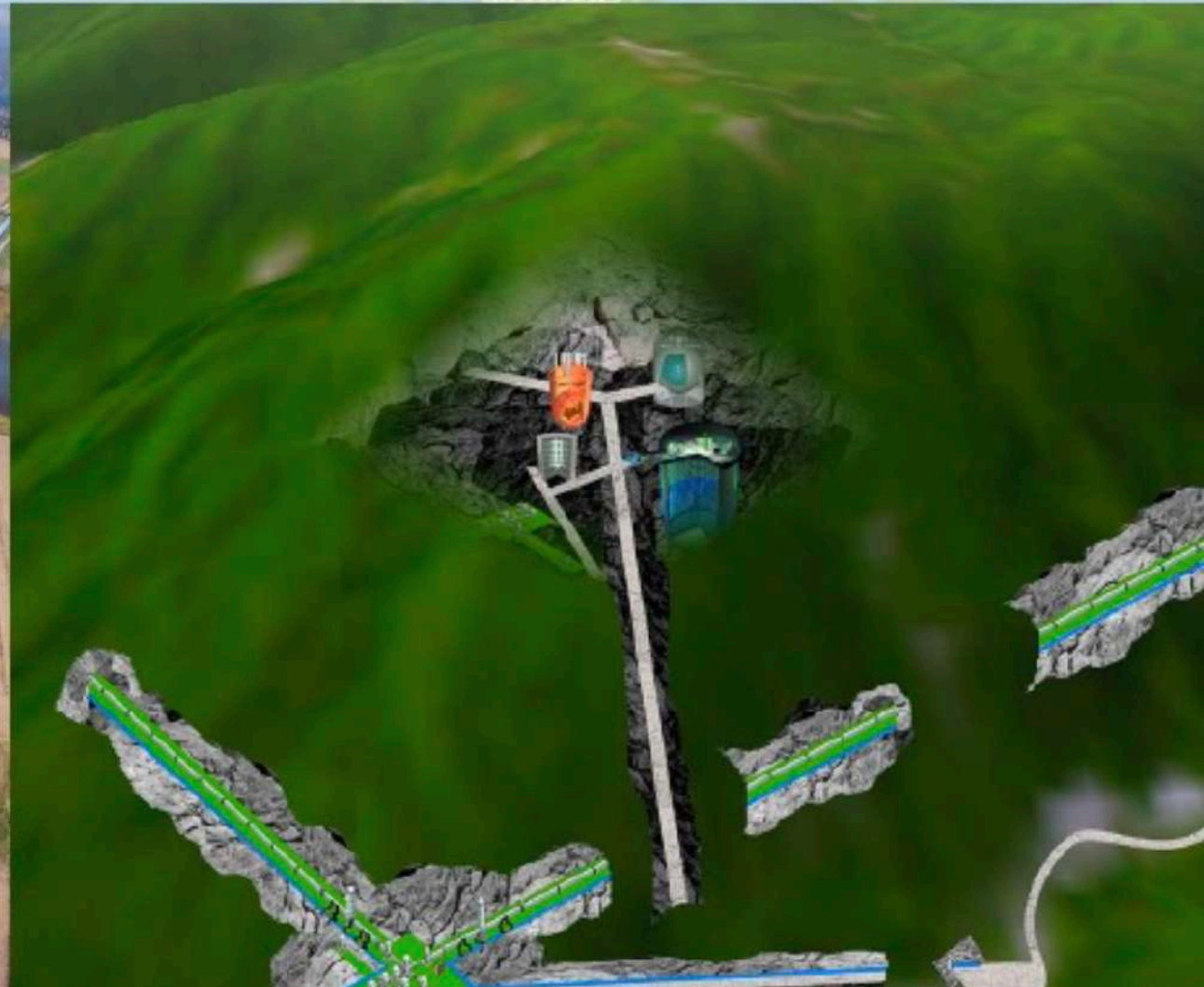
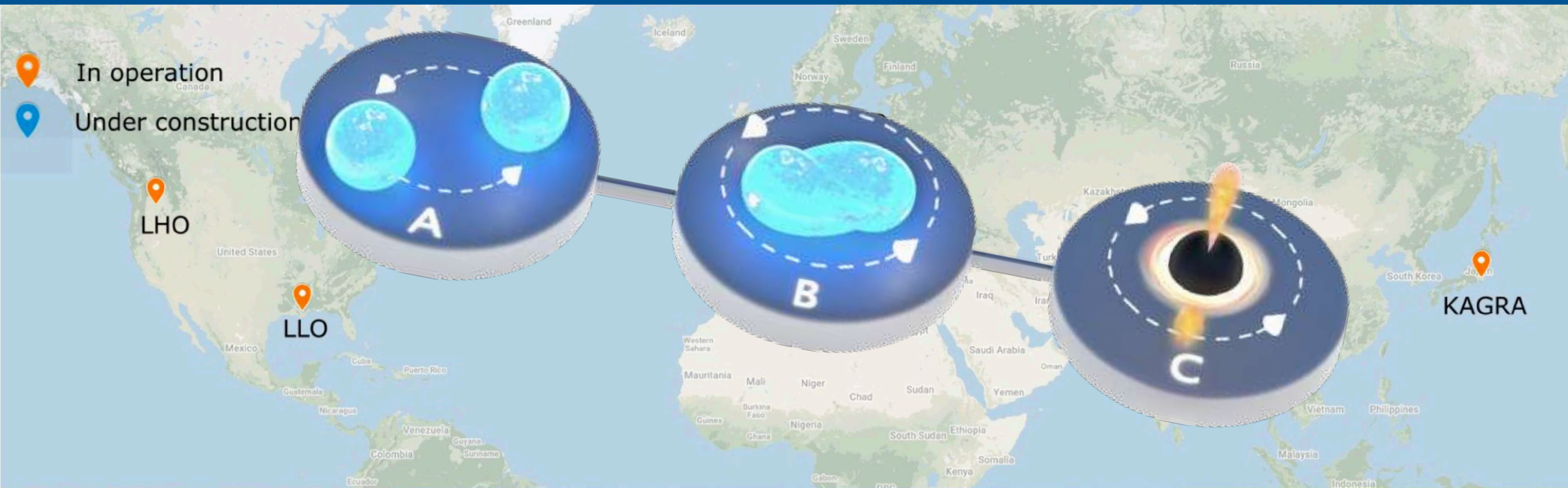
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



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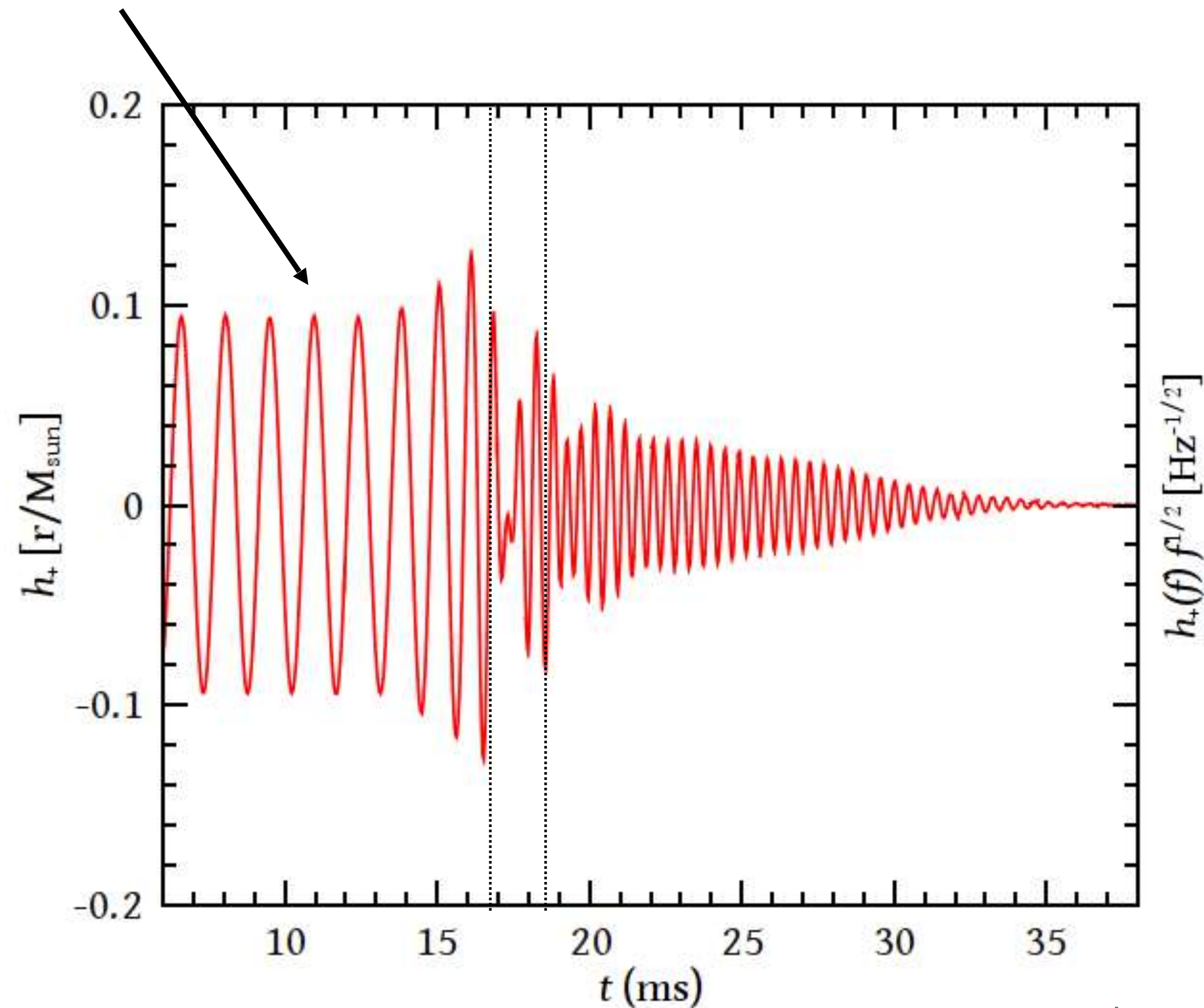


INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:
inspiral, *merger* and *post-merger oscillations*.

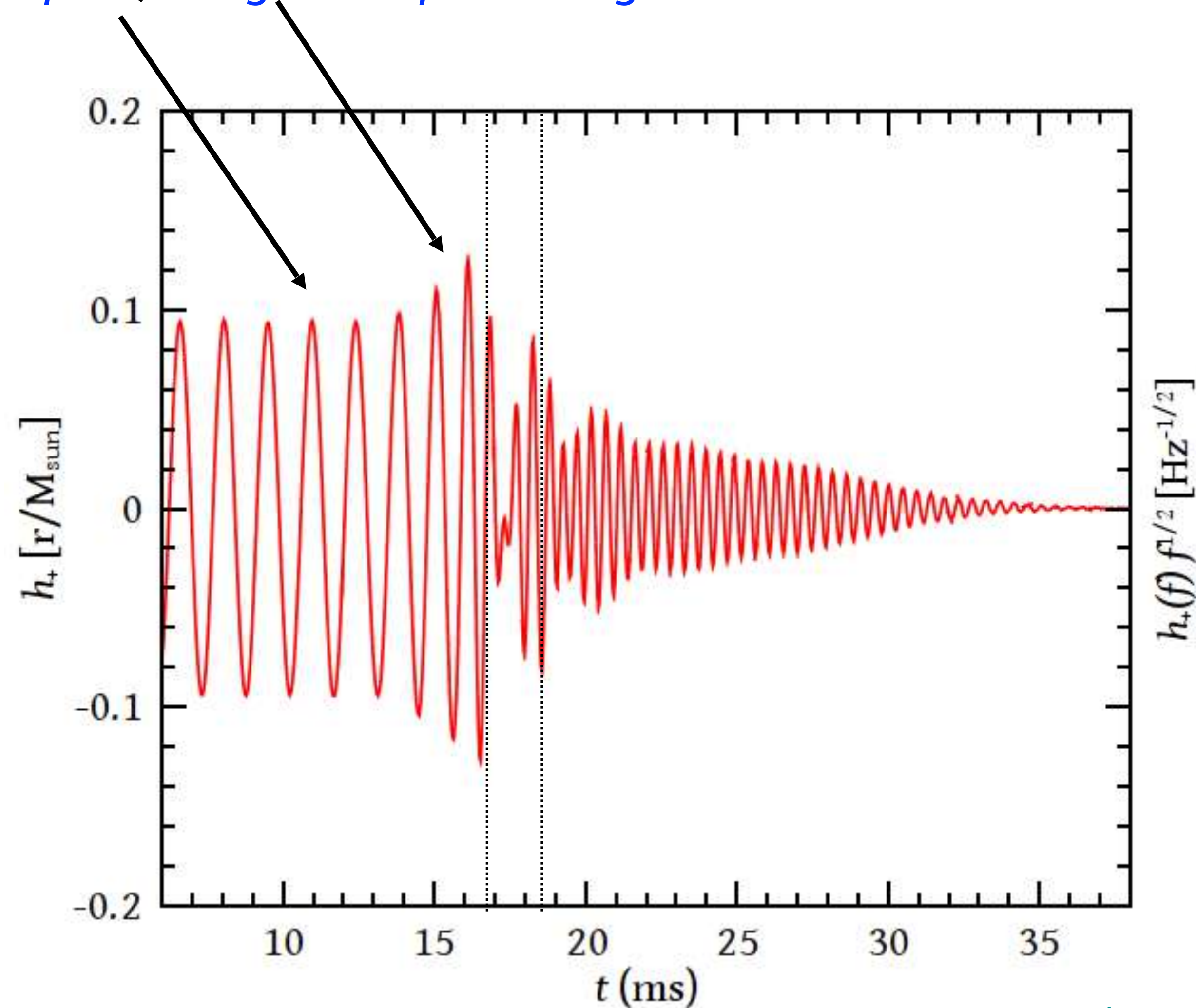


Stergioulas et al. (2011)

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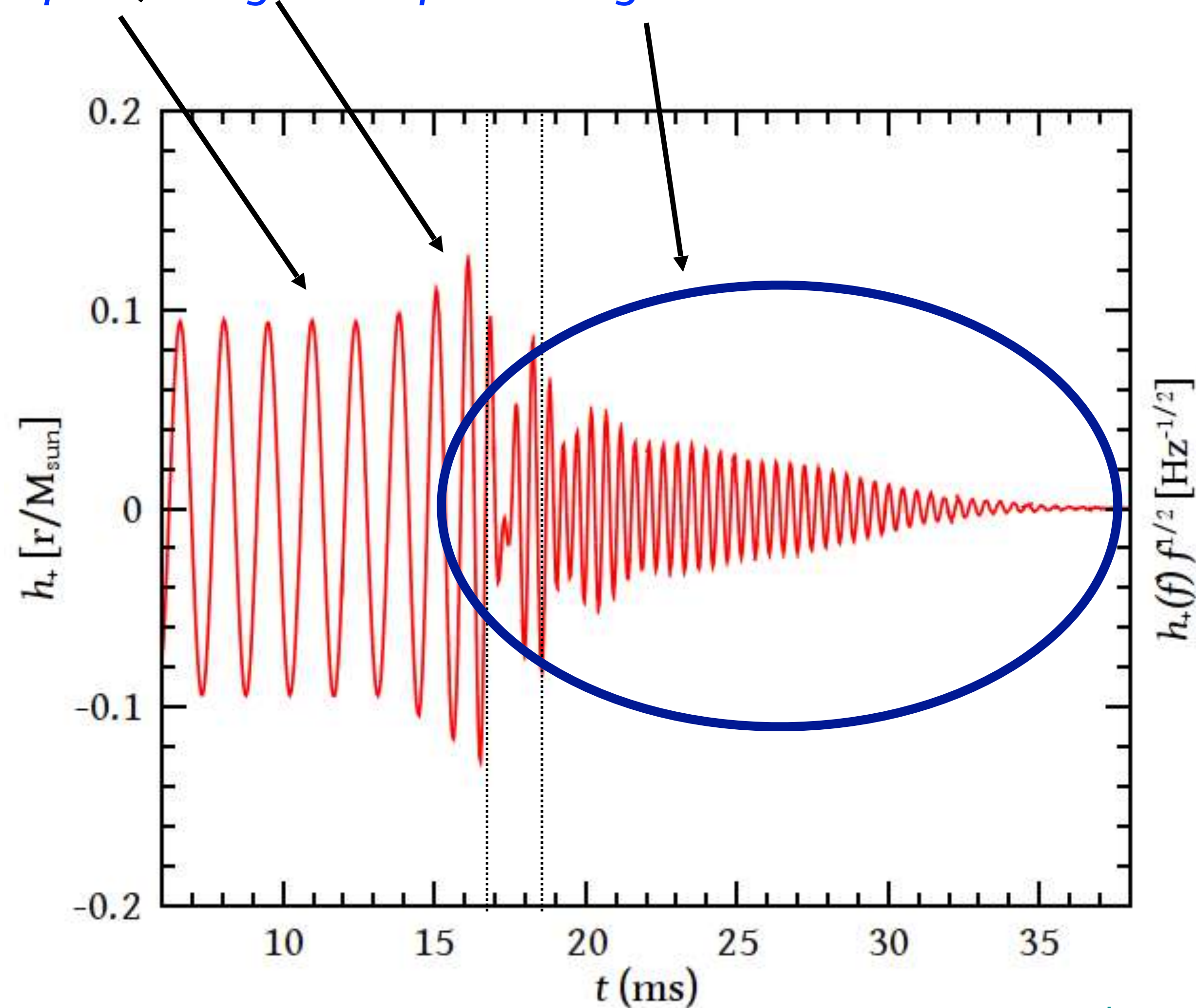


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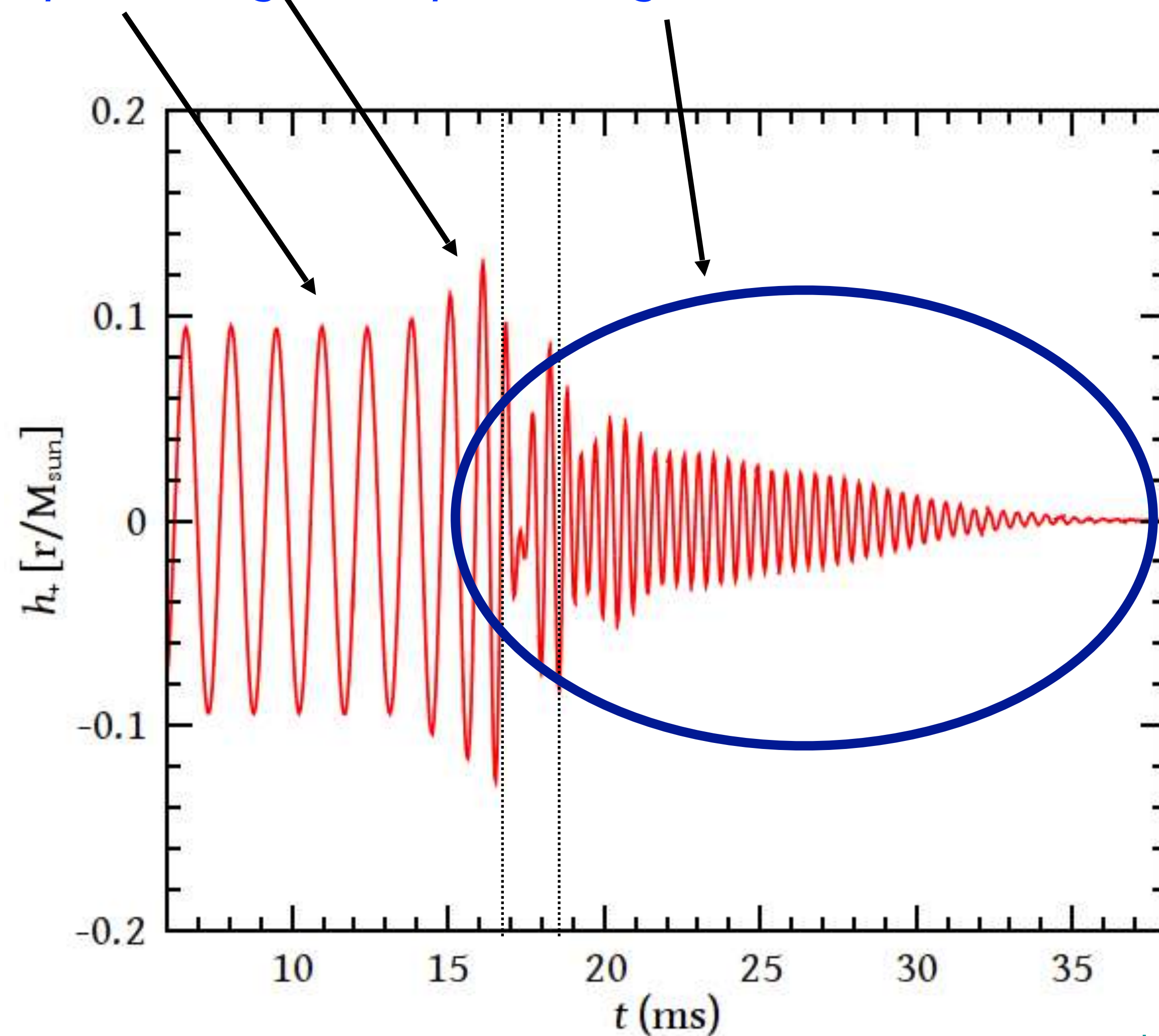


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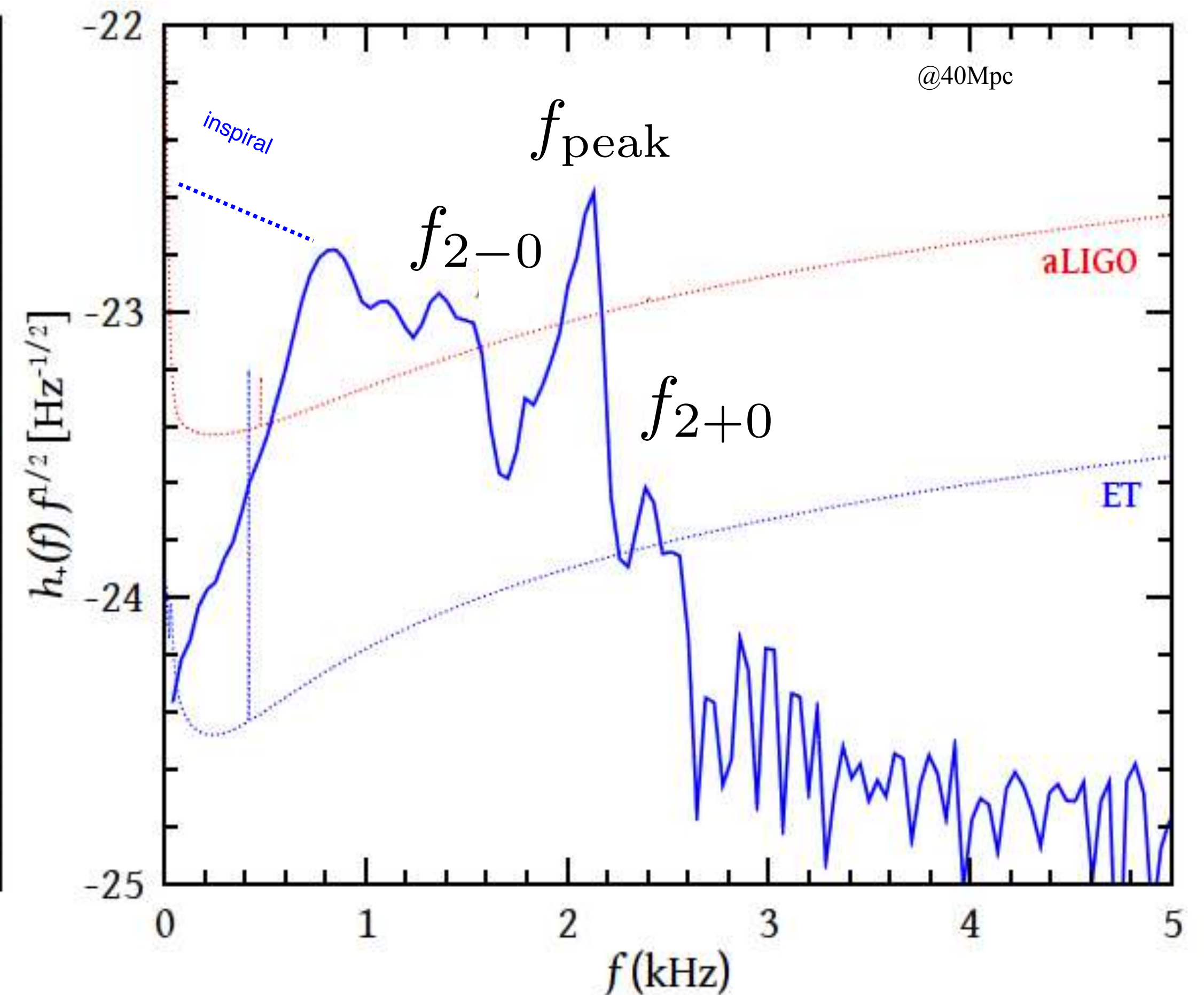
inspiral, *merger* and *post-merger oscillations*.



Frequency domain:

f_{peak} : $l=m=2$ fundamental mode.

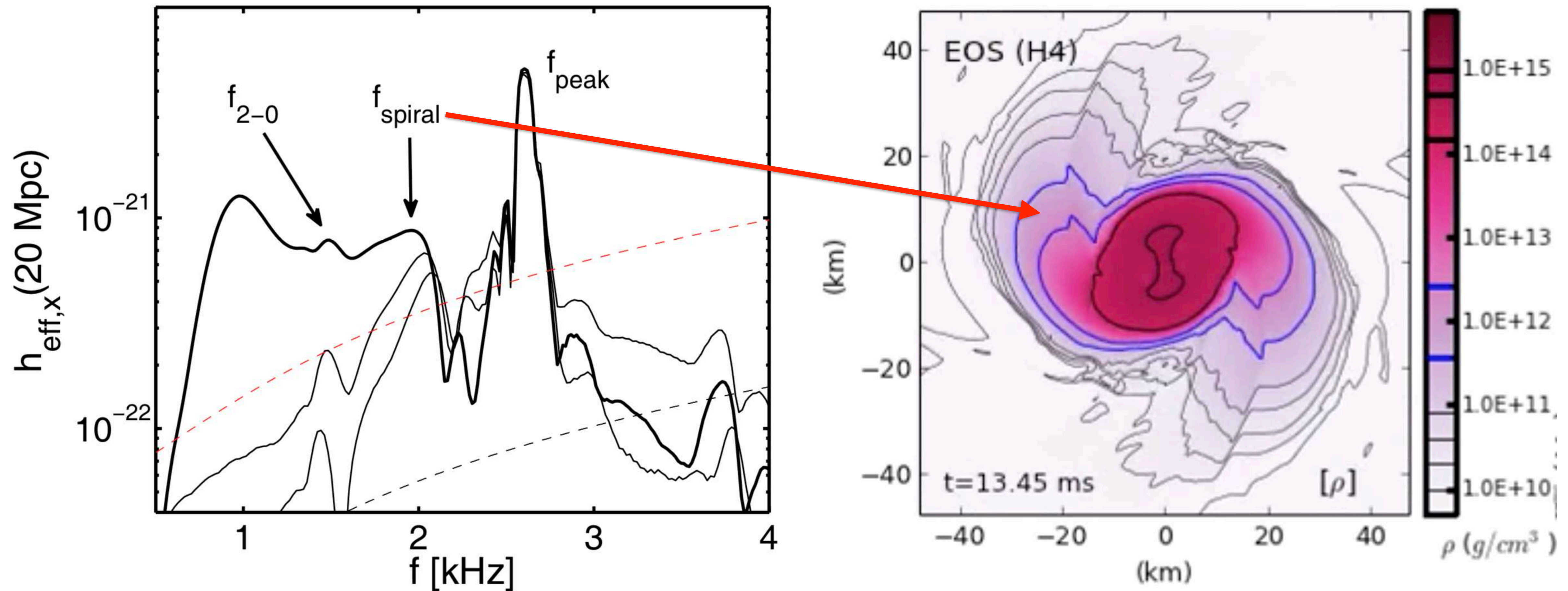
f_{2-0}, f_{2+0} : *nonlinear combination tones*



Stergioulas et al. (2011)

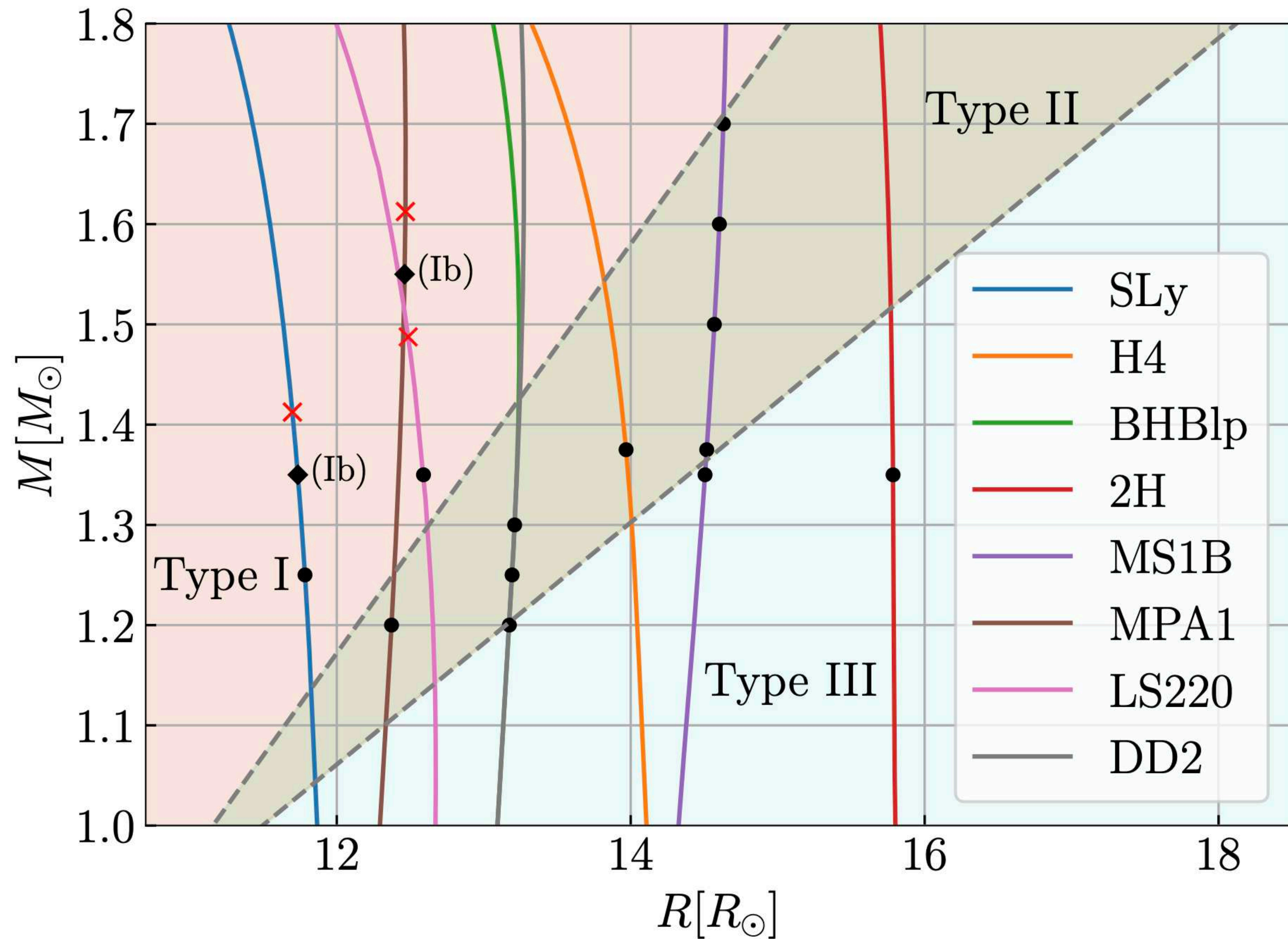
POST-MERGER PHASE IN BNS MERGERS

Orbiting spiral arms also lead to a distinct frequency f_{spiral}



Bauswein & Stergioulas (2015)

CLASSIFICATION OF POST-MERGER WAVEFORMS



Bauswein & Stergioulas (2015)

Vretinaris, Bauswein & Stergioulas (2020)

Type I:

f_{2-0} stronger than f_{spiral}

Type II:

f_{2-0} comparable to f_{spiral}

Type III:

f_{spiral} stronger than f_{2-0}

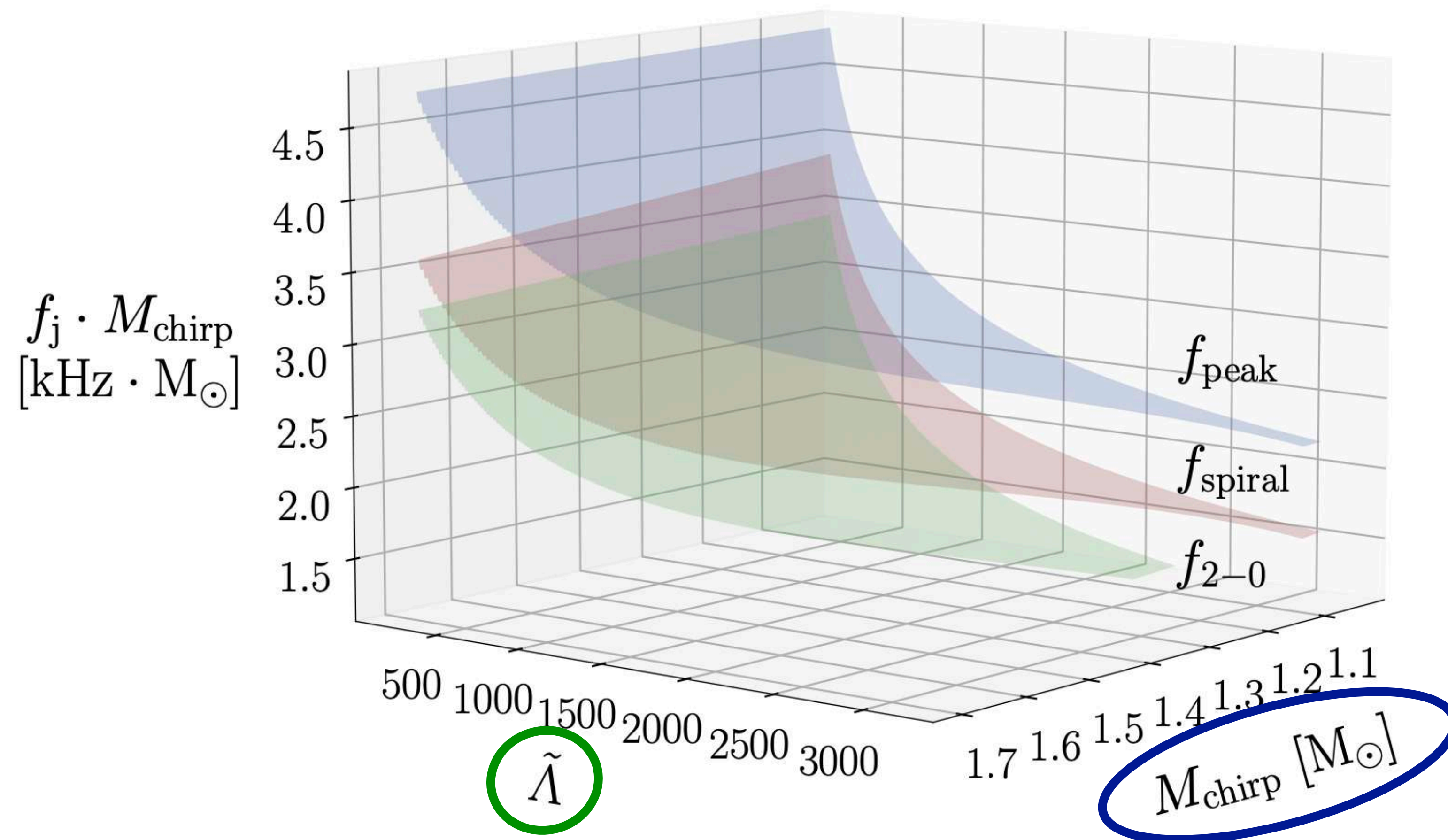
Type Ib:

(close to M_{thres})

Vretinaris et al. (2025)

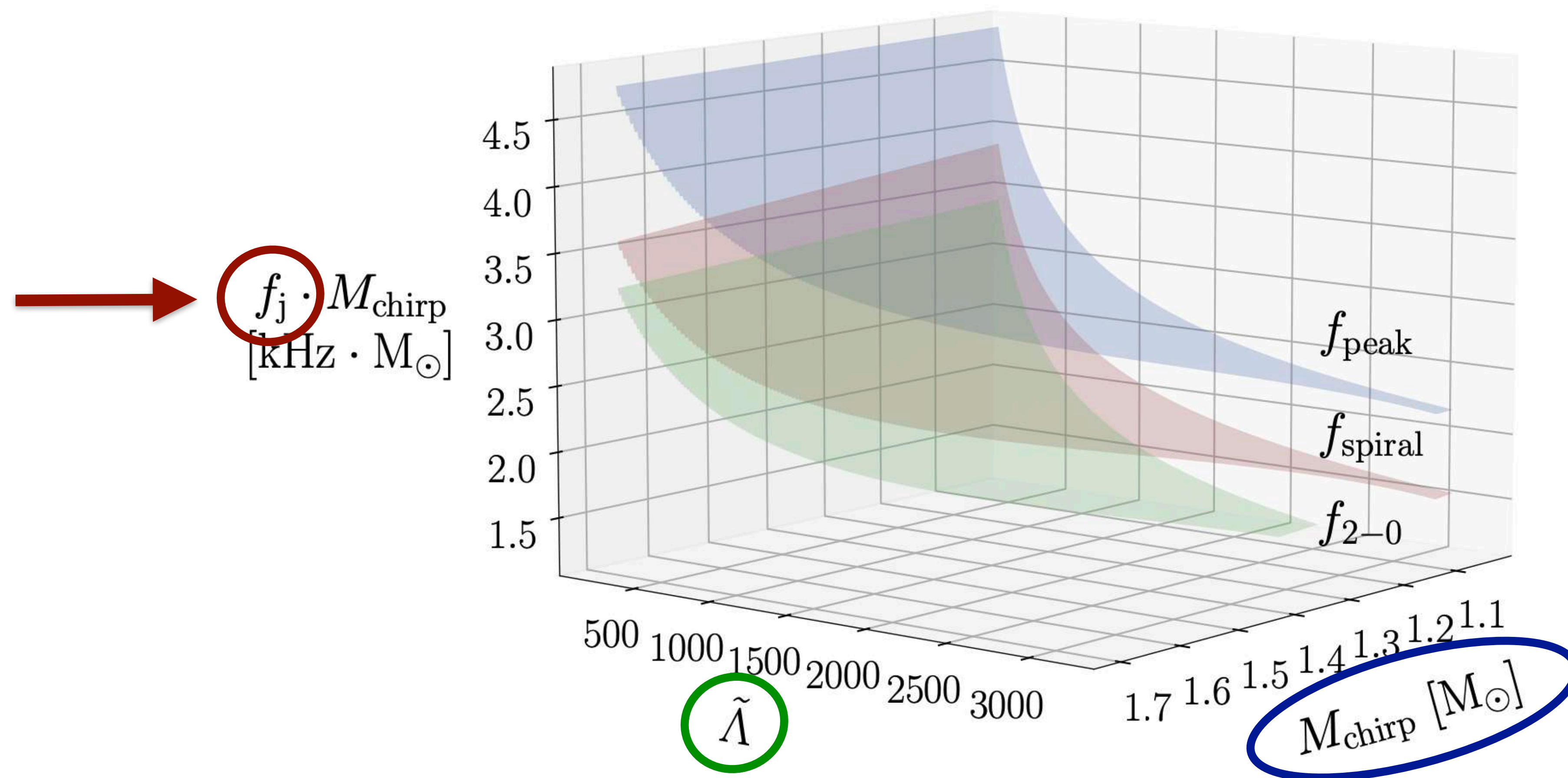
EMPIRICAL RELATIONS OF POST-MERGER FREQUENCIES

$$\begin{aligned} f_{\text{peak}} M_{\text{chirp}} &= 1.392 - 0.108 M_{\text{chirp}} + 51.70 \tilde{\Lambda}^{-1/2} && \text{Vretinaris, Bauswein \& Stergioulas (2020)} \\ f_{2-0} M_{\text{chirp}} &= 0.558 - 0.406 M_{\text{chirp}} + 48.696 \tilde{\Lambda}^{-1/2} && \text{Vretinaris et al. (2025)} \\ f_{\text{spiral}} M_{\text{chirp}} &= 1.2 - 0.442 M_{\text{chirp}} + 45.819 \tilde{\Lambda}^{-1/2} && \text{Vretinaris et al. (2025)} \end{aligned}$$



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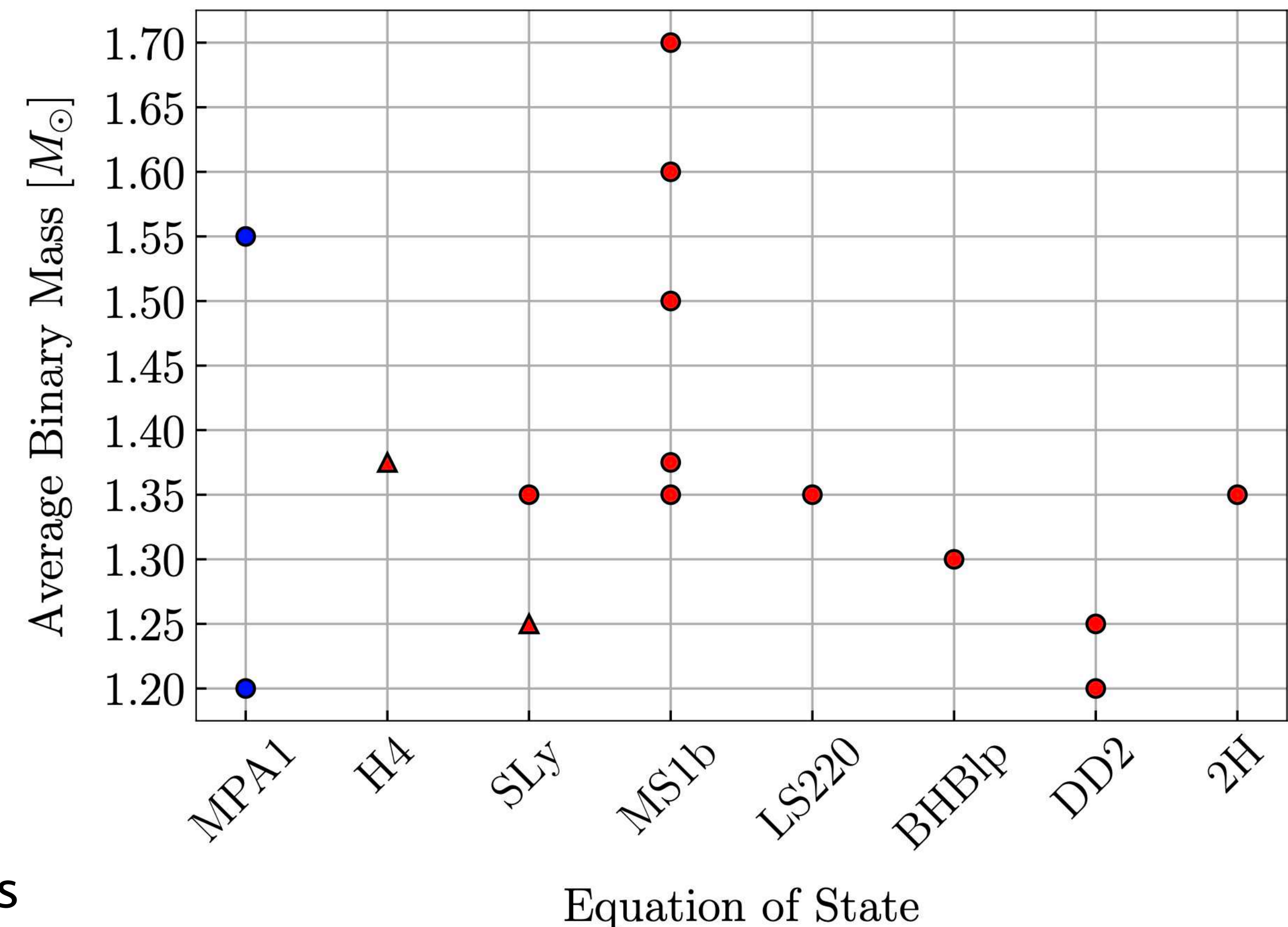
ACCELERATION OF POST-MERGER INFERENCE

13 numerical waveforms from the CoRe database (Gonzalez et al. 2022)

+2 numerical waveforms from Souldanis, Bauswein & Stergioulas (2022)

Label	EOS	q	(Average) Mass	References
THC:0036:R03	SLy	1.0	1.350	[47]
THC:0019:R05	LS220	1.0	1.350	[101, 102]
BAM:0088:R01	MS1b	1.0	1.500	[99, 100]
THC:0002:R01	BHBlp	1.0	1.300	[101, 102]
THC:0011:R01	DD2	1.0	1.250	[101, 102]
BAM:0070:R01	MS1b	1.0	1.375	[103]
BAM:0065:R03	MS1b	1.0	1.350	[104]
THC:0010:R01	DD2	1.0	1.200	[101, 102]
BAM:0002:R02	2H	1.0	1.350	[104]
BAM:0053:R01	H4	1.5	1.375	[105]
BAM:0124:R01	SLy	1.5	1.250	[103]
BAM:0090:R02	MS1b	1.0	1.600	[99, 100]
BAM:0092:R02	MS1b	1.0	1.700	[99, 100]
Souldanis et al.	MPA1	1.0	1.200	[67]
Souldanis et al.	MPA1	1.0	1.550	[67]

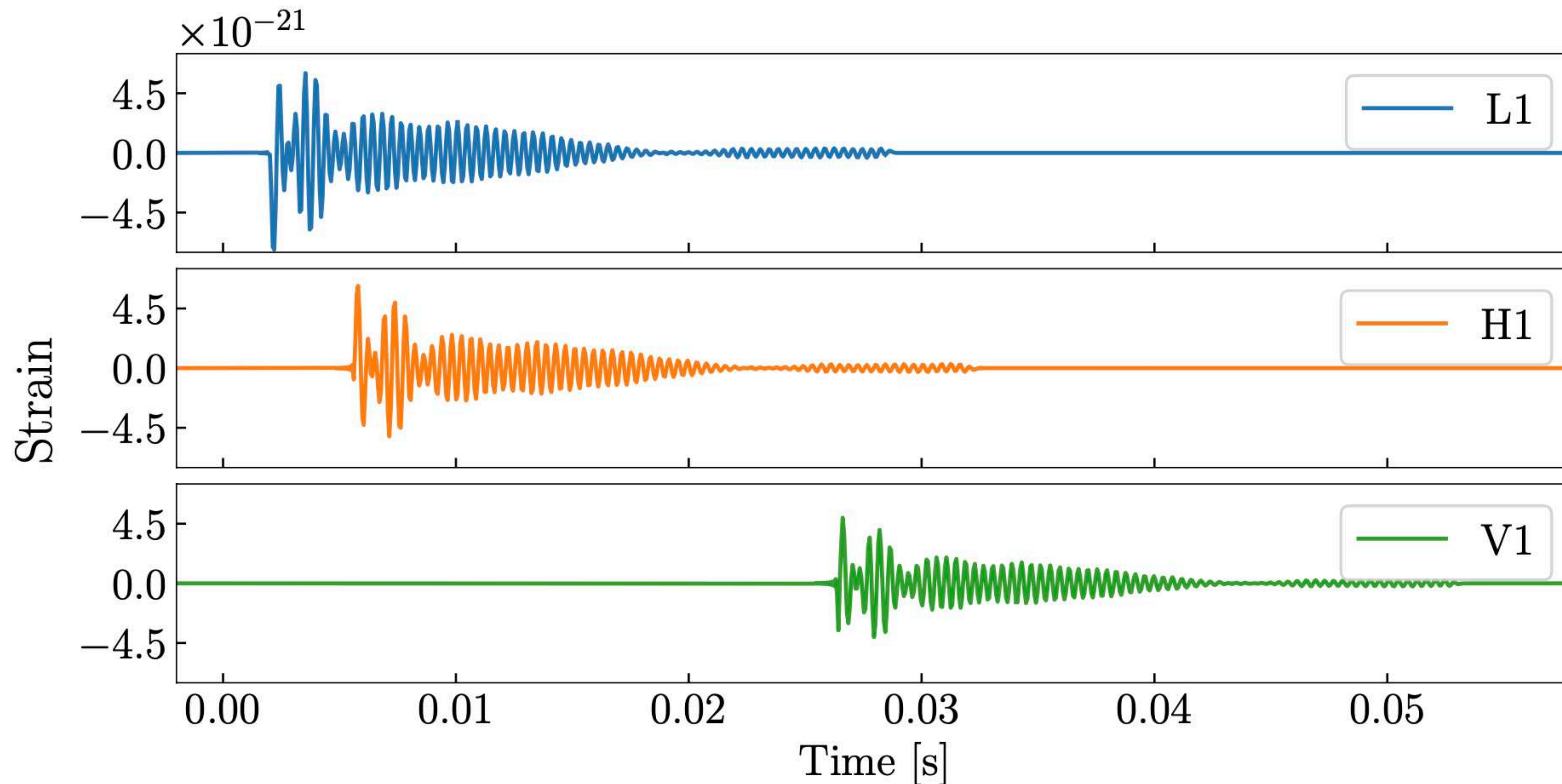
Extension of the set of 9 waveforms used in previous work by Easter et al. (2020)



INJECTIONS IN 3-DETECTOR NETWORK

Waveforms are injected in 3-detector HLV network at design sensitivity, using BILBY (Ashton et al. 2019)

We choose post-merger SNR of 8, 16 and 50, to simulate detection by 3G network (ET/CE) at distances as close as 200Mpc.



Several analytic models exist in the time- and frequency-domains.

Here, we extend the analytic model of Easter et al. (2020) as follows:

$$\begin{aligned} h(\boldsymbol{\theta}, t) &= h_+(\boldsymbol{\theta}, t) - ih_\times(\boldsymbol{\theta}, t) \\ &= \sum_{j=1}^4 [h_{j,+}(\boldsymbol{\theta}, t) - ih_{j,\times}(\boldsymbol{\theta}, t)] \\ h_{j,+}(\boldsymbol{\theta}, t) &= A_j \exp \left[-\frac{t}{T_j} \right] \cos [2\pi f_j t (1 + a_j t) + \psi_j] \end{aligned}$$

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Intrinsic parameters

$$\boldsymbol{\theta} = \{A_j, T_j, f_j, a_j, \psi_j\} \quad \text{for } j \in [1, 4]$$

$h_{j,\times}(\boldsymbol{\theta}, t)$ is obtained by applying a $\pi/2$ phase shift to $h_{j,+}(\boldsymbol{\theta}, t)$

- We have added a 4th oscillator at high frequencies $> f_{\text{peak}}$ (e.g. f_{2+0})
- Amplitudes A_j are free parameters

INFORMED PRIORS

In Easter et al. (2020) flat priors in a wide frequency range of 1-5 kHz for every oscillator were used.

- Here, we take advantage of the [empirical relations](#) to set [Gaussian priors](#) in a [narrow frequency range](#) around each expected frequency.
- In addition, the priors [differ](#), according to the [type of the post-merger](#) waveform:
 - Type I: Gaussian priors, $\mathcal{N}(f_{2-0}, \sigma^2)$ for f_{2-0} and uniform priors $\mathcal{U}(1, 5)[\text{kHz}]$ for f_{spiral} .
 - Type II: Gaussian priors, $\mathcal{N}(f_{2-0}, \sigma^2)$ for f_{2-0} and $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$ for f_{spiral} .
 - Type III: Gaussian priors, $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$ for f_{spiral} and uniform priors $\mathcal{U}(1, 5)[\text{kHz}]$ for f_{2-0} .

where $\sigma = 3 \times \text{max error of empirical relations}$. For f_{peak} : Gaussian ; for f_4 : flat in $[f_{\text{peak}} + 0.3\text{kHz}, 5\text{kHz}]$.

priors for A_j : uniform in $[-24, -19]$

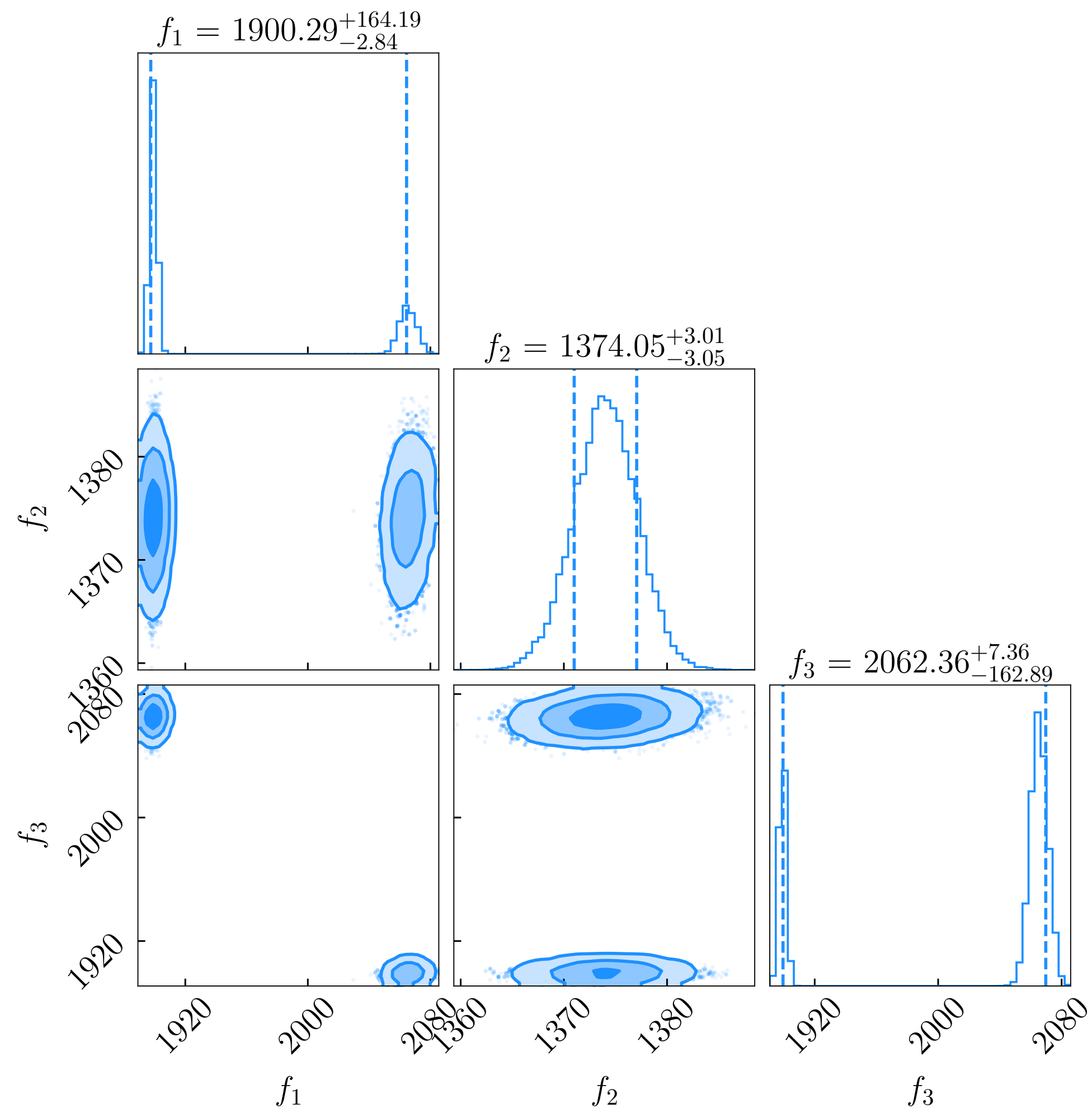
priors for a_j : uniform in $[-6.4, 6.4]$

priors for remaining parameters: as in Easter et al. (2020)

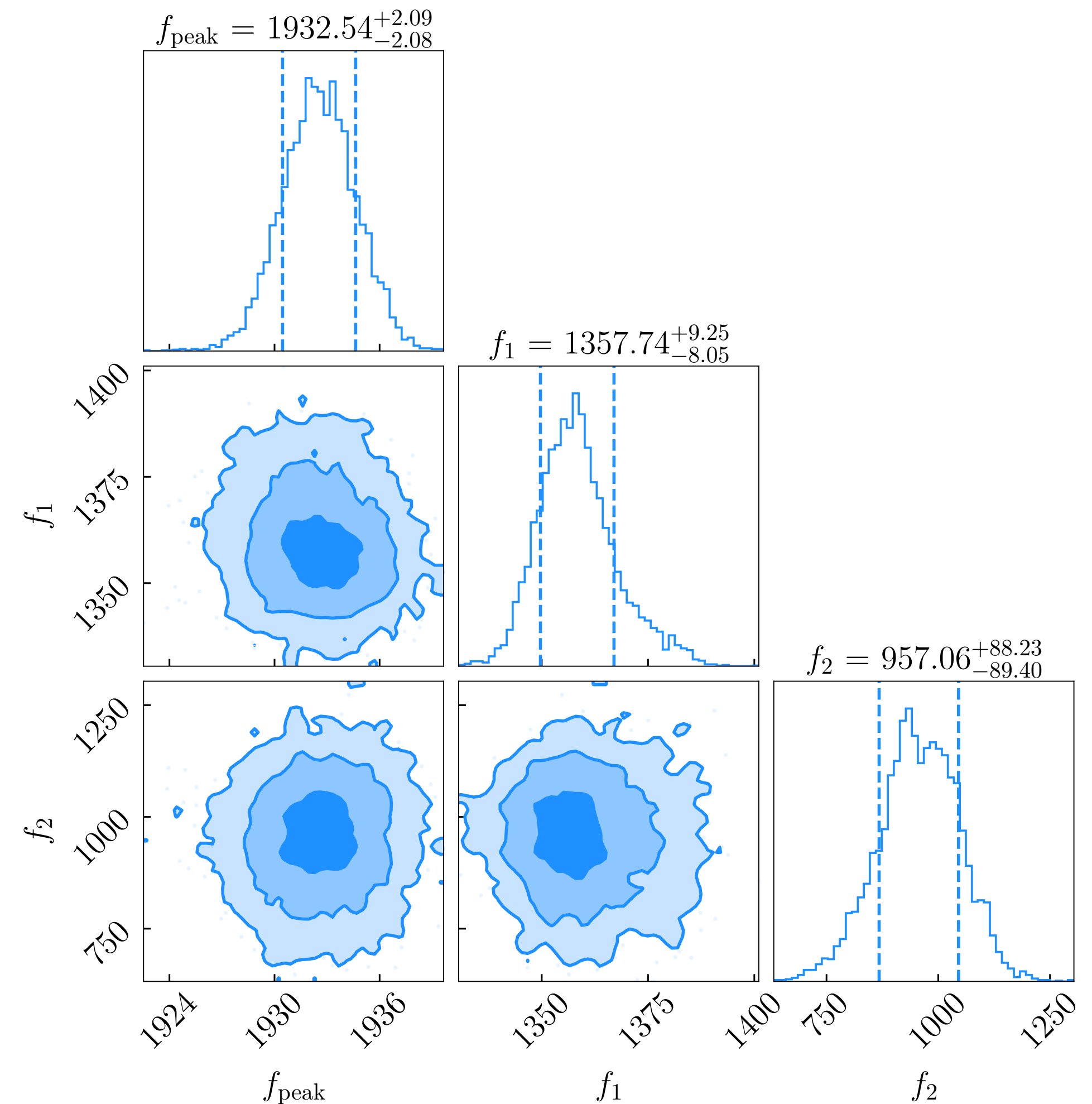
POSTERIOR DISTRIBUTIONS

EOS 2H 1.35+1.35, SNR = 50

using flat priors



using informed priors (through empirical relations)

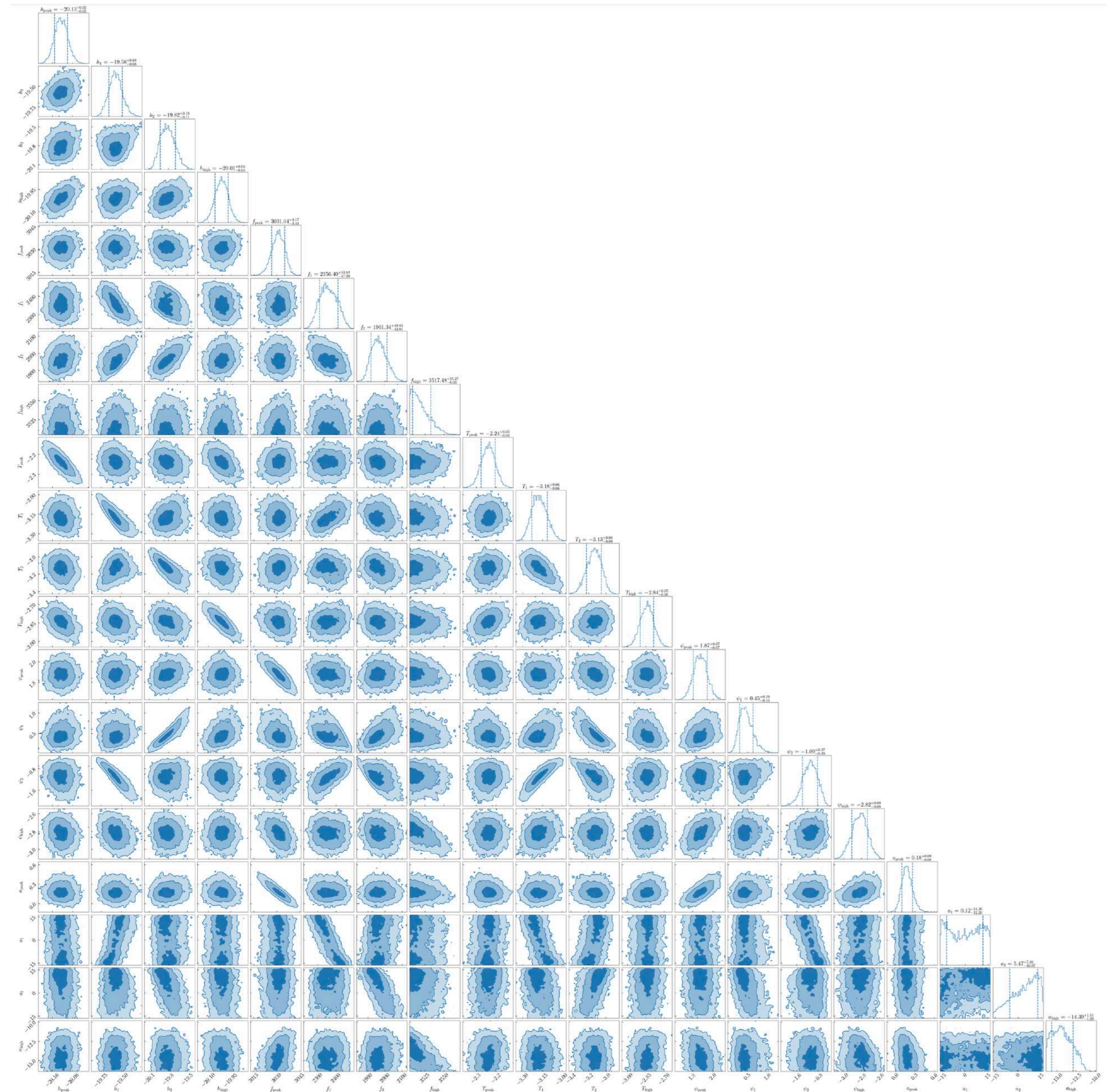


POSTERIOR DISTRIBUTIONS

EOS MPA 1.55+1.55, SNR = 50

using informed priors

all parameters



POCOMC: PRECONDITIONED MONTE CARLO SAMPLER

Preconditioned Monte Carlo Sampling (Karamanis et al. 2022)

PMC targets an **annealed version of the posterior**, with density given by

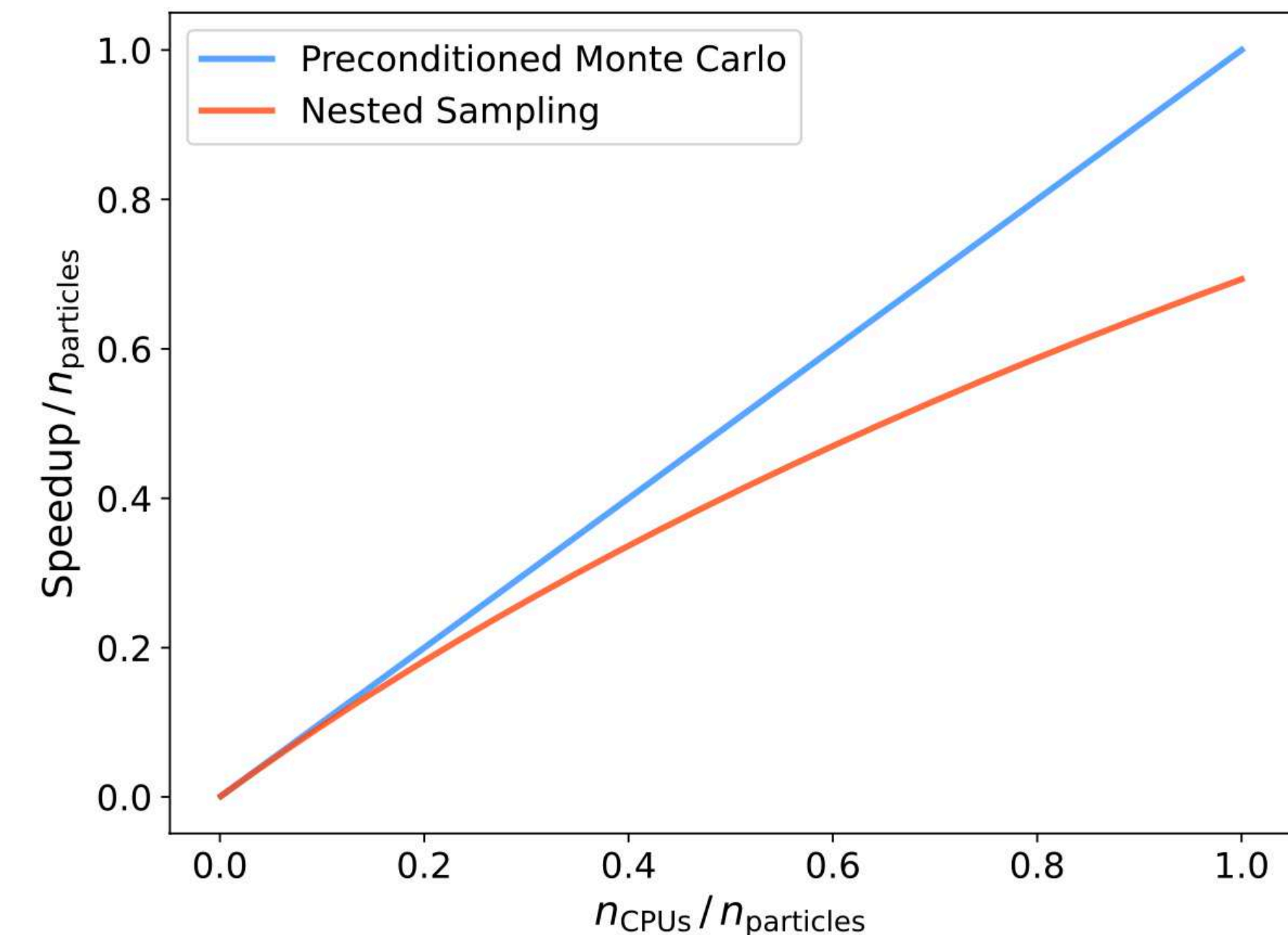
$$p_t(\boldsymbol{\theta} \mid d) \propto \mathcal{L}^{\beta_t}(\boldsymbol{\theta} \mid d)\pi(\boldsymbol{\theta})$$

where β_t a parameter (inverse temperature).

We use 2000 particles that **transition from the prior ($\beta_0 = 0$) to the posterior distribution ($\beta_T = 1$)**, through a sequence of reweighing, resampling and mutation steps.

pocomc

<https://github.com/minaskar/pocomc>



PocoMC is highly parallelizable

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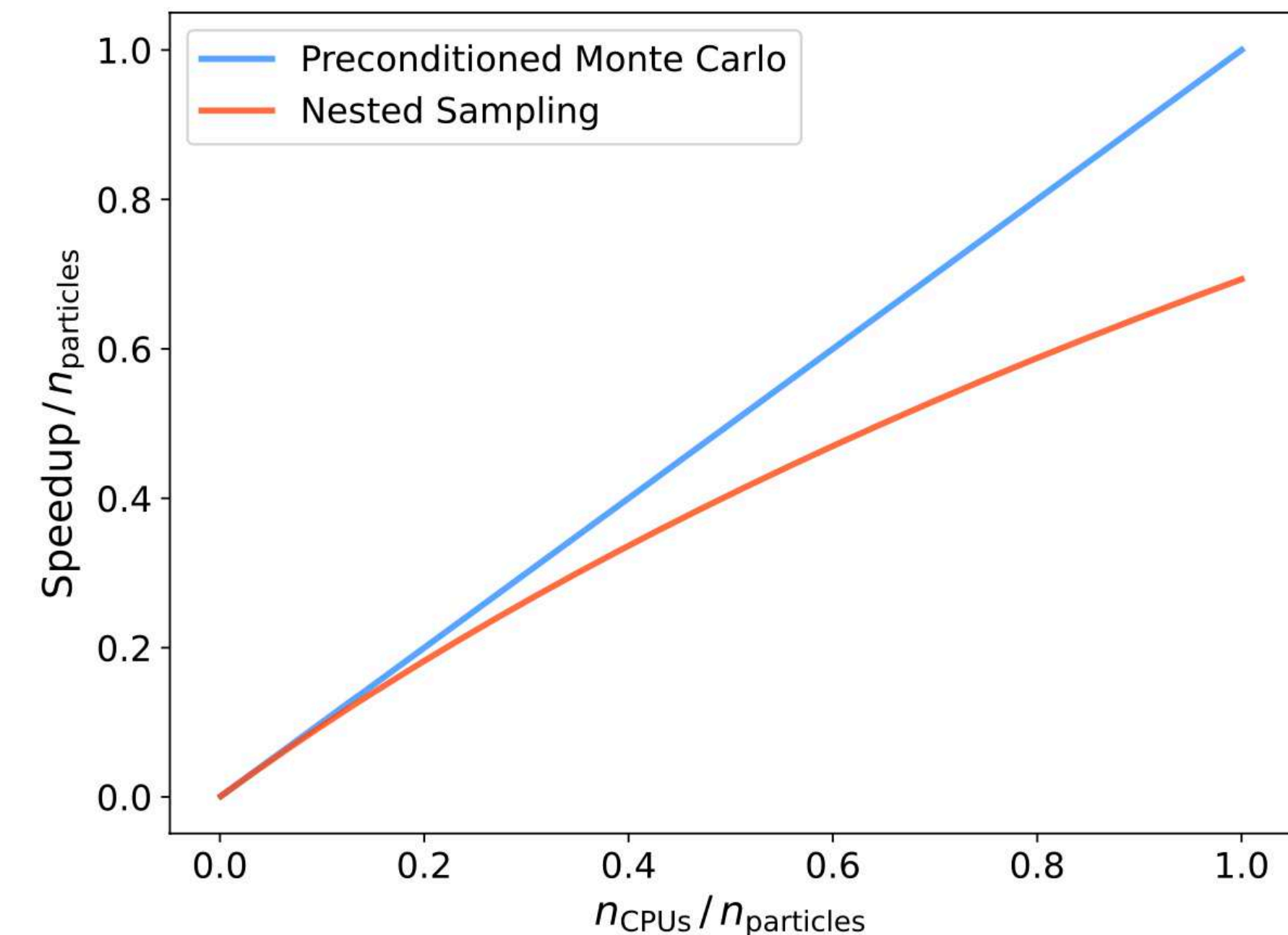
We use 2000 particles that **transition from the prior** ($\beta_0 = 0$) to **the posterior distribution** ($\beta_T = 1$), through a sequence of reweighing, resampling and mutation steps.

After each iteration, a **normalizing flow** transforms the **distribution to a simpler one** (almost Gaussian), decorrelating the parameters. This allows for a much faster sampling.

On same number of CPUs: pocoMC is **~10 times faster** than dynesty.

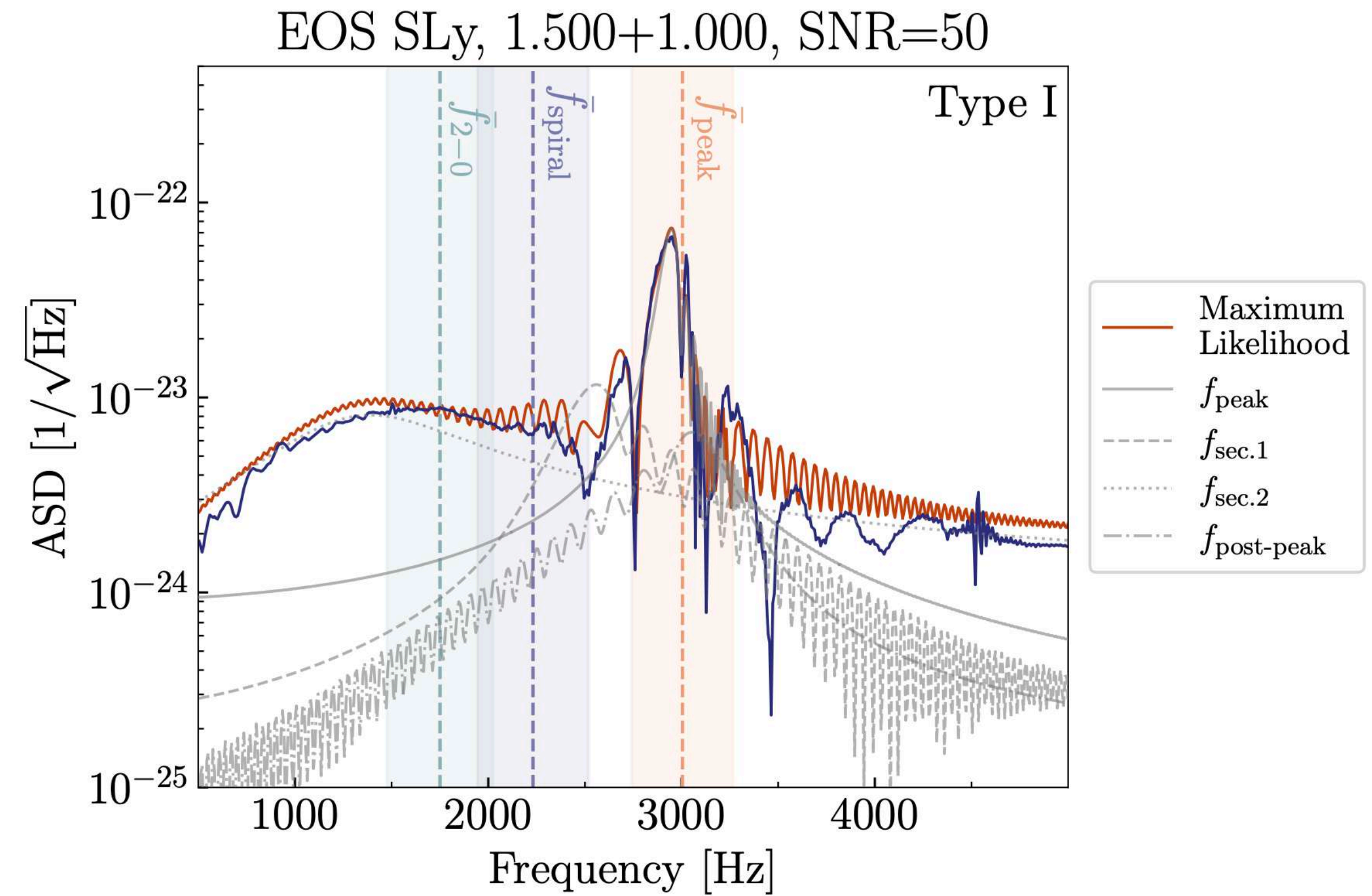
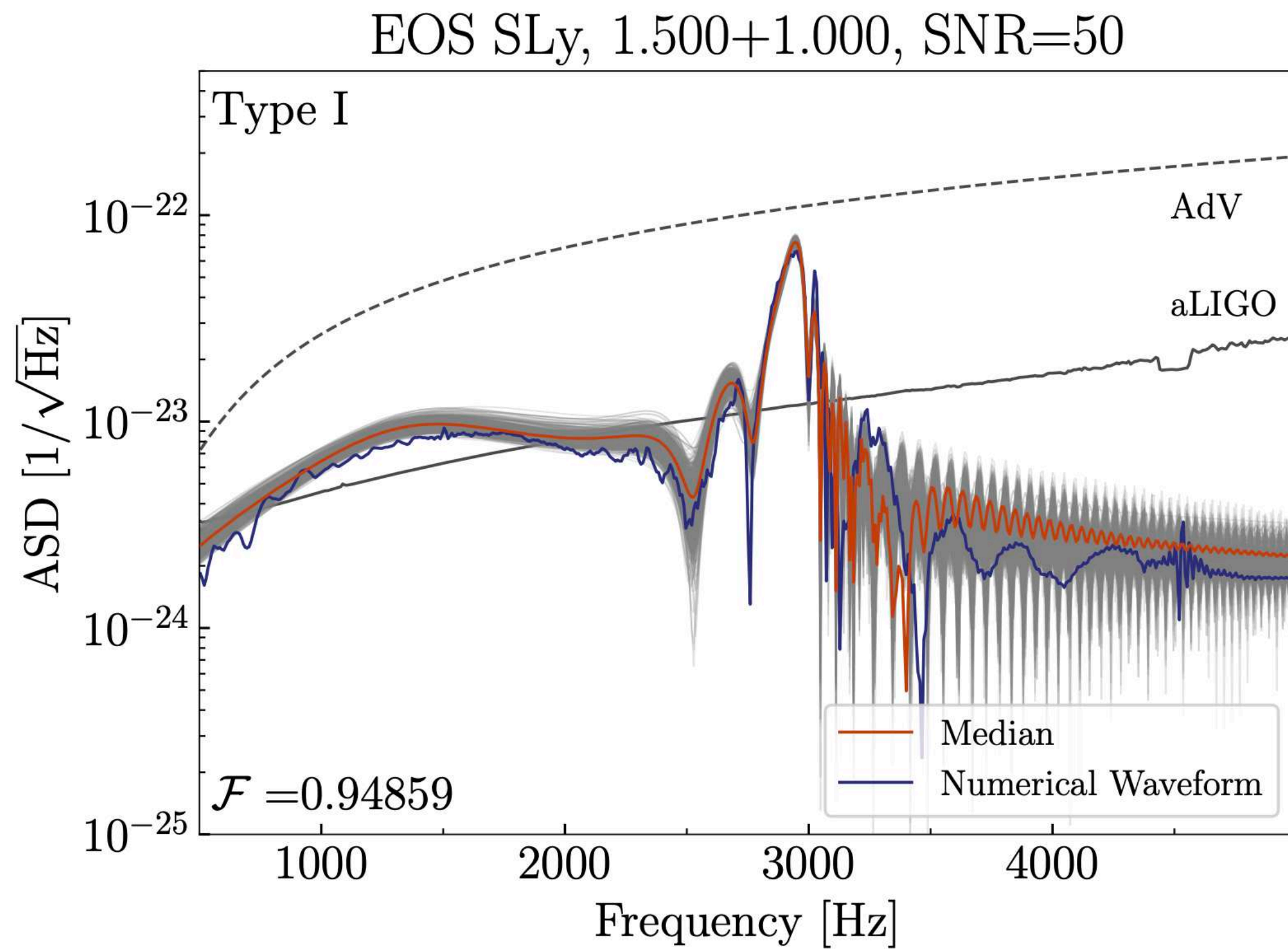
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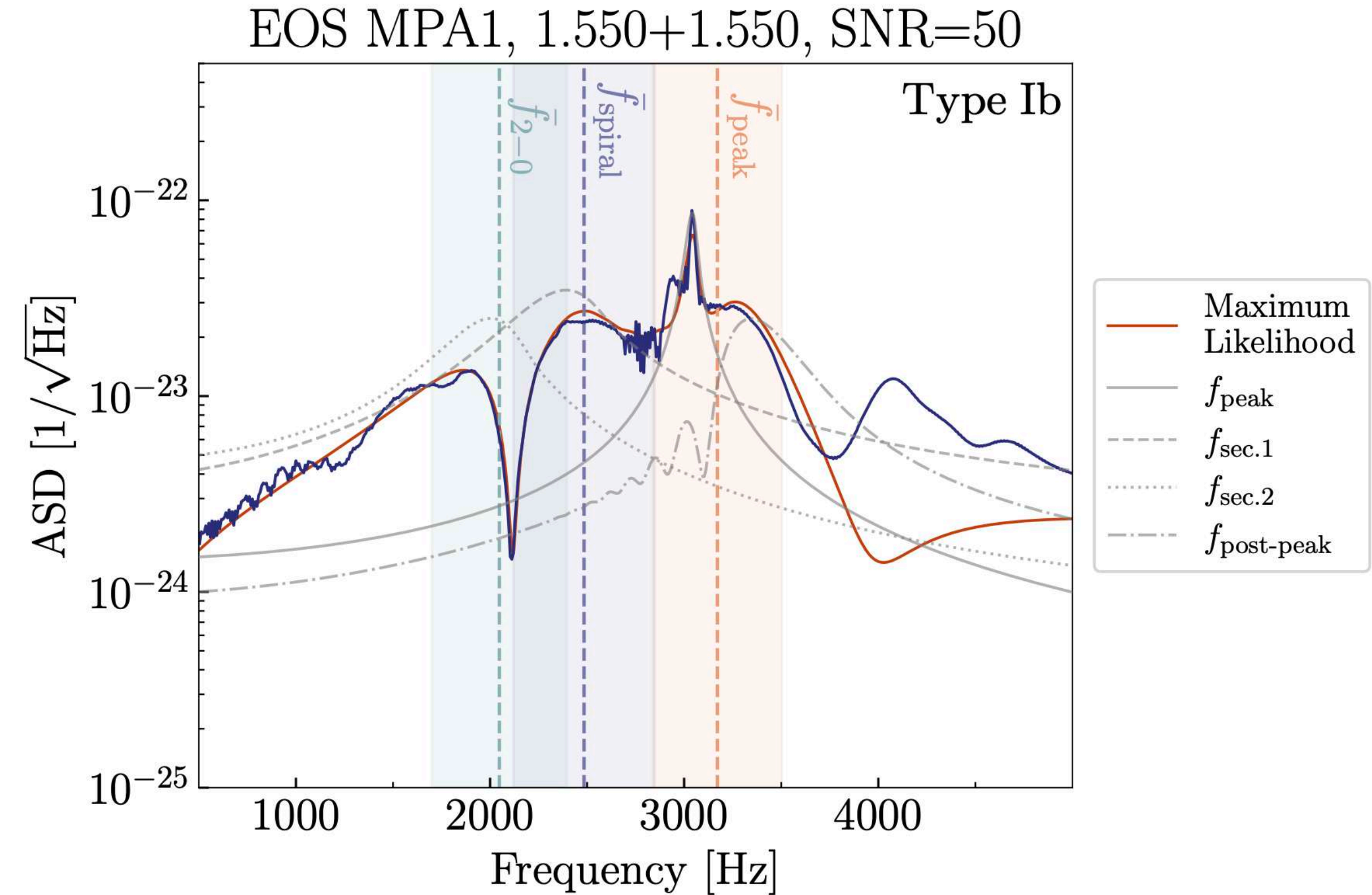
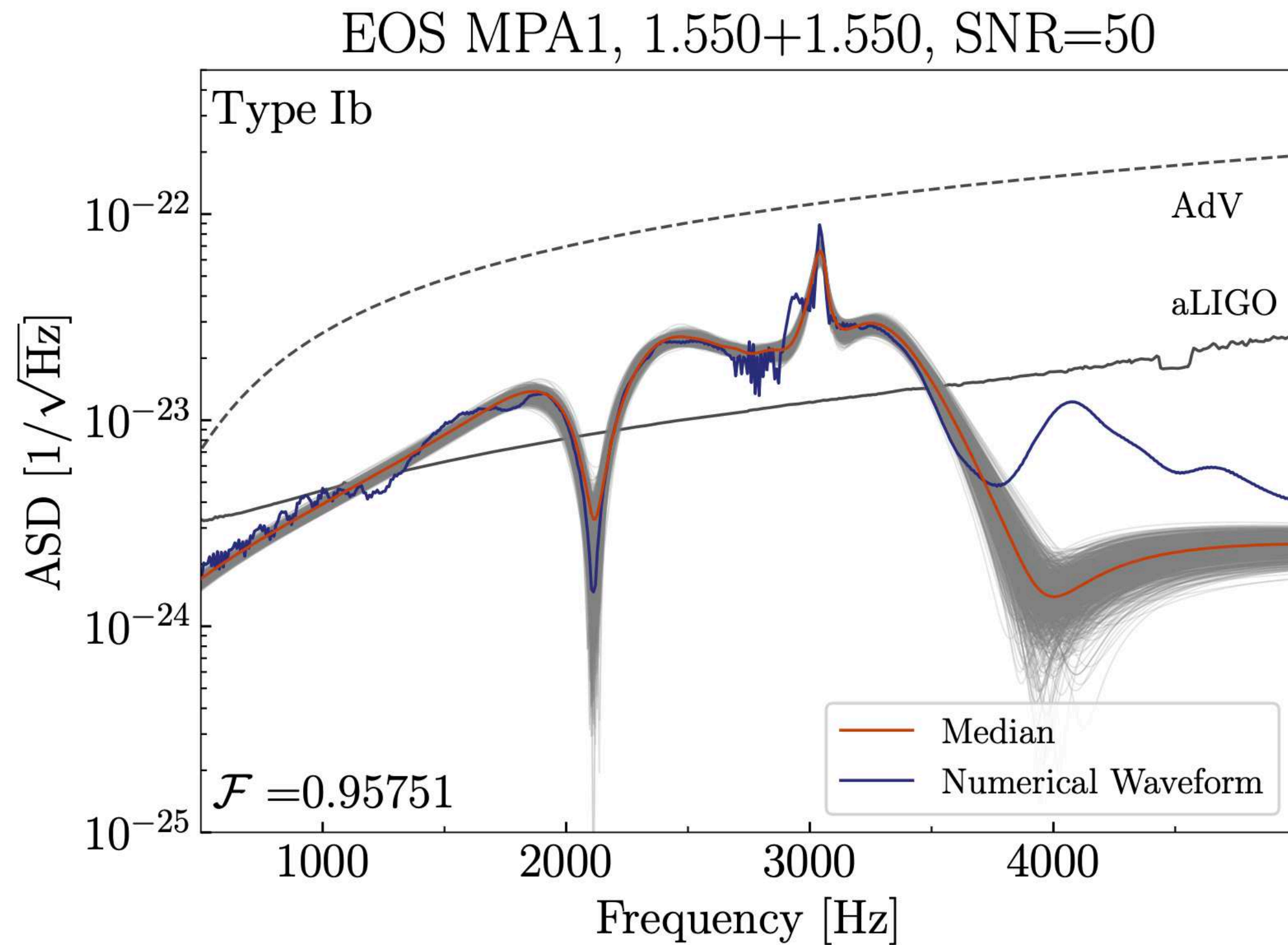


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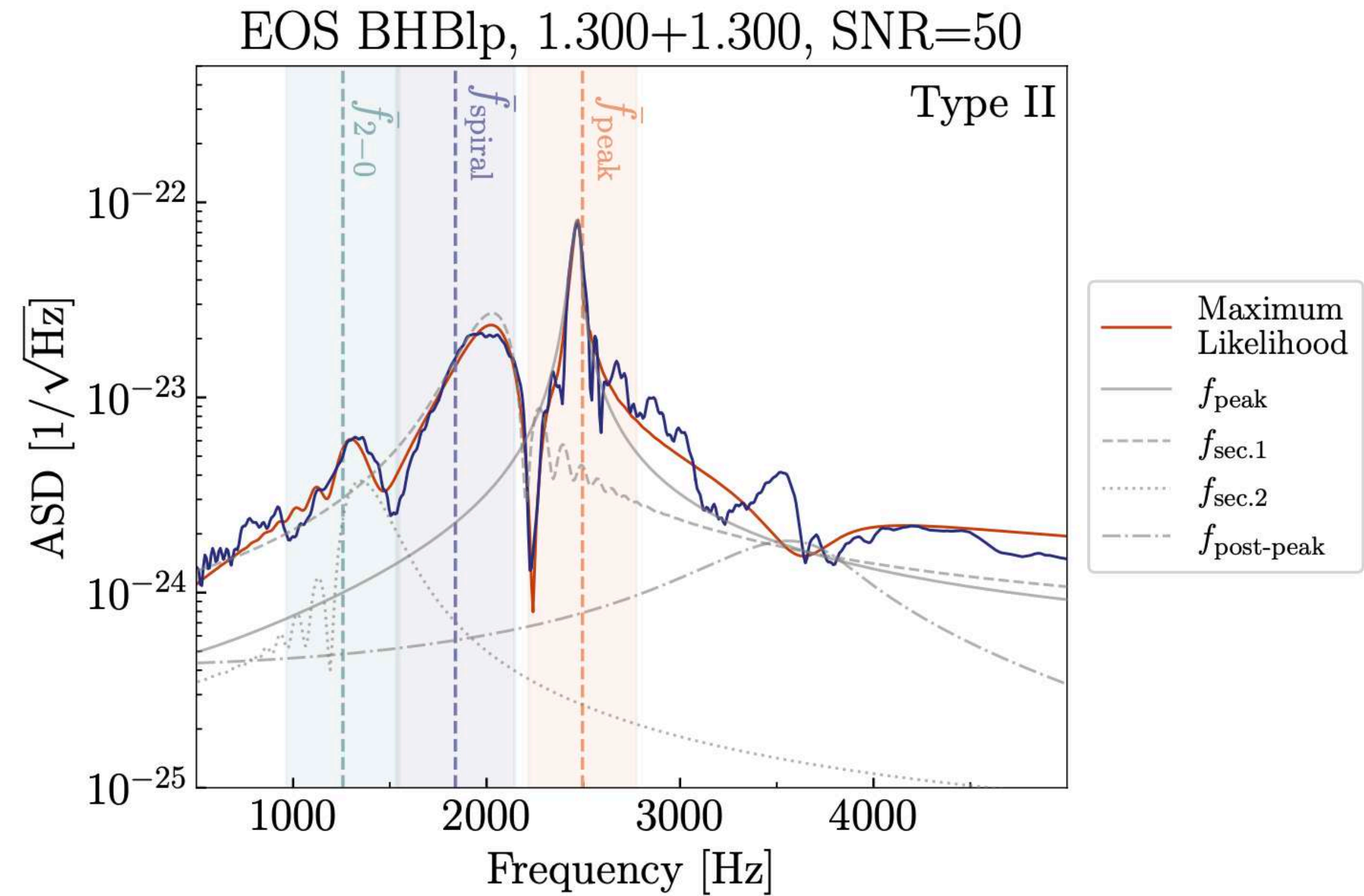
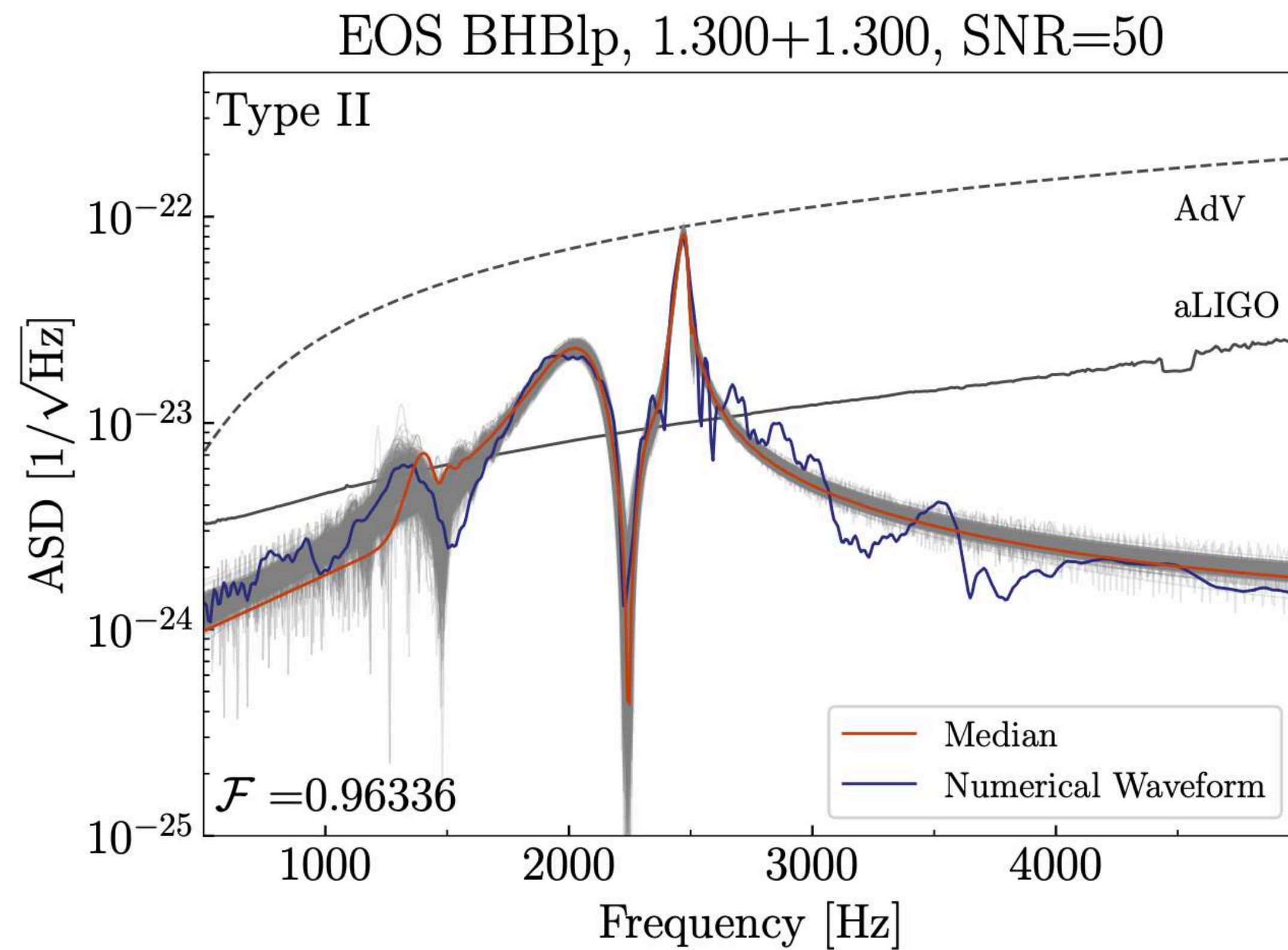
RECONSTRUCTION IN THE FREQUENCY DOMAIN



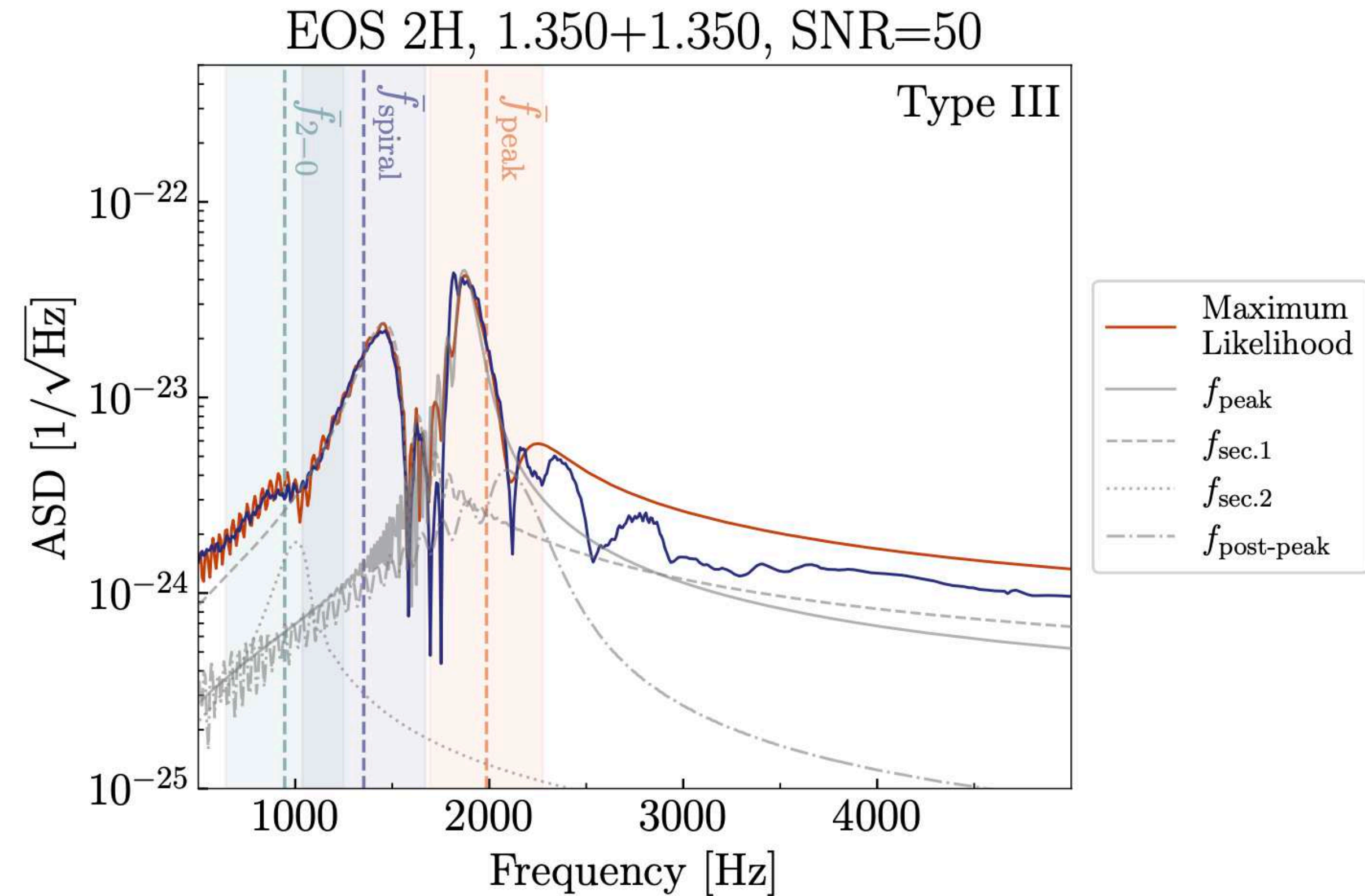
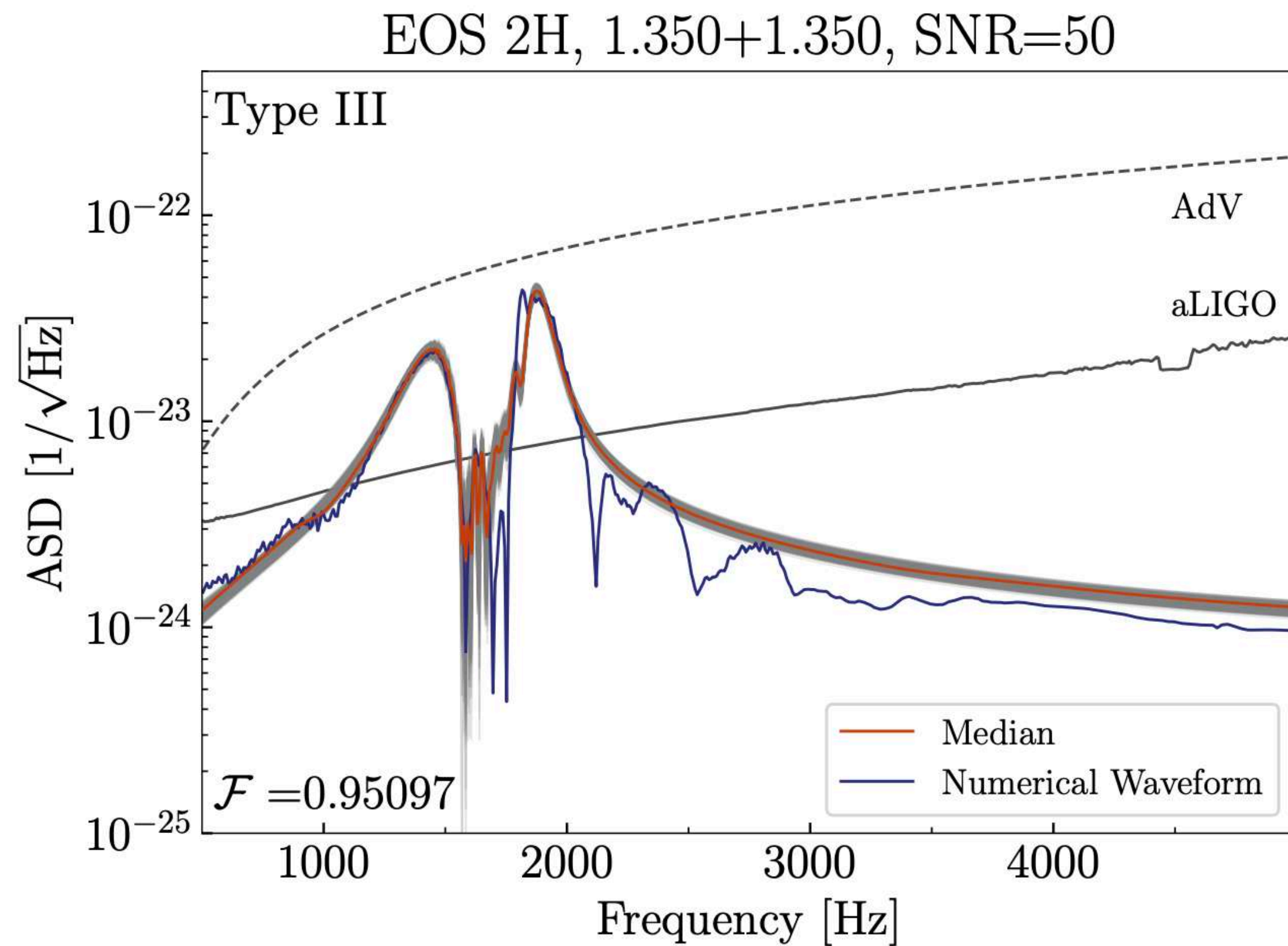
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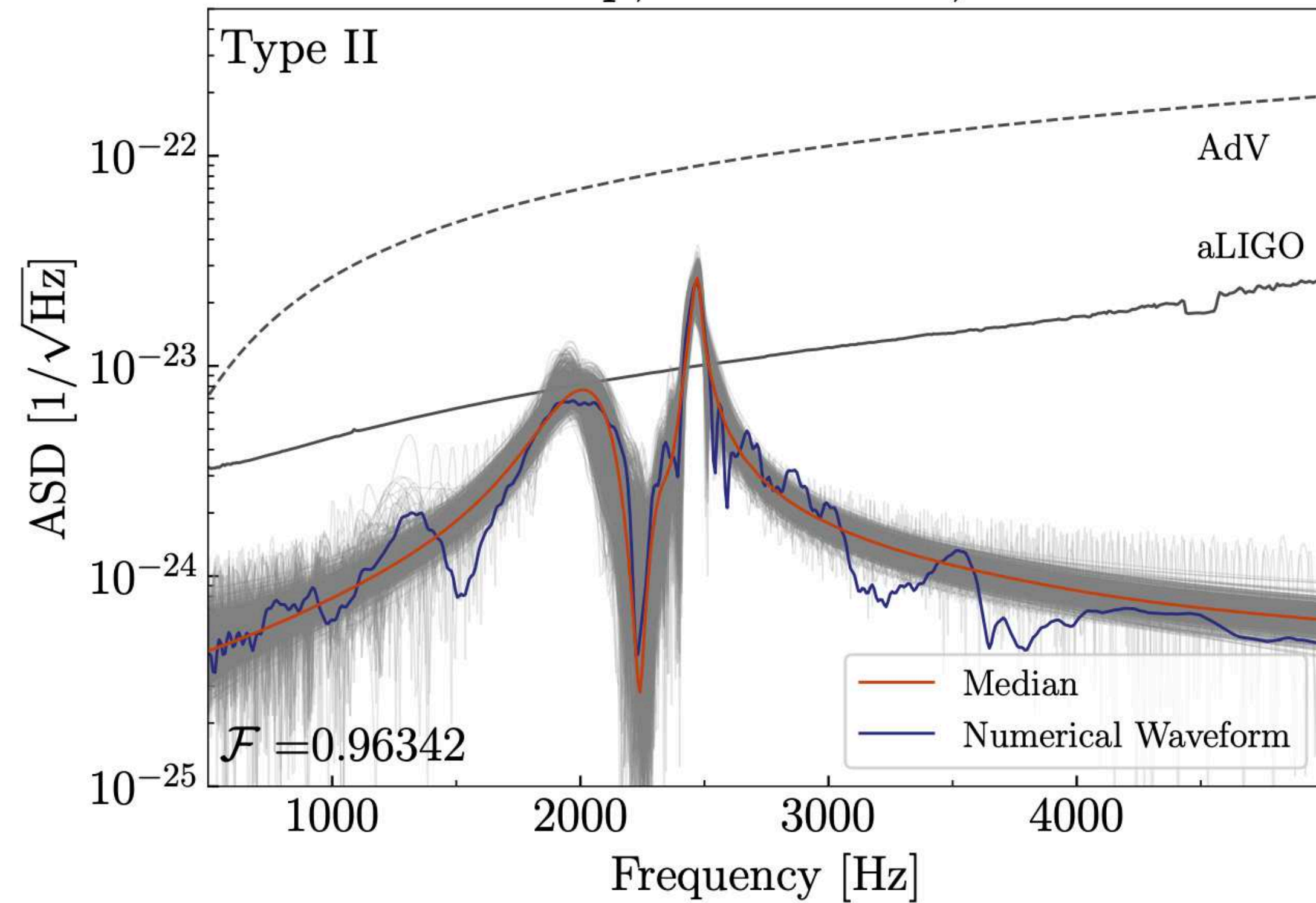


RECONSTRUCTION IN THE FREQUENCY DOMAIN

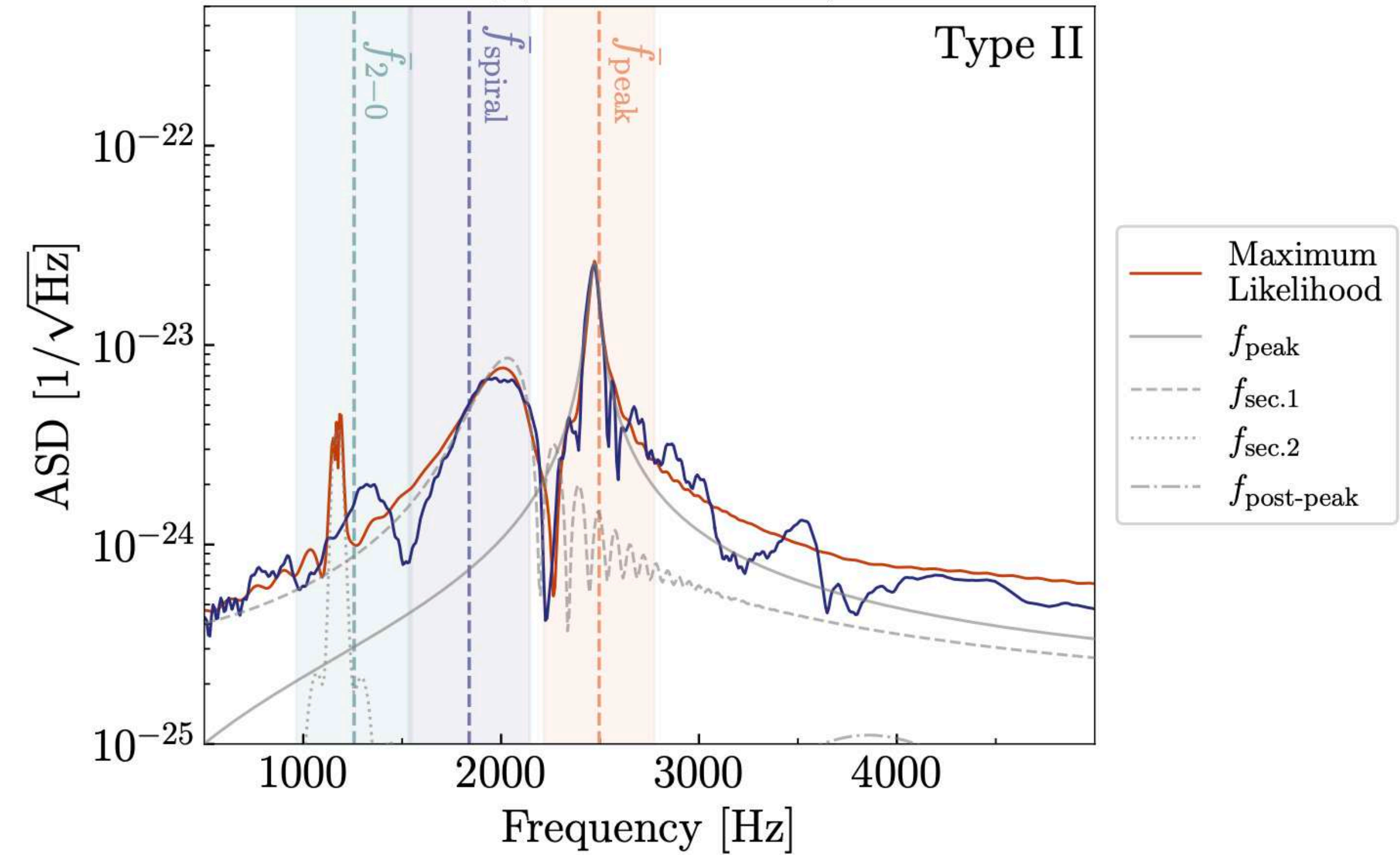


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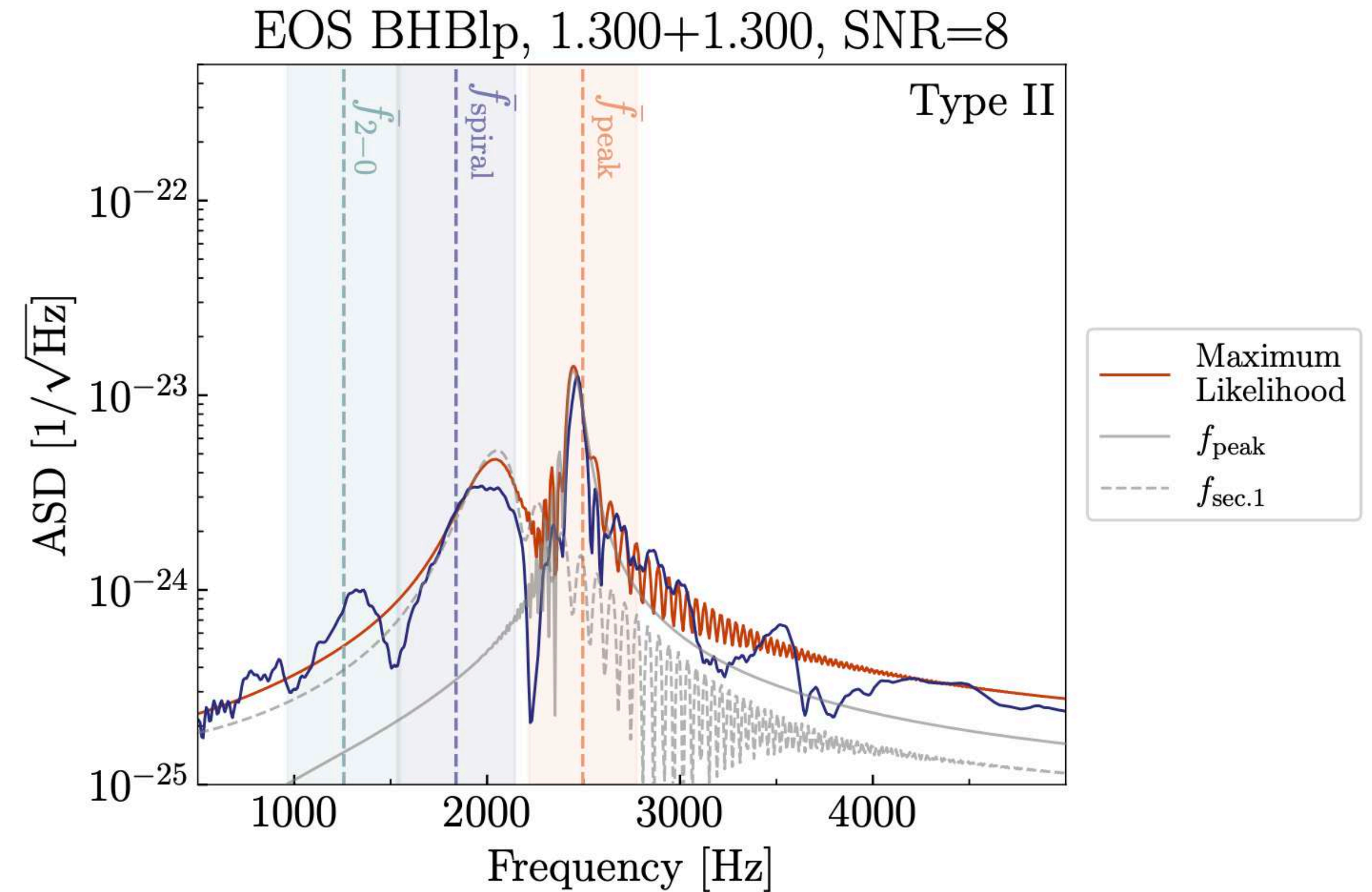
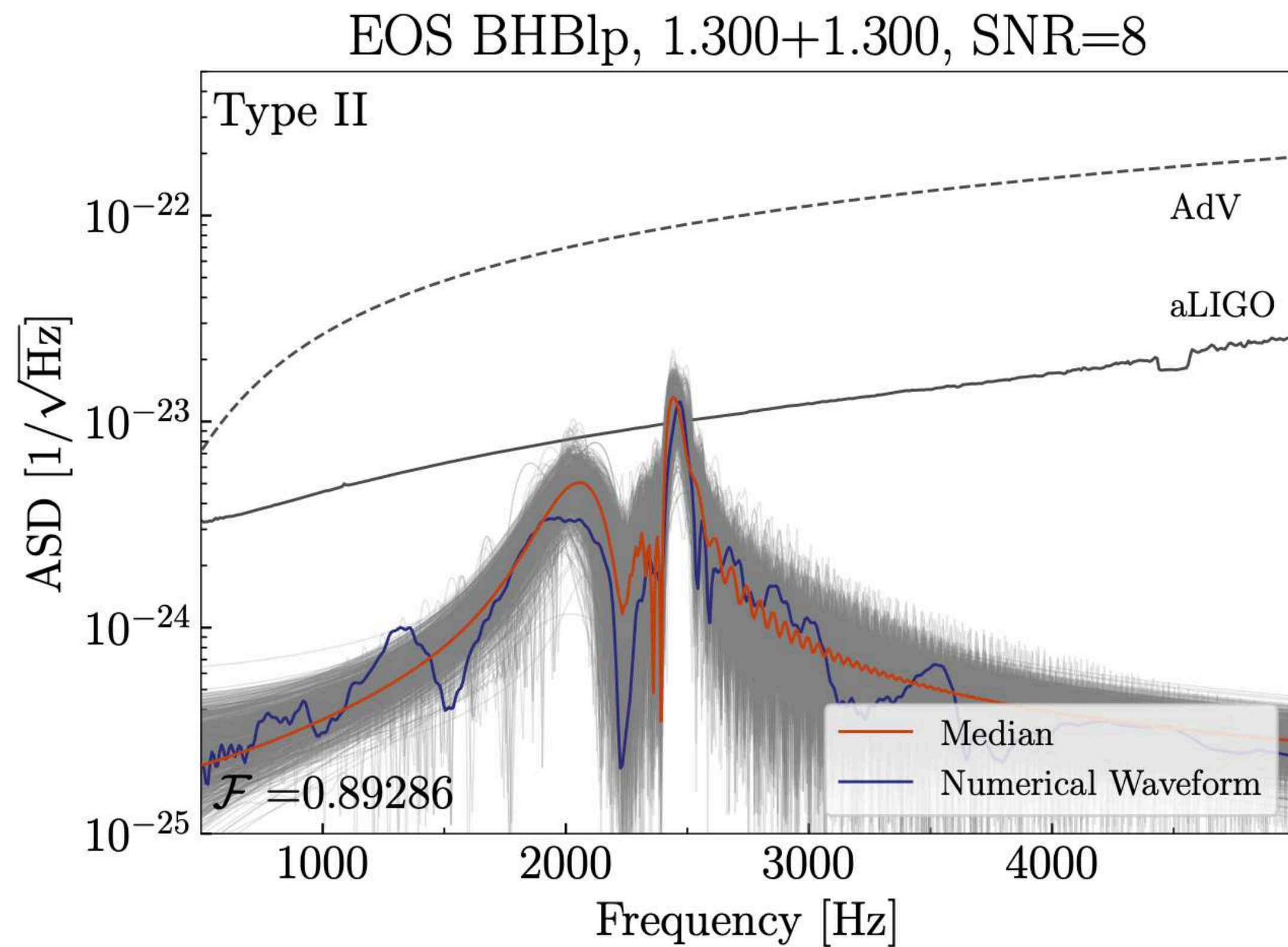
EOS BHBlp, 1.300+1.300, SNR=16



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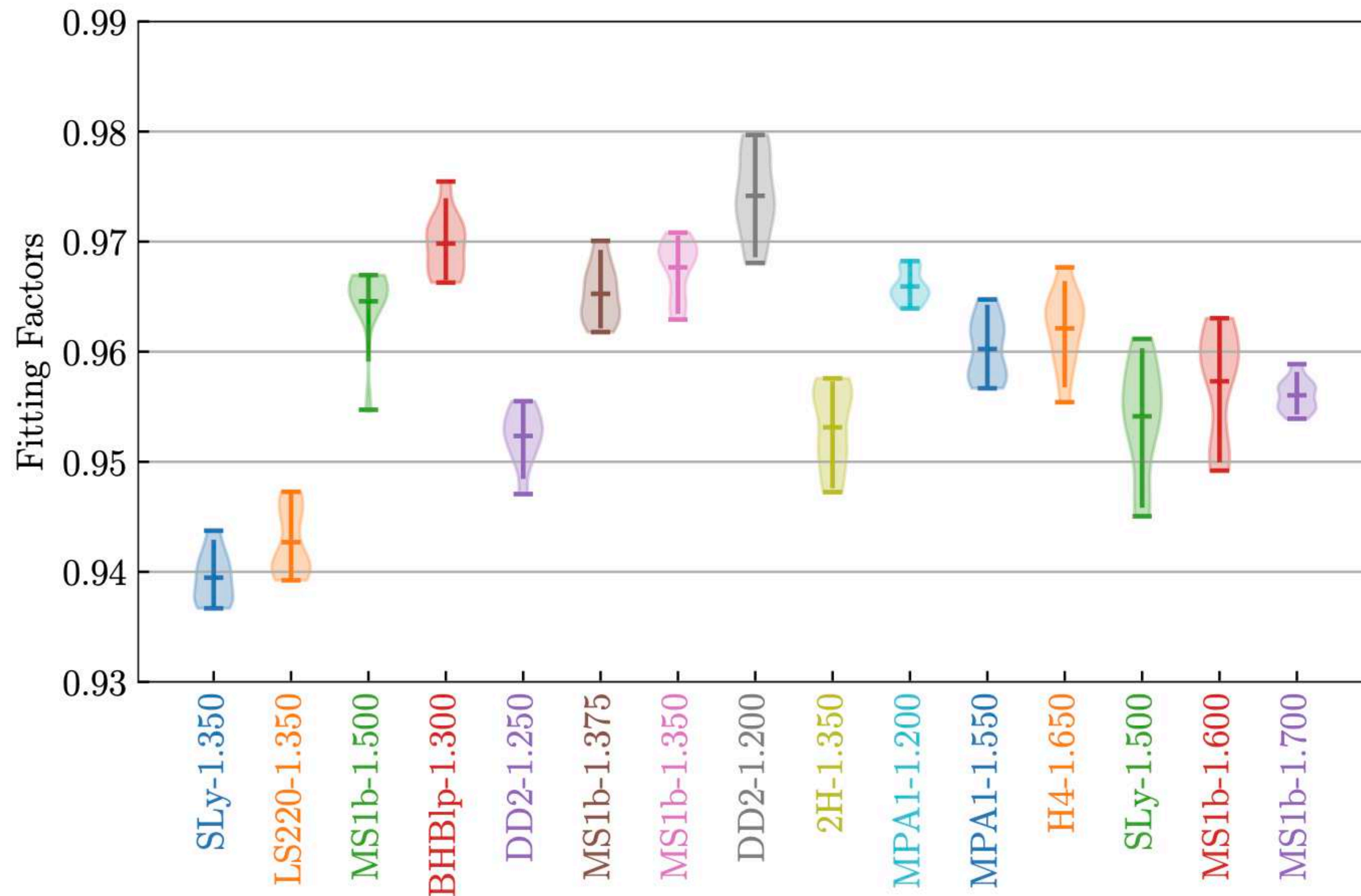


RECONSTRUCTION IN THE FREQUENCY DOMAIN



FITTING FACTORS FOR SNR=50

The fitting factors achieved are consistent with those in Easter et al. (2020) for a smaller set of EOS.

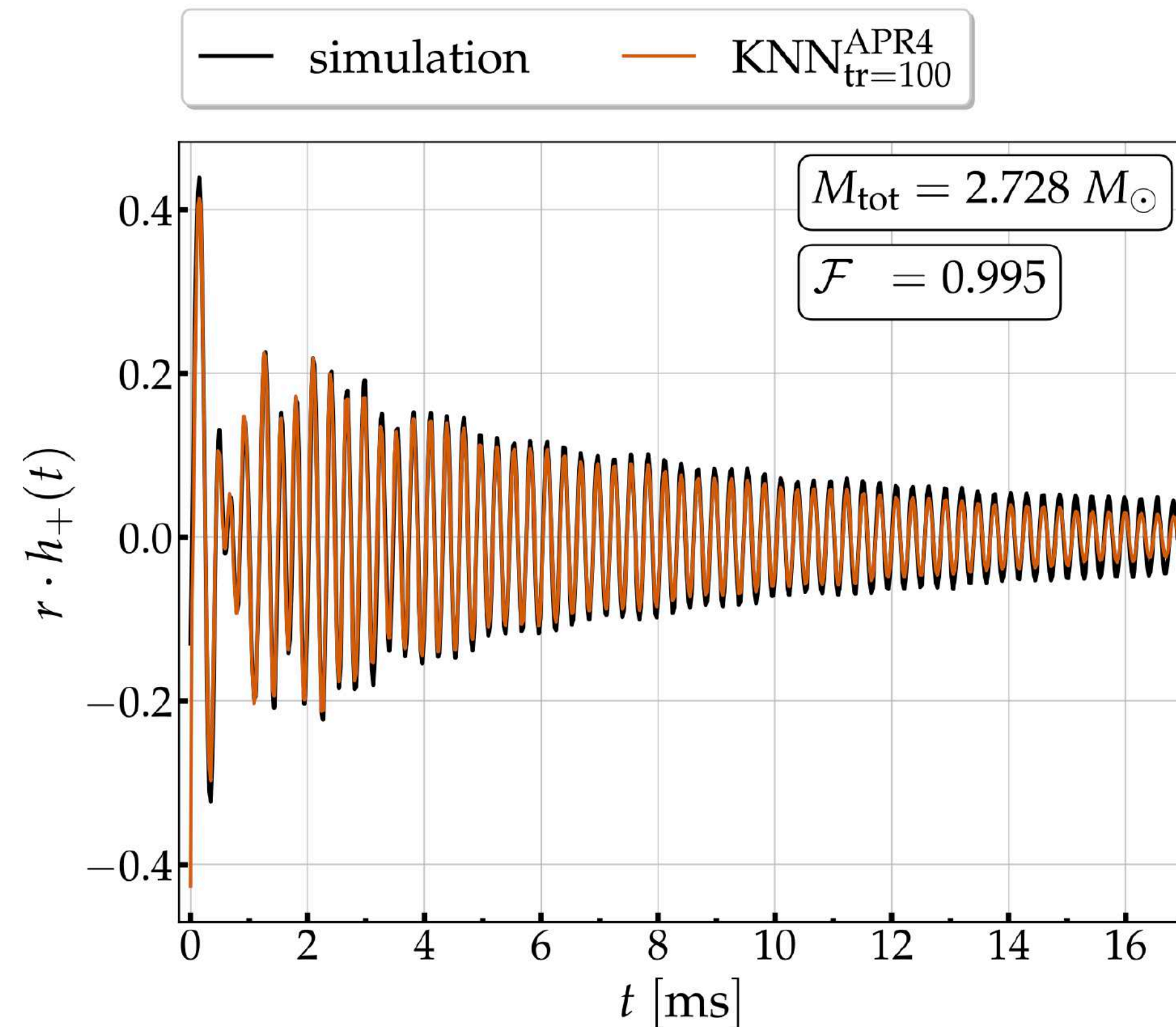


APPLICATION OF MACHINE LEARNING TO THE POST-MERGER PHASE

Problem: Only O(200) substantially different numerical BNS simulations are currently available.

Solution: Construct surrogate model of post-merger GWs as function of e.g. M , q , $\text{EOS}(\Lambda)$

Time domain surrogate model using
K-Nearest Neighbor (KNN) regression:

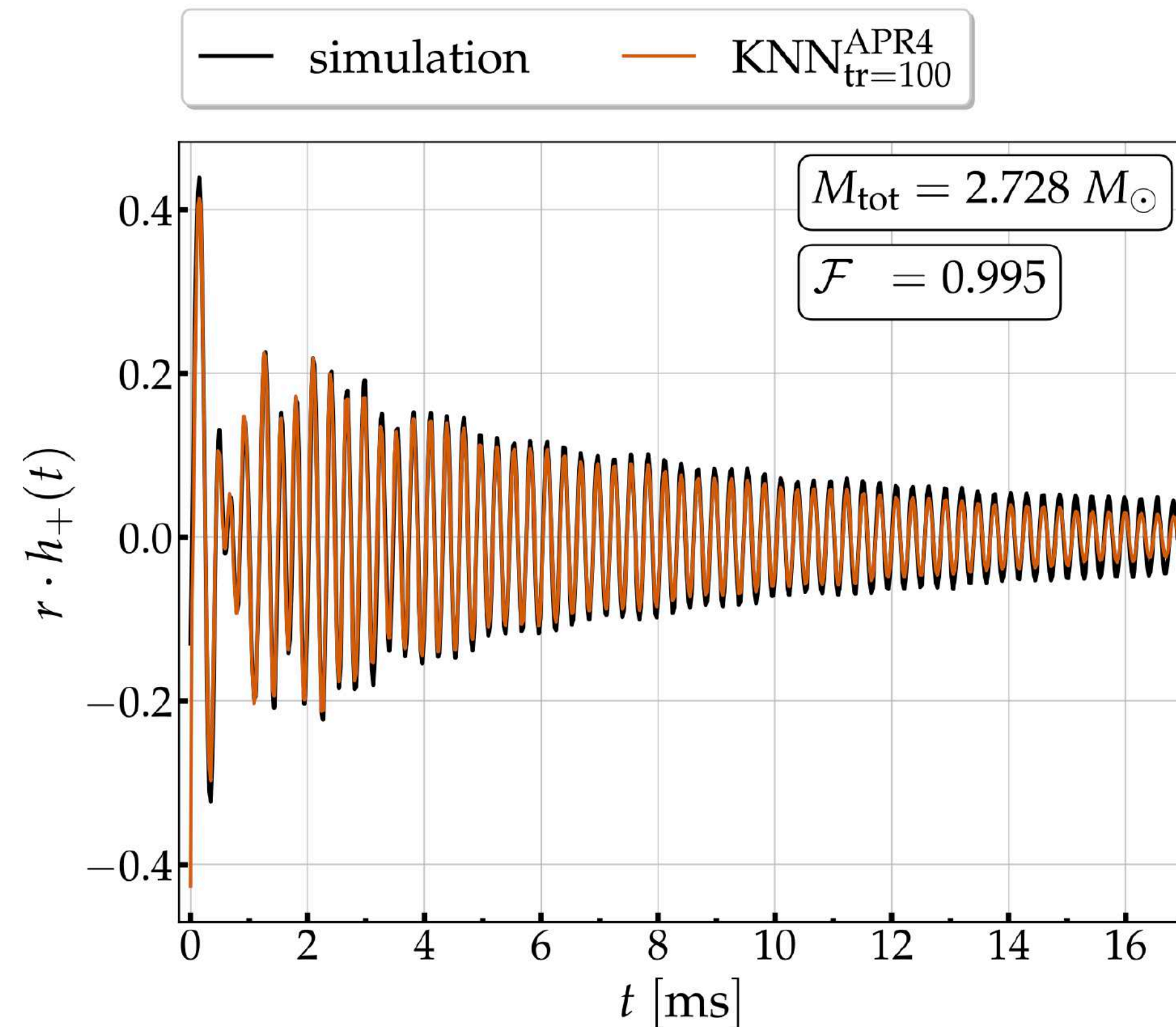


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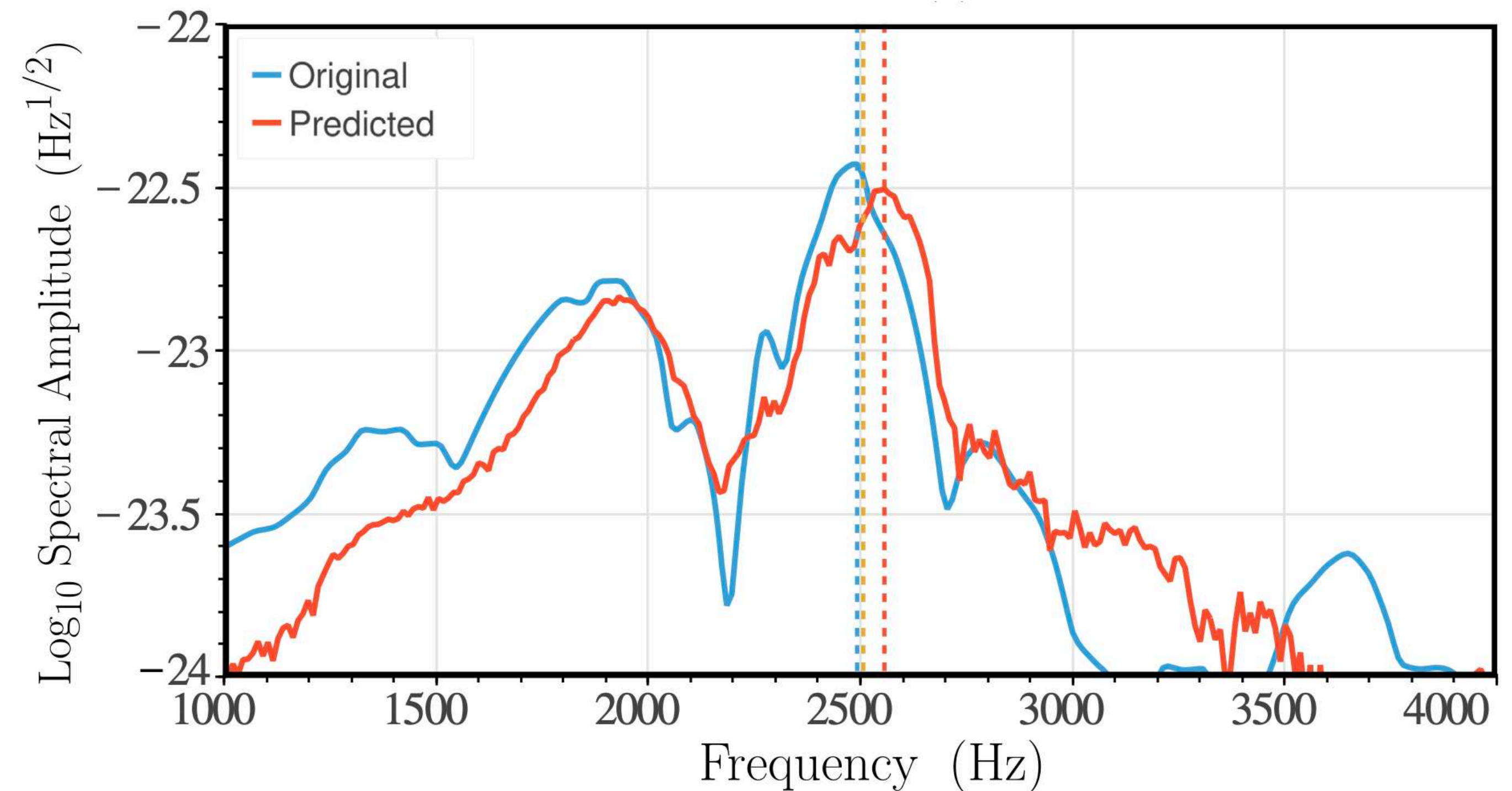
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Time domain surrogate model using
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Soultanis et al. (2025)

Frequency domain surrogate model using
Artificial Neural Networks (ANN) regression:



Pesios et al. (2024)

K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

Training set: 20-100 different M_{tot}
($q=1$) between 2.4 and 2.8 M_{sun} .

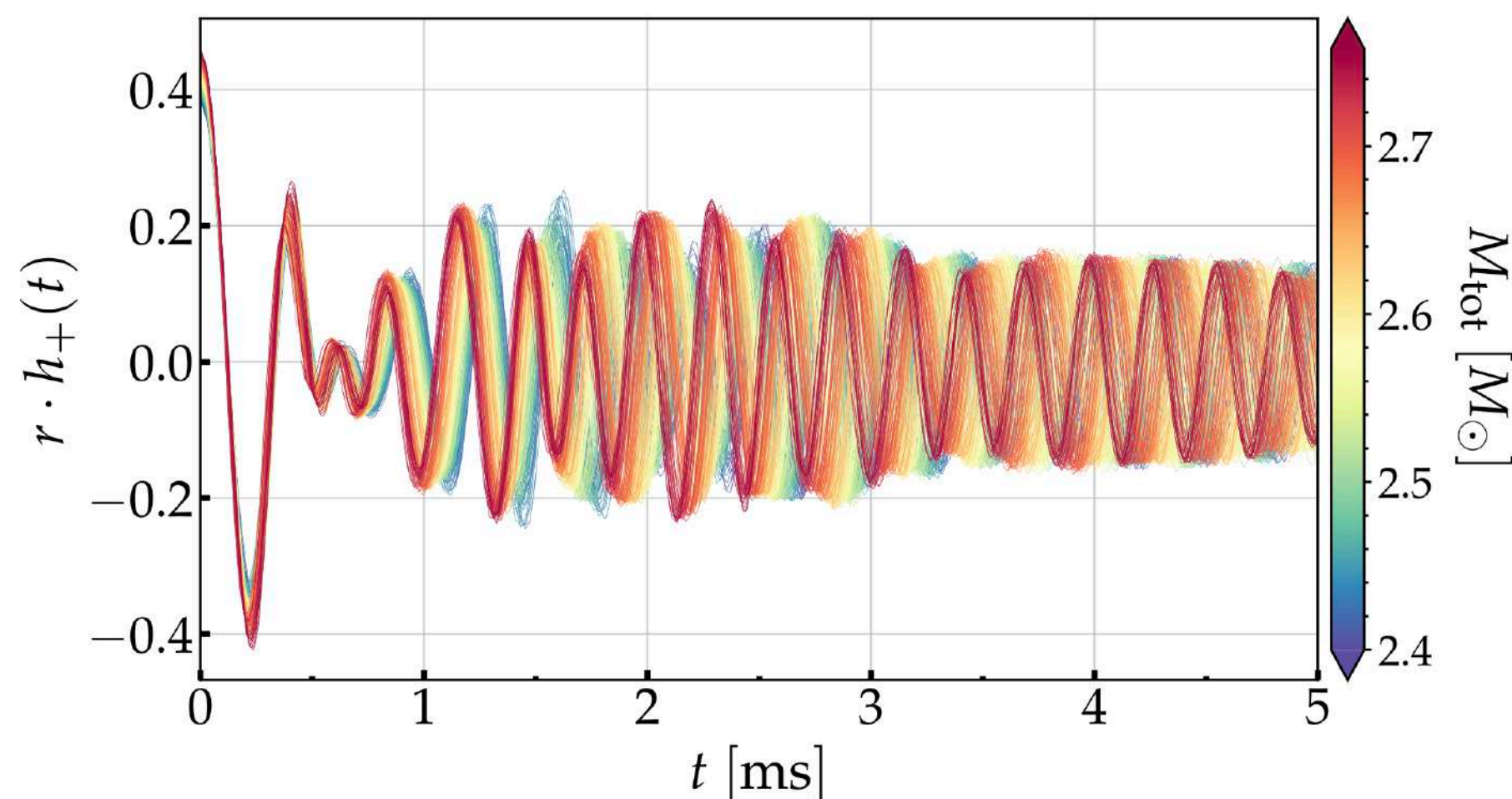
Choose specific EOS (APR4; SFHX).

Complex GW strain:

$$h(t) = h_+(t) + ih_\times(t)$$

$$= |h(t)| \cdot e^{+i\phi(t)},$$

Signals are aligned at merger time:



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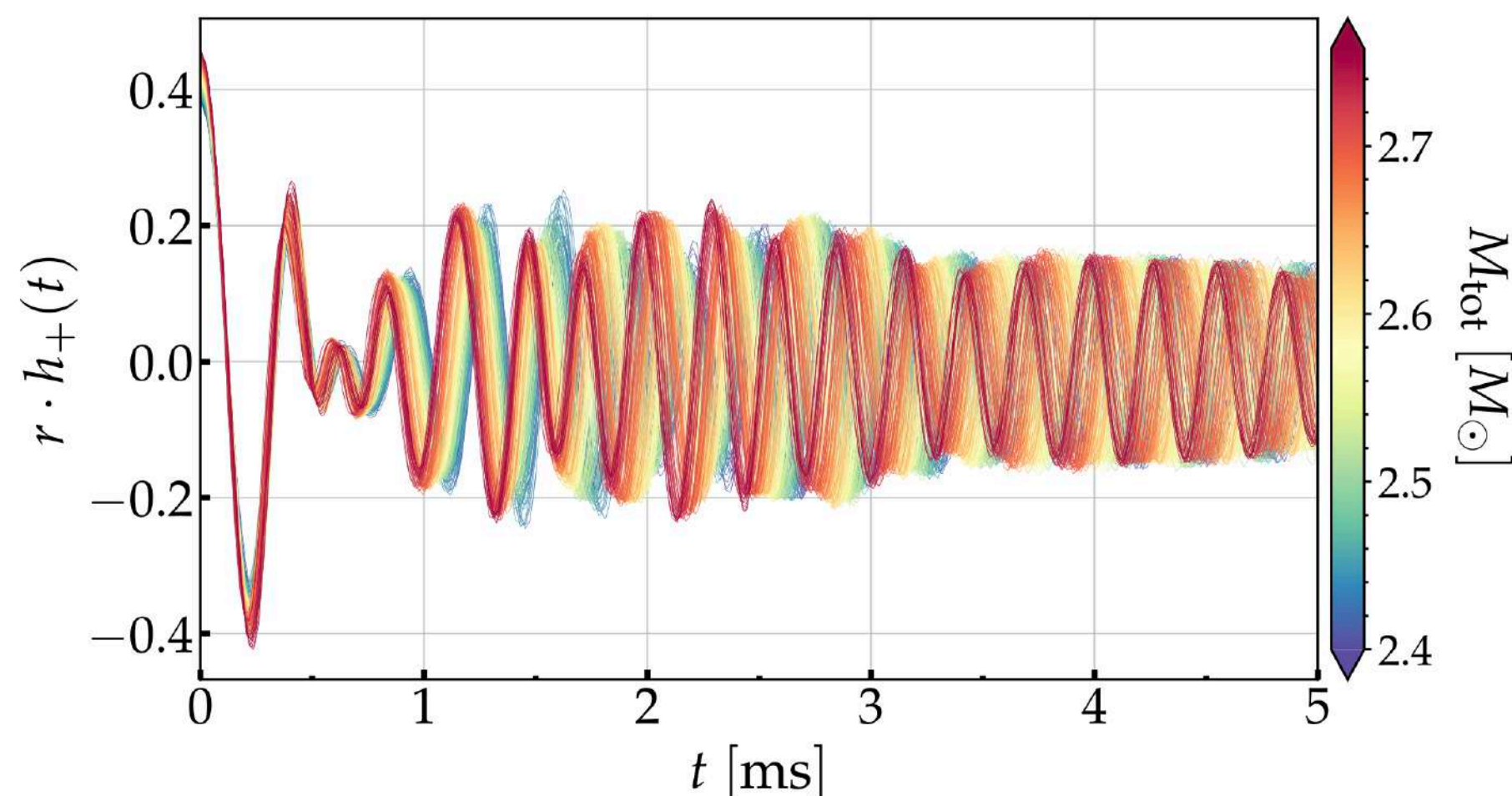
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Signals are aligned at merger time:



Input features: $\vec{X}_i = \{M_{\text{tot}}, t_j\}$

Predictions: $\vec{Y}_i = \text{strain data}$

KNN algorithm: For given input $\vec{X}_0$, find set N_0 of K nearest neighbors

The prediction is a weighted average

$$\vec{Y}_0 = \frac{1}{K} \sum_{\vec{X}_i \in \mathcal{N}_0} \frac{w_i \cdot \vec{Y}_i}{W}, \quad \text{where } W = \sum_{\vec{X}_i \in \mathcal{N}_0} w_i$$

and $w_i = 1/d_i$ where d_i is the distance between $\vec{X}_0$ and $\vec{X}_i$.

Hyperparameters: K and w_i
(tuned to optimal choices using a validation set)

Noise-weighted inner product for two signals:

$$\langle h_1(t), h_2(t) \rangle \equiv 4 \operatorname{Re} \int_0^\infty df \frac{\tilde{h}_1(f) \cdot \tilde{h}_2^*(f)}{S_h(f)}$$

Overlap:

$$\mathcal{O} \equiv \frac{\langle h_1(t), h_2(t) \rangle}{\sqrt{\langle h_1(t), h_1(t) \rangle \langle h_2(t), h_2(t) \rangle}}$$

Faithfulness (maximized overlap)

$$\mathcal{F} \equiv \max_{\phi_0, t_0} \frac{\langle h_1(t), h_2(t) \rangle}{\sqrt{\langle h_1(t), h_1(t) \rangle \langle h_2(t), h_2(t) \rangle}}$$

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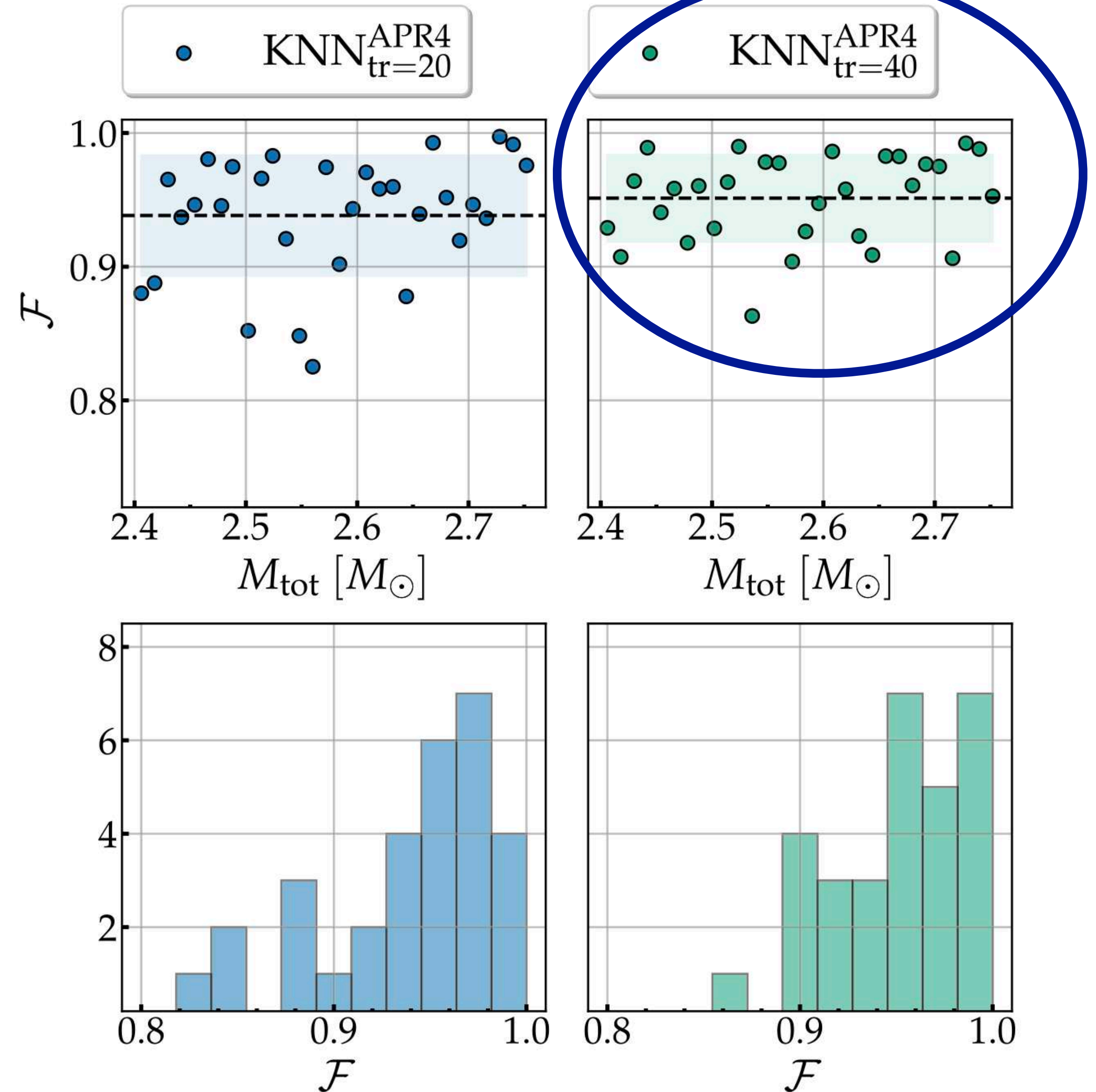
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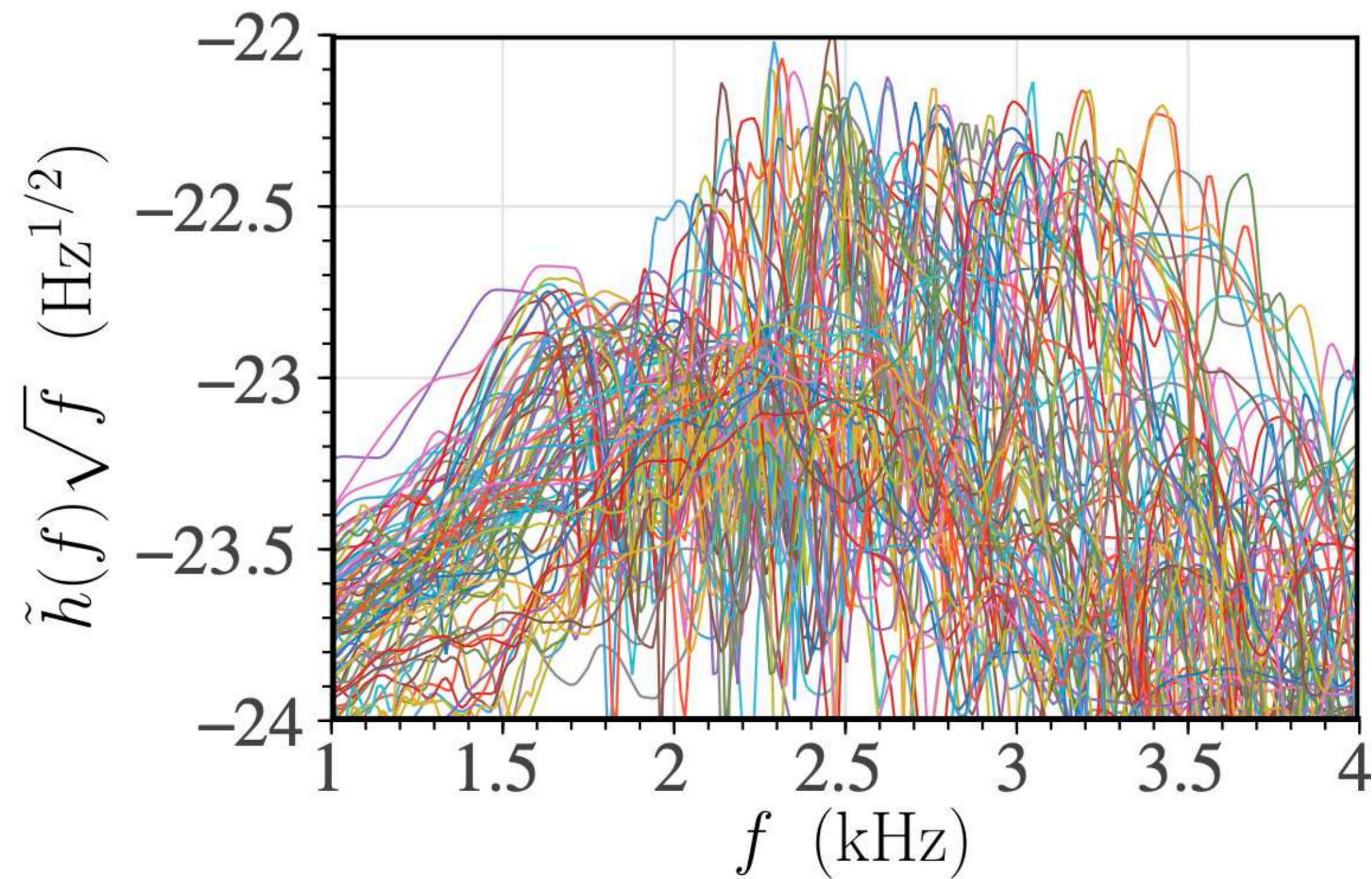
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ANN REGRESSION IN THE FREQUENCY DOMAIN

Expanded training set: 87 equal-mass models using 14 different EOS

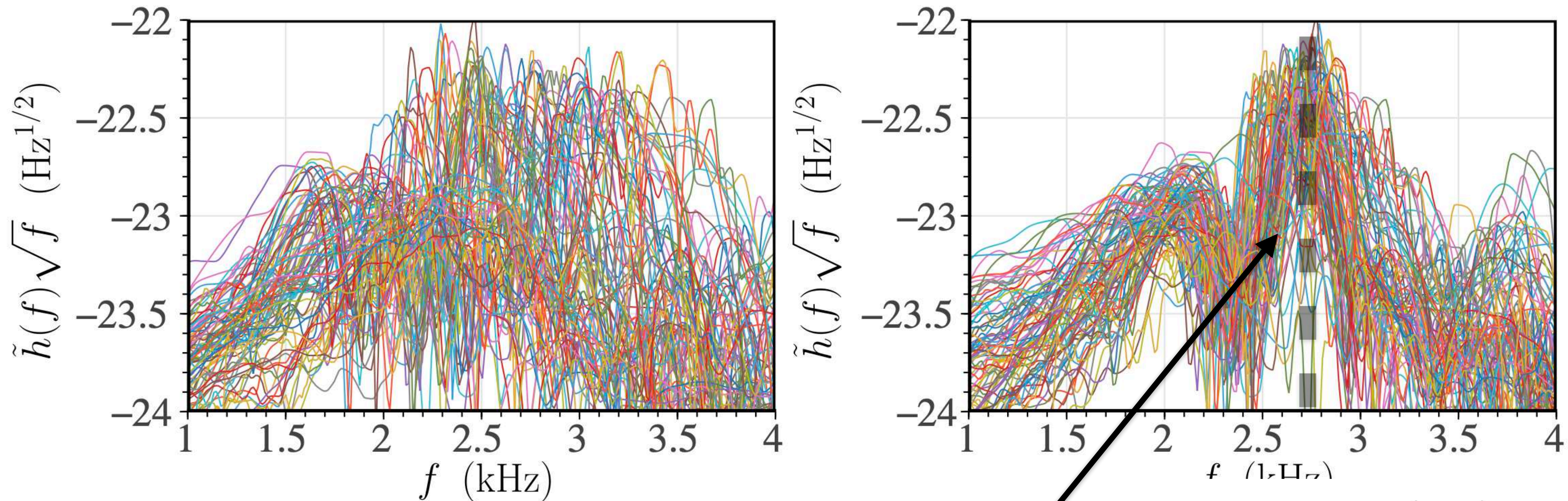
Surrogate model now depends on both mass and tidal deformability.



ANN REGRESSION IN THE FREQUENCY DOMAIN

Expanded training set: 87 equal-mass models using 14 different EOS

Surrogate model now depends on both mass and tidal deformability.



Partial alignment of spectra using empirical relation: $f_{\text{peak}}(\kappa_2^\tau, M) = 4 \frac{\beta_1}{M} \ln \left(\frac{\beta_0}{8\kappa_2^\tau} \right)$

Pesios, Koutalios, Kugiumtzis, Stergioulas (2024)

ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

1) Mass, 2) tidal coupling constant, 3) dR/dM

Prediction:

Magnitude of GW spectrum (1-4 kHz).

ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

1) *Mass*, 2) *tidal coupling constant*, 3) *dR/dM*

Prediction:

Magnitude of GW spectrum (1-4 kHz).

4-layer feed-forward ANN

Added Gaussian noise and dropout layers

Adam optimizer

Layer	Type	Shape	Activation	Params
1	Gaussian noise (0.1)	(None, 3)	...	0
2	Dense	(None, 200)	Linear	800
3	Gaussian noise (0.05)	(None, 200)	...	0
4	Dropout (0.15)	(None, 200)	...	0
5	Dense	(None, 400)	Sigmoid	80400
6	Gaussian noise (0.1)	(None, 400)	...	0
7	Dropout (0.15)	(None, 400)	...	0
8	Dense	(None, 400)	Sigmoid	160400
9	Gaussian noise (0.1)	(None, 400)	...	0
10	Dropout (0.05)	(None, 400)	...	0
11	Dense	(None, 370)	Linear	148370

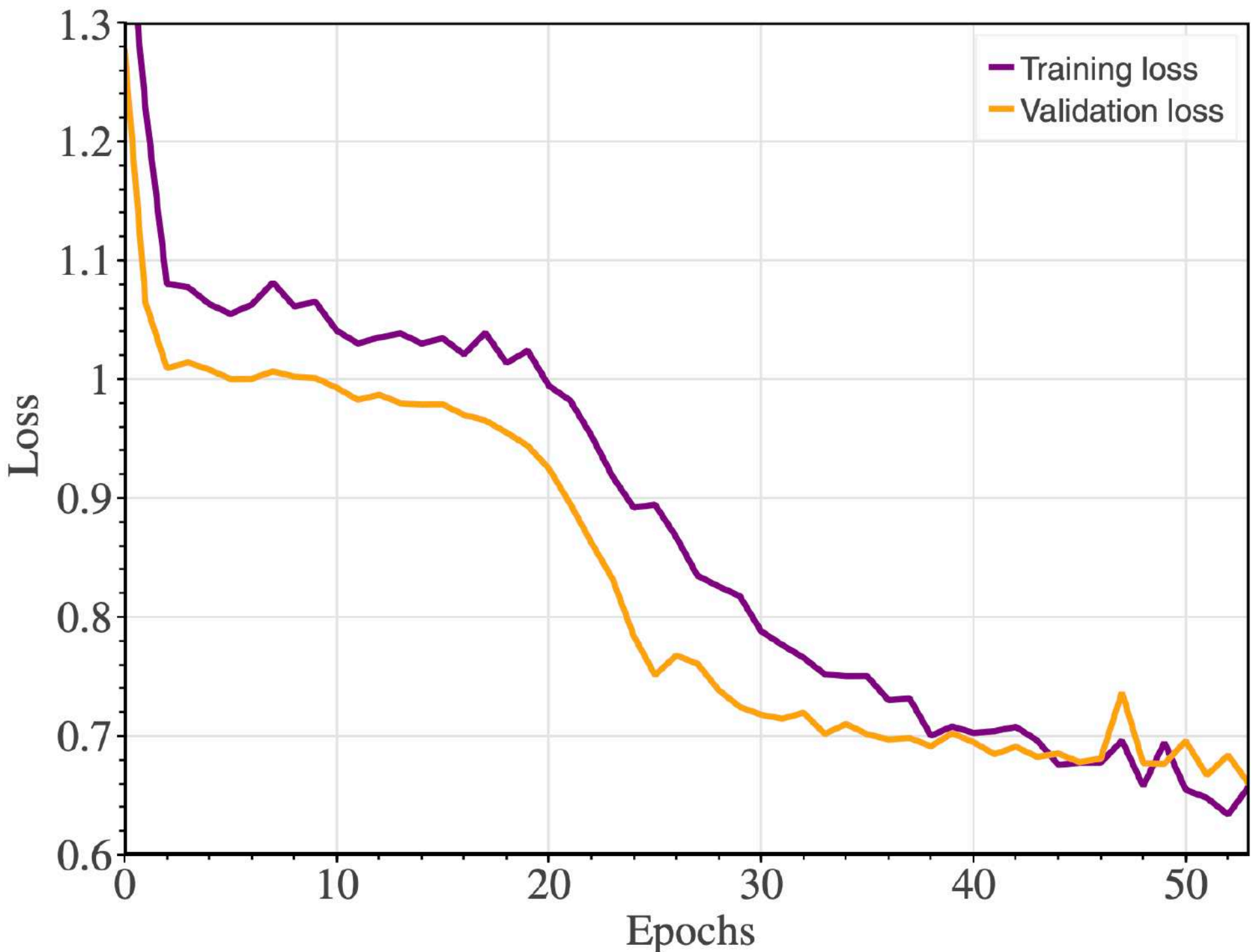
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8	Dense	(None, 400)	Sigmoid	160400
9	Gaussian noise (0.1)	(None, 400)	...	0
10	Dropout (0.05)	(None, 400)	...	0
11	Dense	(None, 370)	Linear	148370

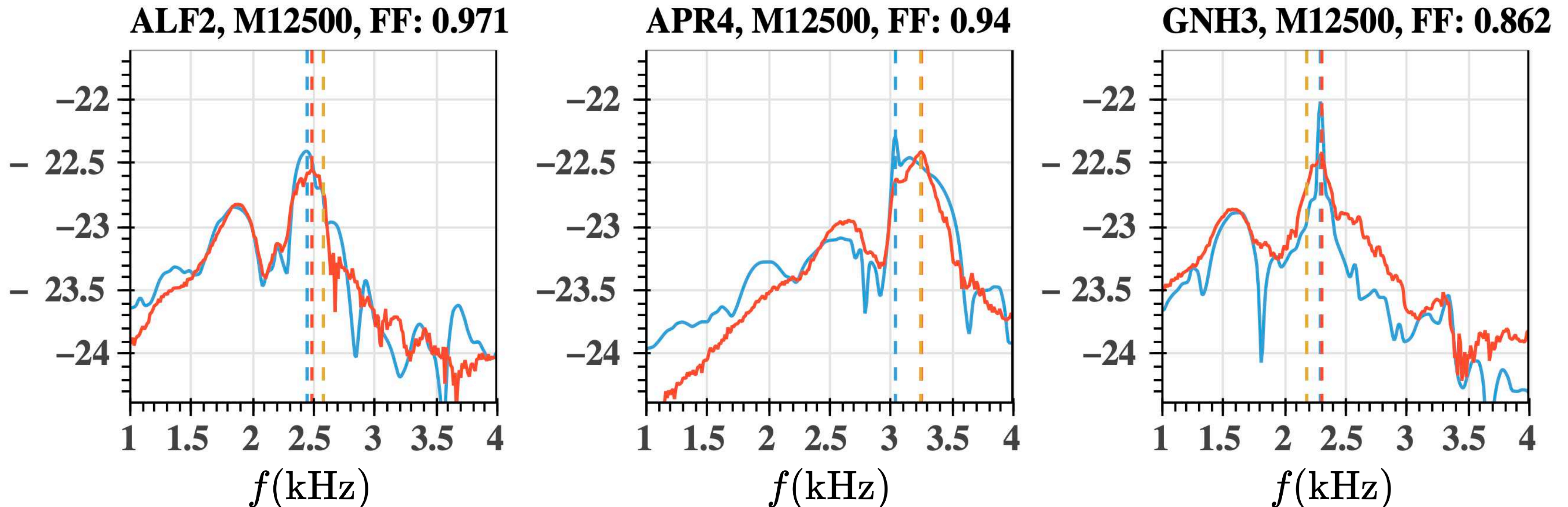
ANN SURROGATE IN THE FREQUENCY DOMAIN

Typical examples of predicted magnitudes of GW spectra

FF = 0 = overlap

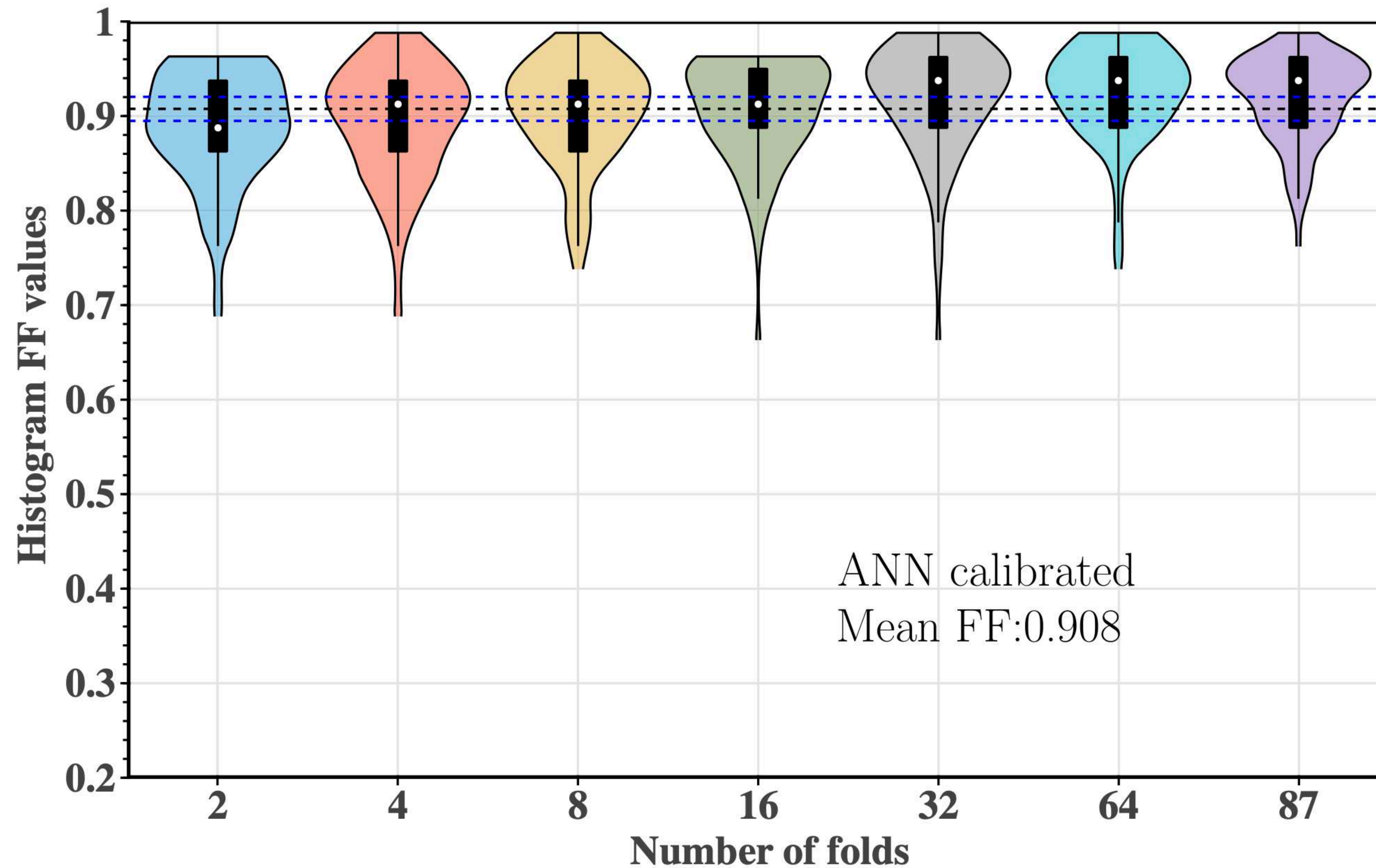
Impact of uncertainty in empirical relation offset by re-calibration of spectra.

ANN outperforms multivariate linear regression.



ANN SURROGATE IN THE FREQUENCY DOMAIN

Cross-validation study of fitting factors distribution:



THANK YOU FOR YOUR ATTENTION

SEARCH IN O3 DATA WITH ARESGW

Total number of BBH events previously found by GWTC+OGC+IAS+pycbc_KDE inside training range = **43**

We also find **8 new candidate events** $p_{\text{astro}} > 0.5$.

AresGW detects **42 out of the total of 51** events
(*most sensitive pipeline in this mass range*)

TABLE III: Performance of AresGW in comparison to the GWTC, OGC, IAS and pycbc_KDE [15] algorithms on all 51 candidate events (43 previously published plus 8 new events detected by AresGW) that are within the effective training range.

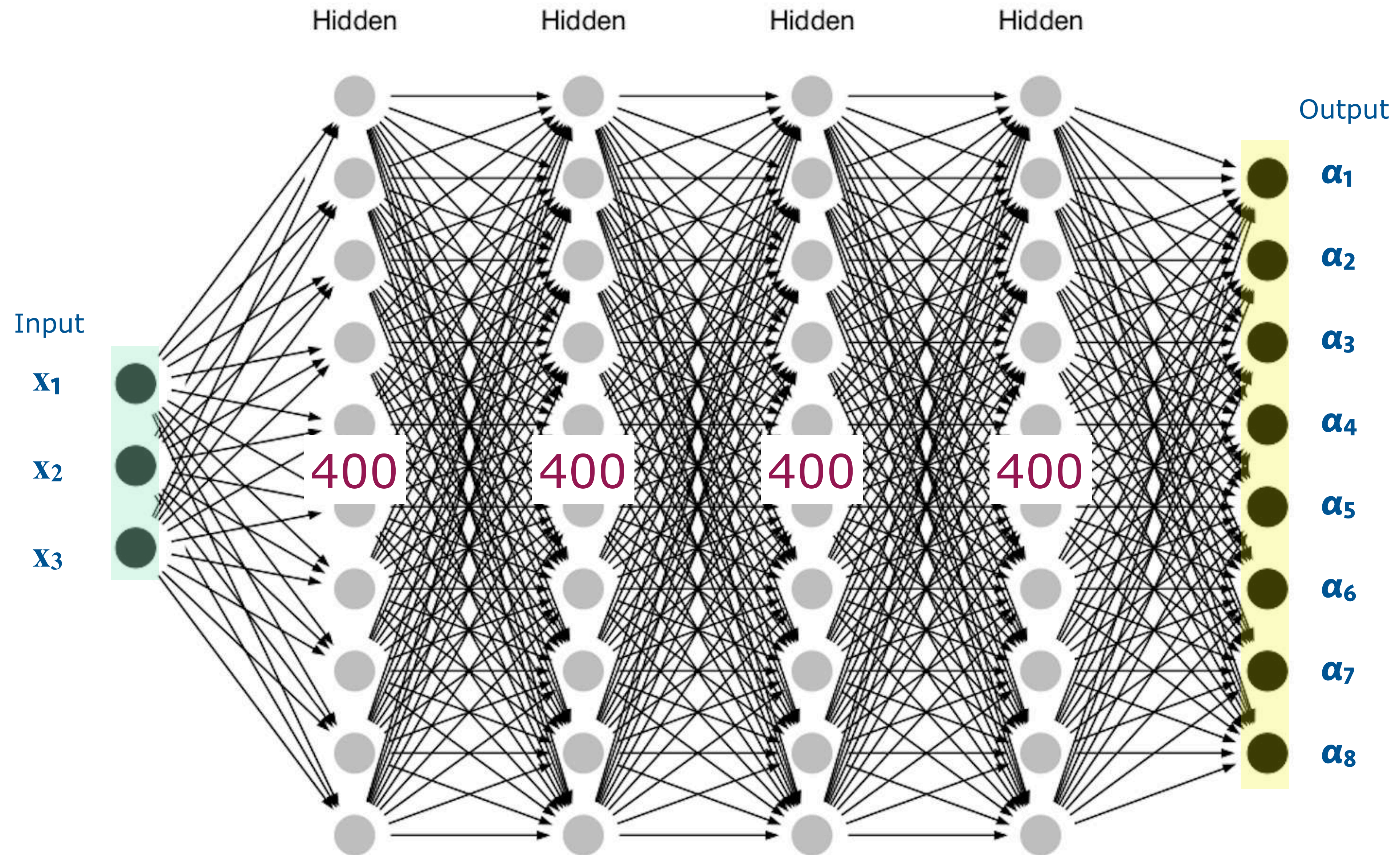
cwb	pycbc_broad	mbta	gstlal	pycbc_KDE	pycbc_bbh	IAS_a	IAS_b	OGC	AresGW
7	20	27	27	29	31	34	36	37	42

PARAMETERS OF NEW GW DETECTIONS WITH AresGW

TABLE VIII: Parameter estimation for the new AresGW candidate events.

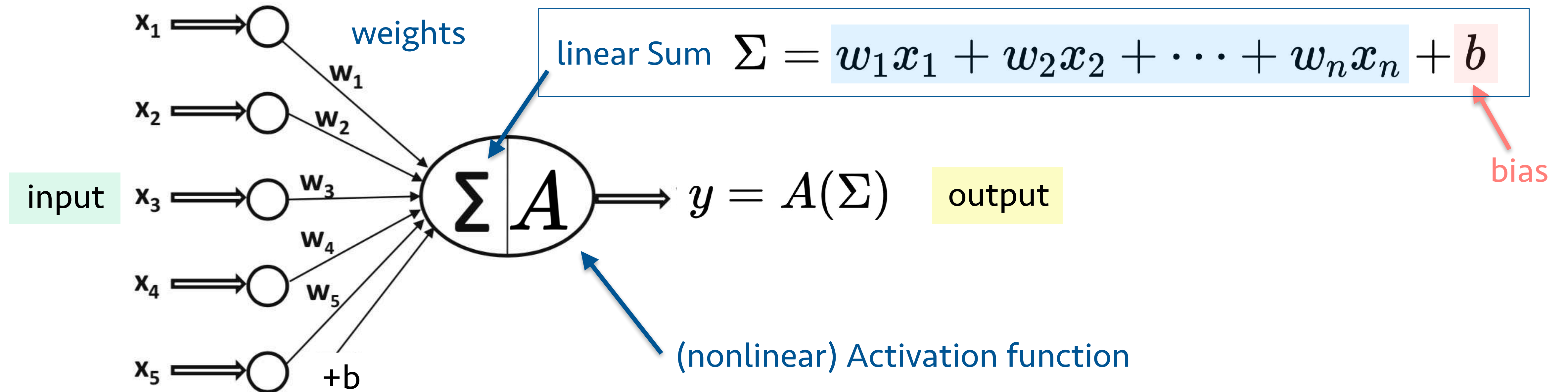
#	Event Name	$\mathcal{M}$ ($M_{\odot}$)	q	m_1 ($M_{\odot}$)	m_2 ($M_{\odot}$)	D_L (Mpc)	χ_{eff}	SNR (H1)	SNR (L1)	SNR $\hat{\rho}$ (network)
1	GW190511_125545	$28.95^{+9.45}_{-6.86}$	$0.72^{+0.25}_{-0.36}$	$40.7^{+16.2}_{-10.5}$	$28.2^{+11.6}_{-11.2}$	3707^{+3471}_{-2173}	$0.23^{+0.25}_{-0.29}$	2.29	7.34	7.29
2	GW190614_134749	$25.97^{+16.59}_{-6.20}$	$0.70^{+0.27}_{-0.36}$	$37.0^{+31.8}_{-10.7}$	$25.2^{+15.2}_{-9.7}$	6551^{+9562}_{-3558}	$0.05^{+0.34}_{-0.34}$	3.51	6.08	7.02
3	GW190607_083827	$30.48^{+7.21}_{-4.68}$	$0.78^{+0.19}_{-0.29}$	$40.5^{+12.0}_{-7.6}$	$31.0^{+9.1}_{-8.2}$	4928^{+2725}_{-2435}	$0.01^{+0.26}_{-0.30}$	4.04	7.29	8.33
4	GW190904_104631	$21.24^{+5.76}_{-4.40}$	$0.64^{+0.31}_{-0.33}$	$31.3^{+14.5}_{-8.5}$	$19.7^{+7.1}_{-7.2}$	5614^{+4441}_{-2864}	$0.05^{+0.30}_{-0.37}$	4.50	4.88	6.64
5	GW190523_085933	$23.82^{+10.24}_{-7.95}$	$0.49^{+0.45}_{-0.32}$	$41.7^{+19.3}_{-15.5}$	$19.4^{+14.6}_{-10.5}$	6091^{+6613}_{-3702}	$0.42^{+0.31}_{-0.45}$	3.48	5.14	6.02
6	GW200208_211609	$18.83^{+4.68}_{-3.18}$	$0.69^{+0.28}_{-0.40}$	$26.9^{+14.6}_{-6.3}$	$18.0^{+6.4}_{-6.9}$	3669^{+3413}_{-1985}	$0.01^{+0.37}_{-0.37}$	4.75	6.22	7.83
7	GW190705_164632	$27.21^{+7.34}_{-5.24}$	$0.52^{+0.41}_{-0.32}$	$44.7^{+24.8}_{-12.8}$	$23.0^{+11.7}_{-9.8}$	5692^{+4030}_{-2863}	$0.29^{+0.26}_{-0.34}$	4.42	6.88	8.11
8	GW190426_082124	$17.93^{+4.12}_{-3.42}$	$0.45^{+0.45}_{-0.28}$	$31.5^{+22.5}_{-11.3}$	$13.8^{+6.9}_{-5.2}$	3213^{+4555}_{-1573}	$-0.01^{+0.39}_{-0.50}$	5.15	4.46	6.41

ARTIFICIAL NEURAL NETWORKS



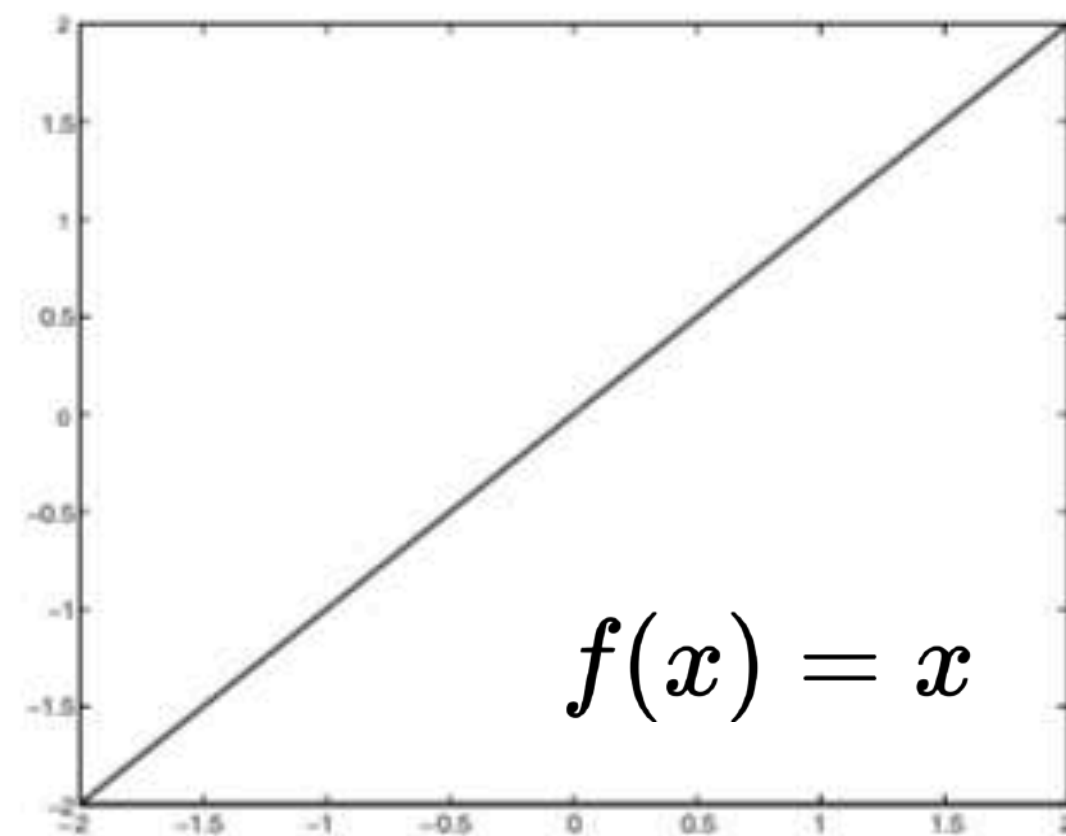
ARTIFICIAL NEURON

- Each **neuron** in the network maps several **input values** $x_1, \dots, x_n$ to an **output value** y

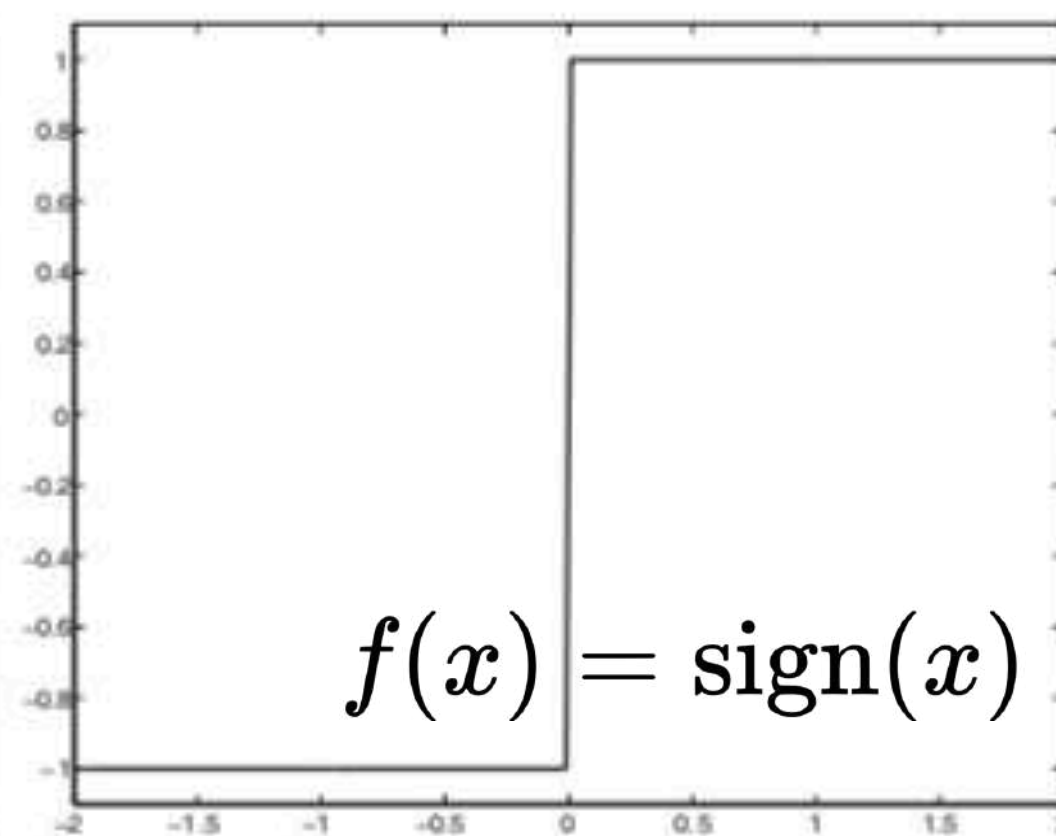


ACTIVATION FUNCTIONS

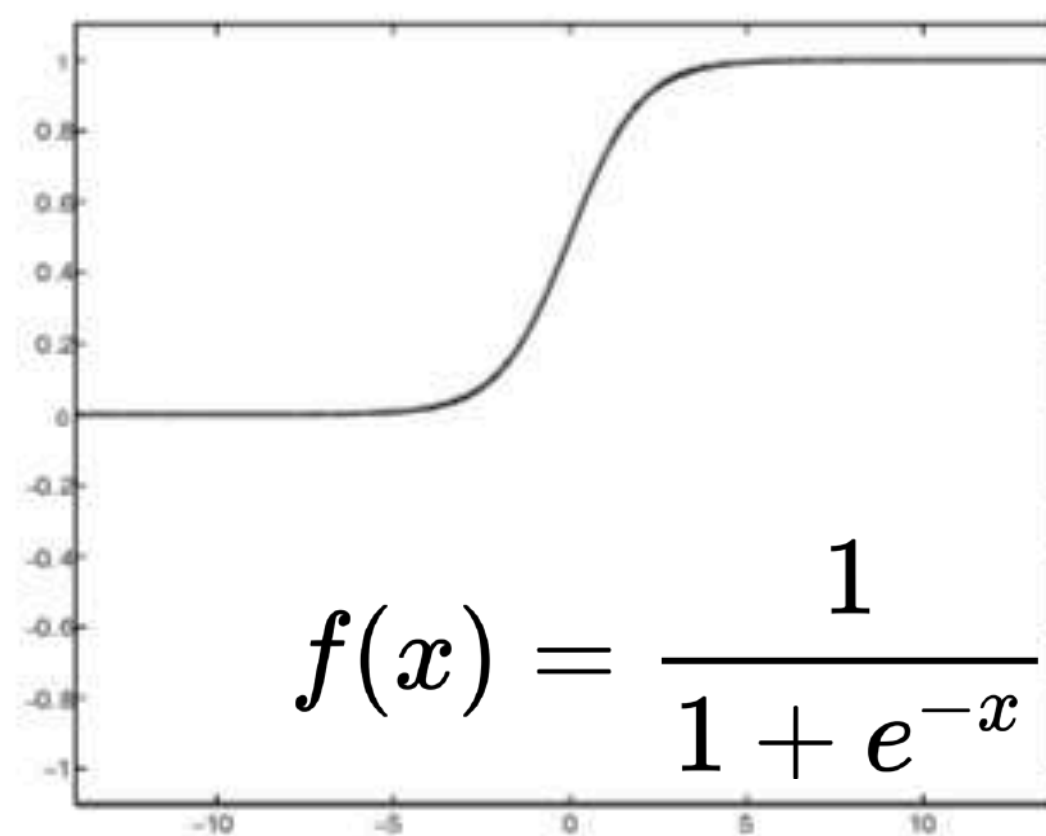
- Different common activation functions:



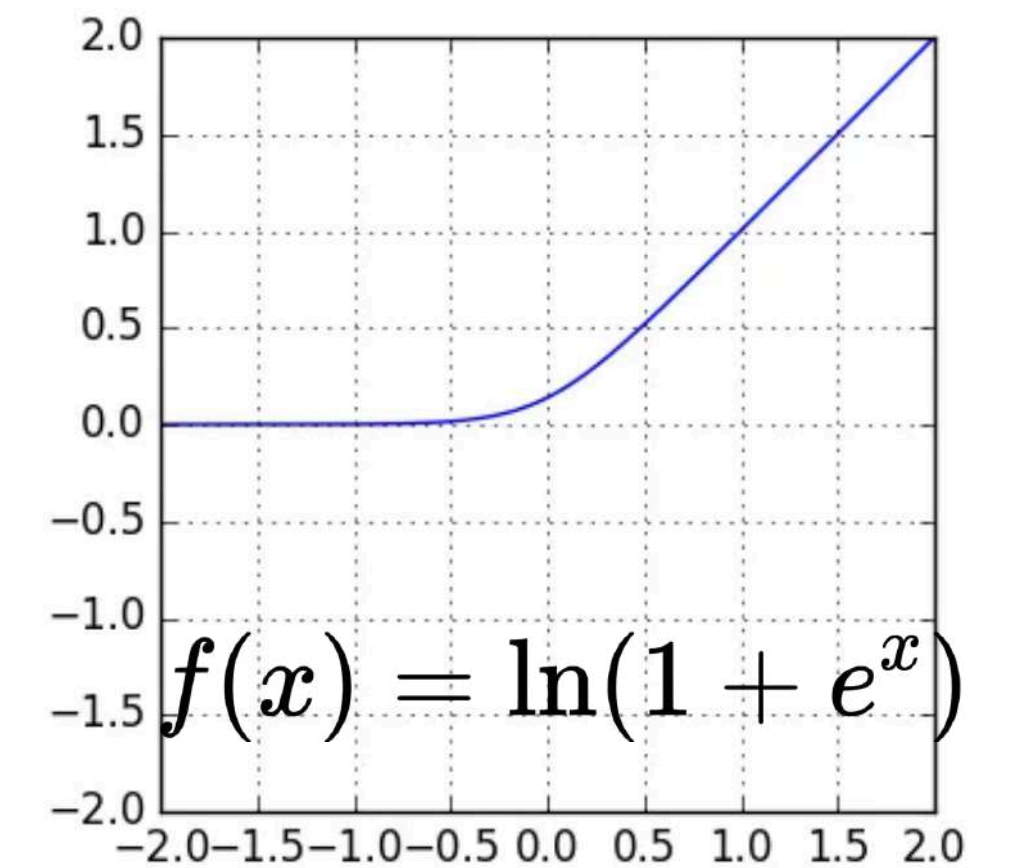
(a) Identity



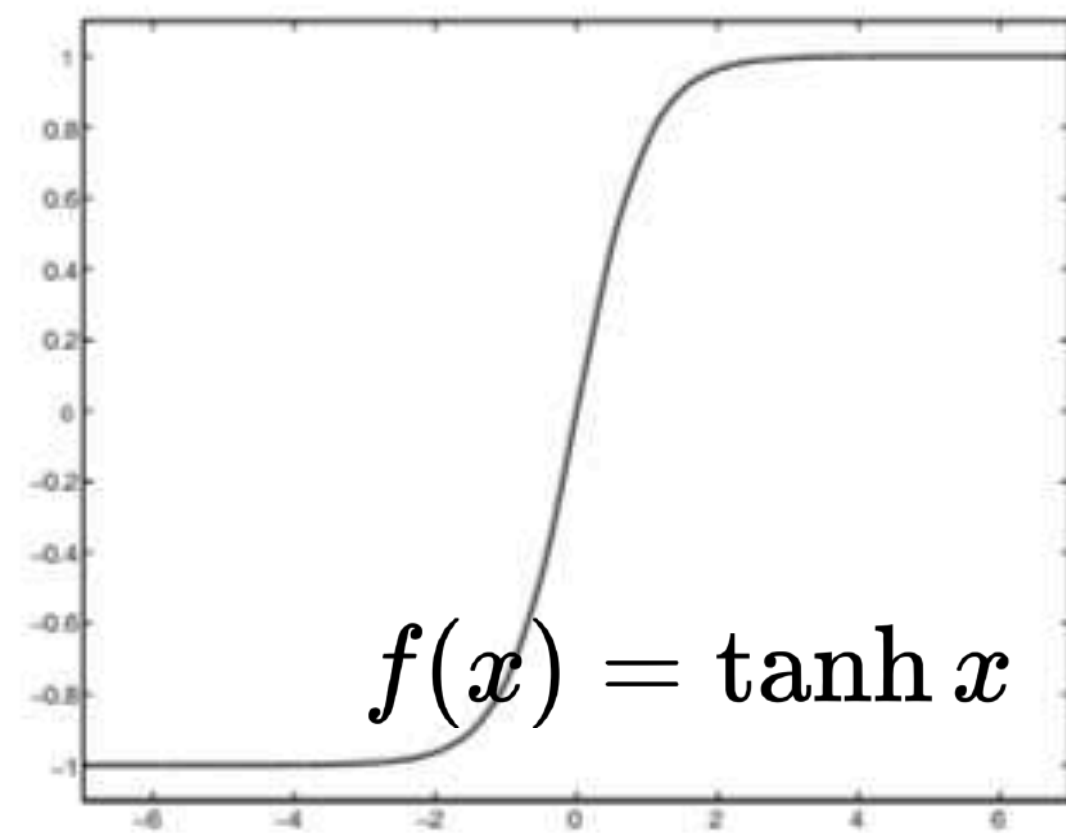
(b) Sign



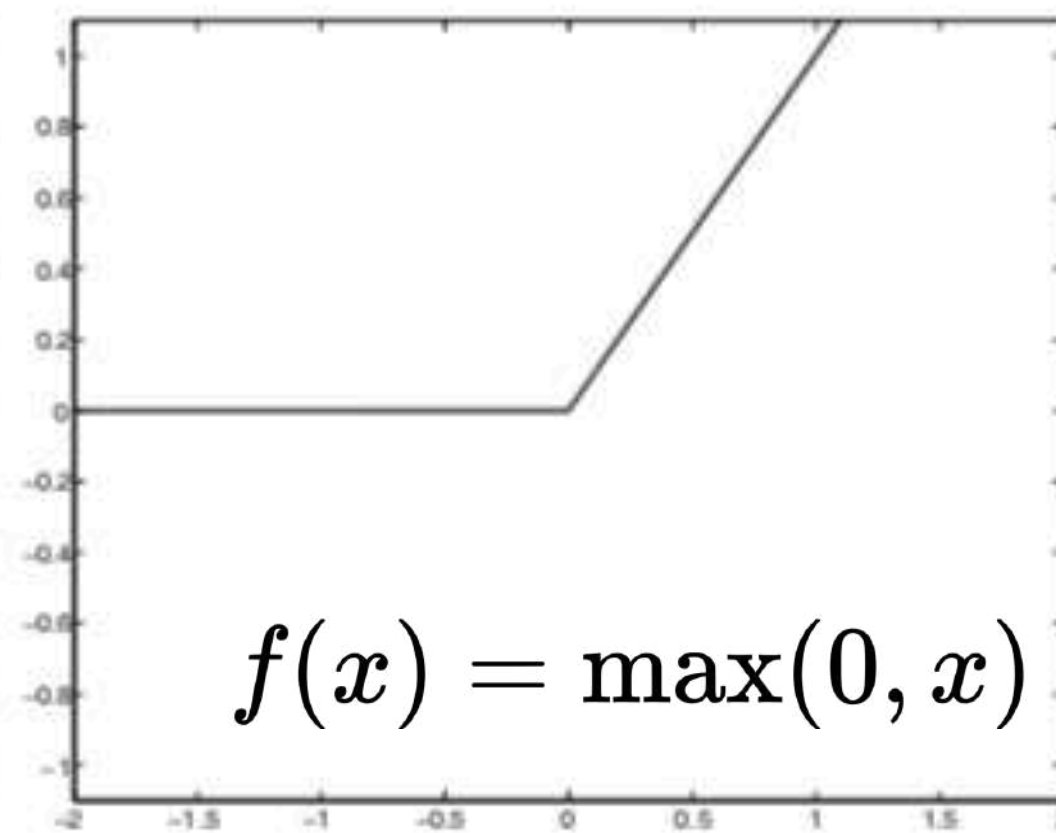
(c) Sigmoid (logistic function)



Softplus

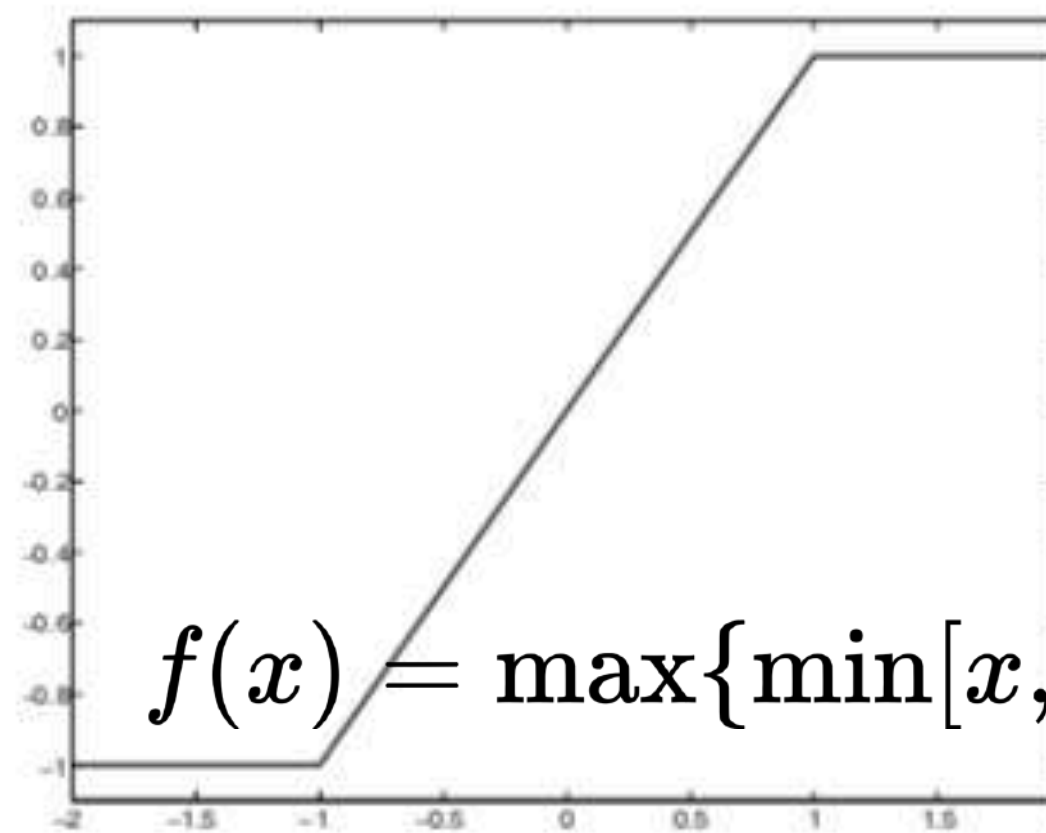


(d) Tanh



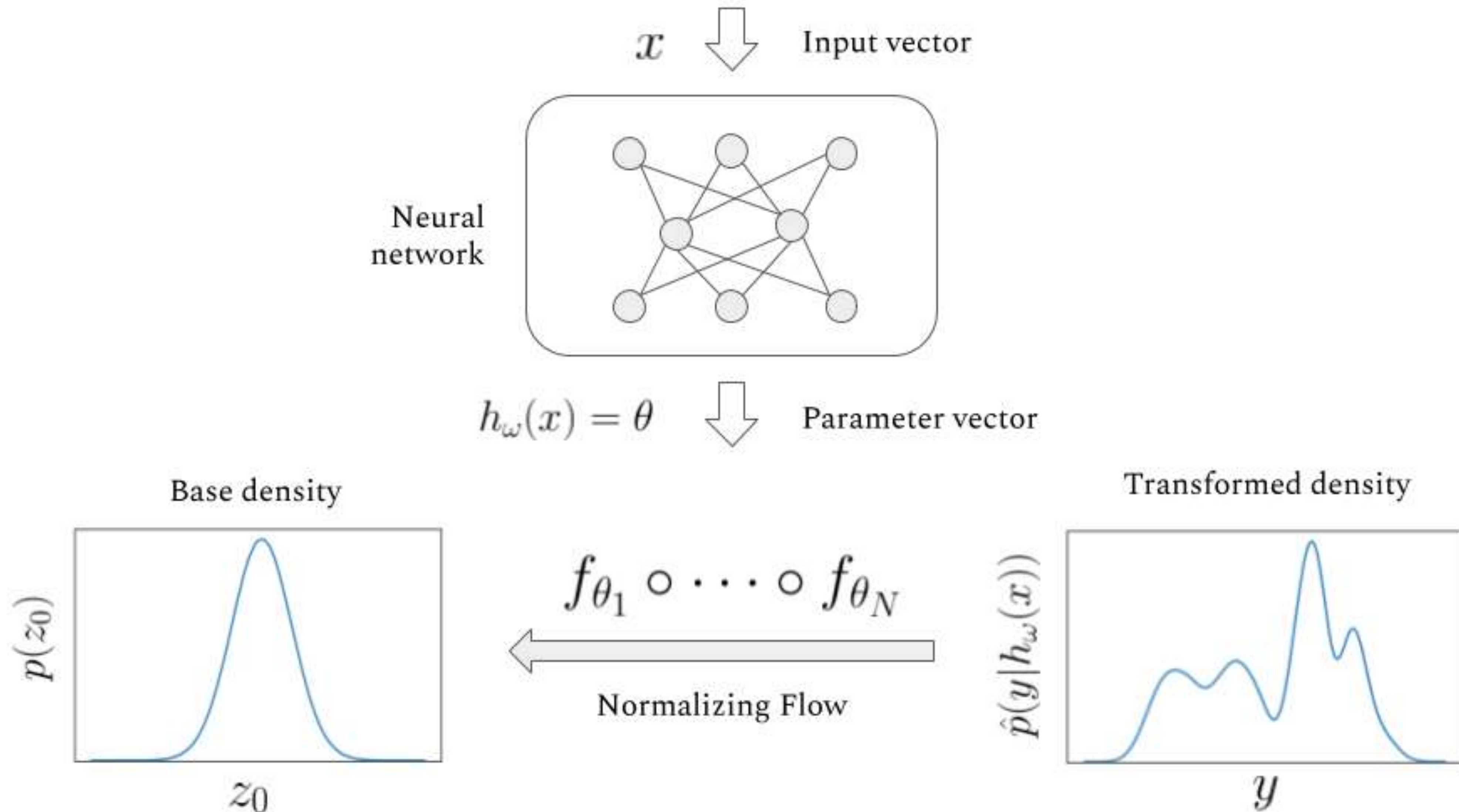
(e) ReLU

(Rectified Linear Unit)



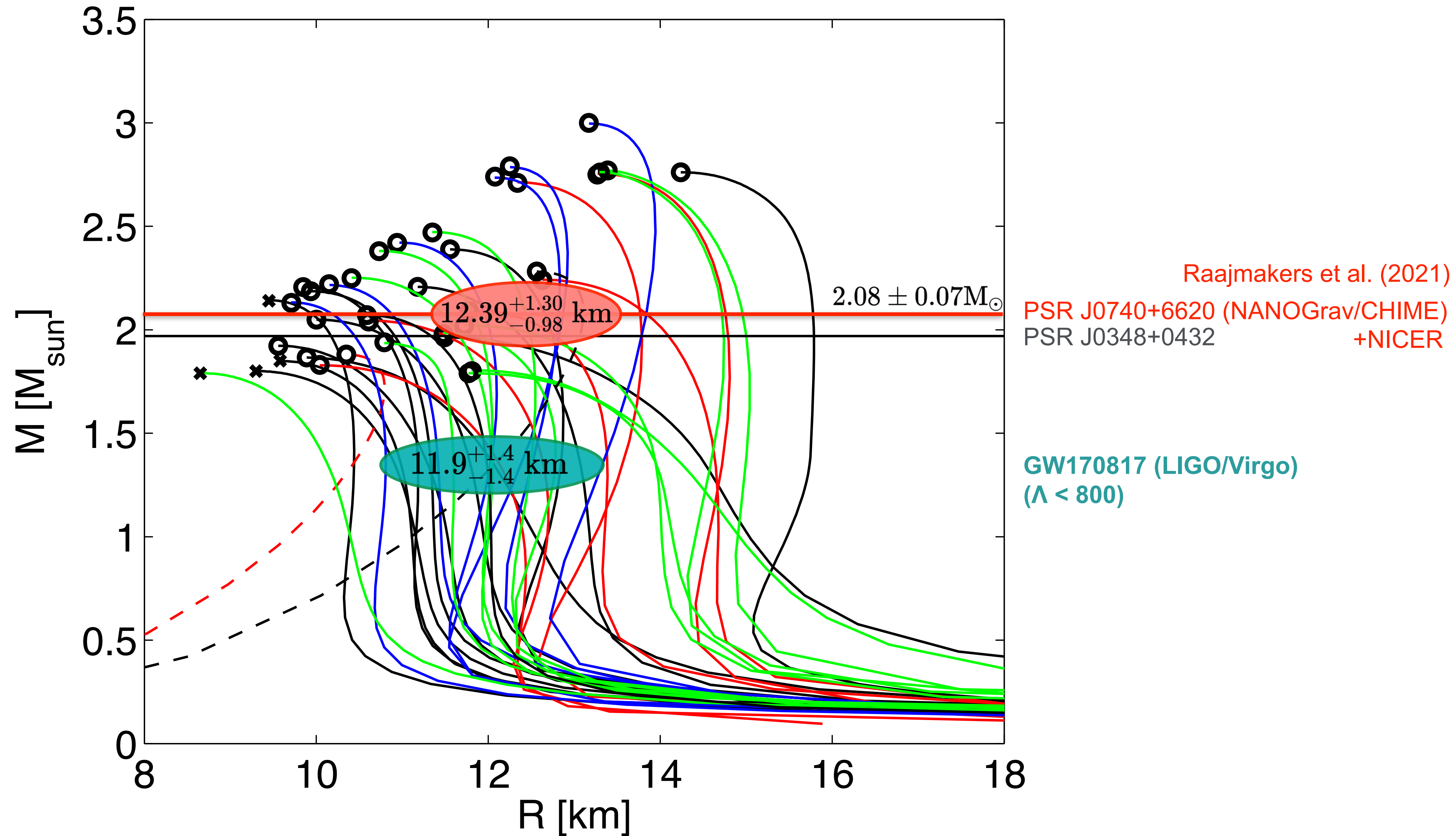
(f) Hard Tanh

NORMALIZING FLOWS



BACKUP SLIDES

CURRENT CONSTRAINTS ON MASS-RADIUS RELATION



ANN REGRESSION IN FREQUENCY DOMAIN

EOS	Waveforms	References	Component masses (in $M_{\odot}$)
ALF2	10	Rezzolla and Takami [45] and CoRe v2 [27]	1.2, 1.225, 1.25, 1.275, 1.3, 1.325, 1.35, 1.3505, 1.375, 1.3755
APR4	7	Rezzolla and Takami [45]	1.2, 1.225, 1.25, 1.275, 1.3, 1.325, 1.35
BHB1p	4	CoRe v2 [27]	1.25, 1.3, 1.35, 1.4
BLh	4	CoRe v2 [27]	1.3, 1.3325, 1.364, 1.4
DD2	7	CoRe v2 [27]	1.2, 1.25, 1.3, 1.35, 1.364, 1.4, 1.5
ENG	1	CoRe v2 [27]	1.3495
GNH3	7	Rezzolla and Takami [45]	1.2, 1.225, 1.25, 1.275, 1.3, 1.325, 1.35
H4	13	Rezzolla and Takami [45] and CoRe v2 [27]	1.2, 1.225, 1.25, 1.275, 1.3, 1.325, 1.3495, 1.35, 1.3505, 1.3715, 1.3725, 1.3735, 1.3795
LS220	4	CoRe v2 [27]	1.2, 1.35, 1.364, 1.4
MPA1	8	Soultanis <i>et al.</i> [97]	1.2, 1.25, 1.3, 1.35, 1.4, 1.45, 1.5, 1.55
MS1	2	CoRe v2 [27]	1.3495, 1.351
MS1b	8	CoRe v2 [27]	1.35, 1.3505, 1.375, 1.3805, 1.381, 1.5, 1.6, 1.7
SFHo	2	CoRe v2 [27]	1.35, 1.364
SLy	10	Rezzolla and Takami [45] and CoRe v2 [27]	1.2, 1.225, 1.25, 1.275, 1.3, 1.325, 1.35, 1.351, 1.3575, 1.364

Injected waveform

$$d(t) = h(t) + n(t)$$

Gaussian likelihood function

$$\mathcal{L}(d \mid \boldsymbol{\theta}) \propto \exp[-\langle d(t) - h(\boldsymbol{\theta}, t), d(t) - h(\boldsymbol{\theta}, t) \rangle]$$

where the inner product is

$$\langle h, g \rangle = 4\Re \int_0^\infty \frac{\tilde{h}(f)\tilde{g}^*(f)}{S(f)} df$$

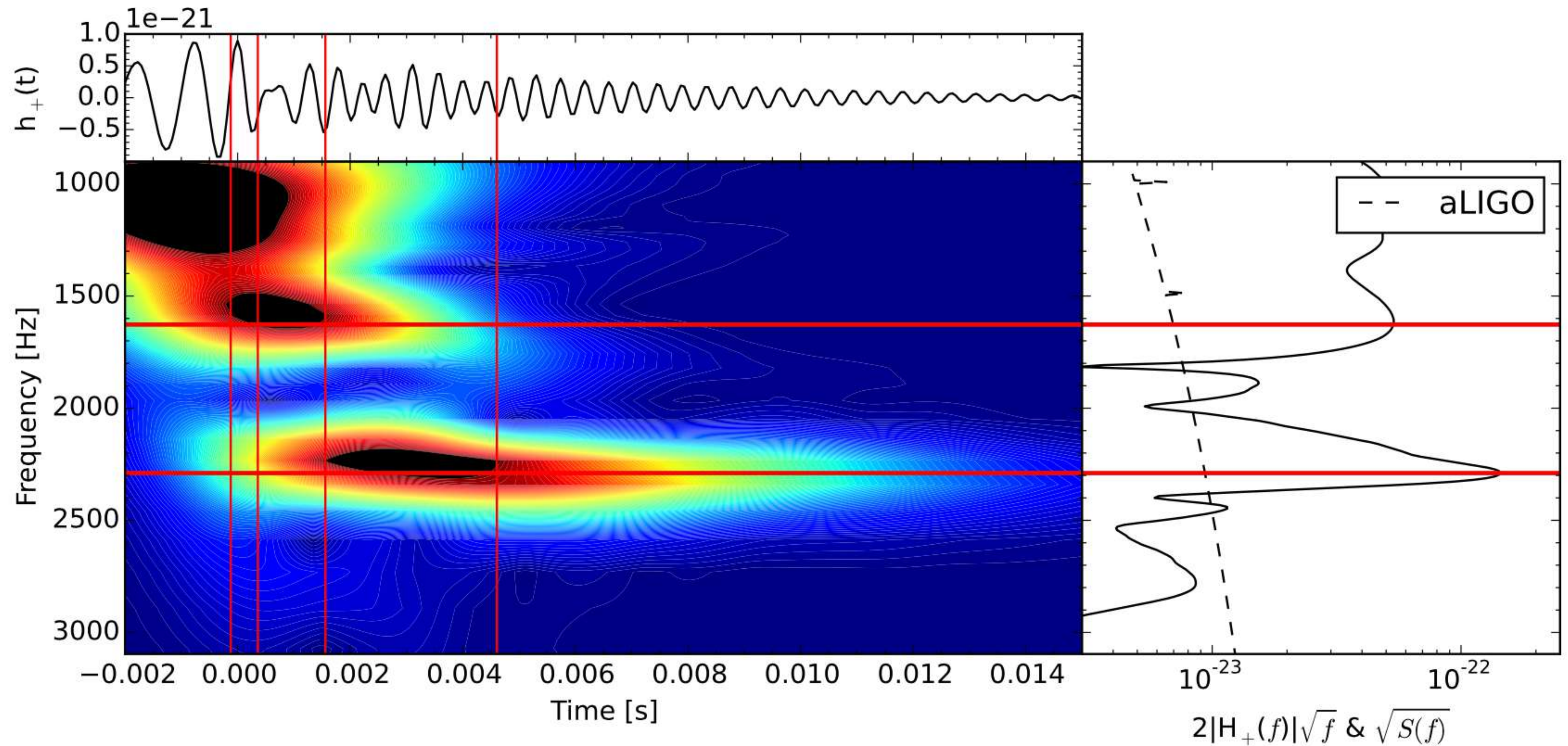
Fitting factor

$$\mathcal{F}(d(t), h(\boldsymbol{\theta}, t)) \equiv \frac{\langle d(t) \mid h(\boldsymbol{\theta}, t) \rangle}{\sqrt{\langle d(t) \mid d(t) \rangle \langle h(\boldsymbol{\theta}, t) \mid h(\boldsymbol{\theta}, t) \rangle}}$$

Optimal SNR

$$\rho_{\text{opt},i} = \langle h, h \rangle^{1/2} \quad \rho_{\text{opt}} = \left(\sum_{i \in \text{HLV}} \rho_{\text{opt},i}^2 \right)^{1/2}$$

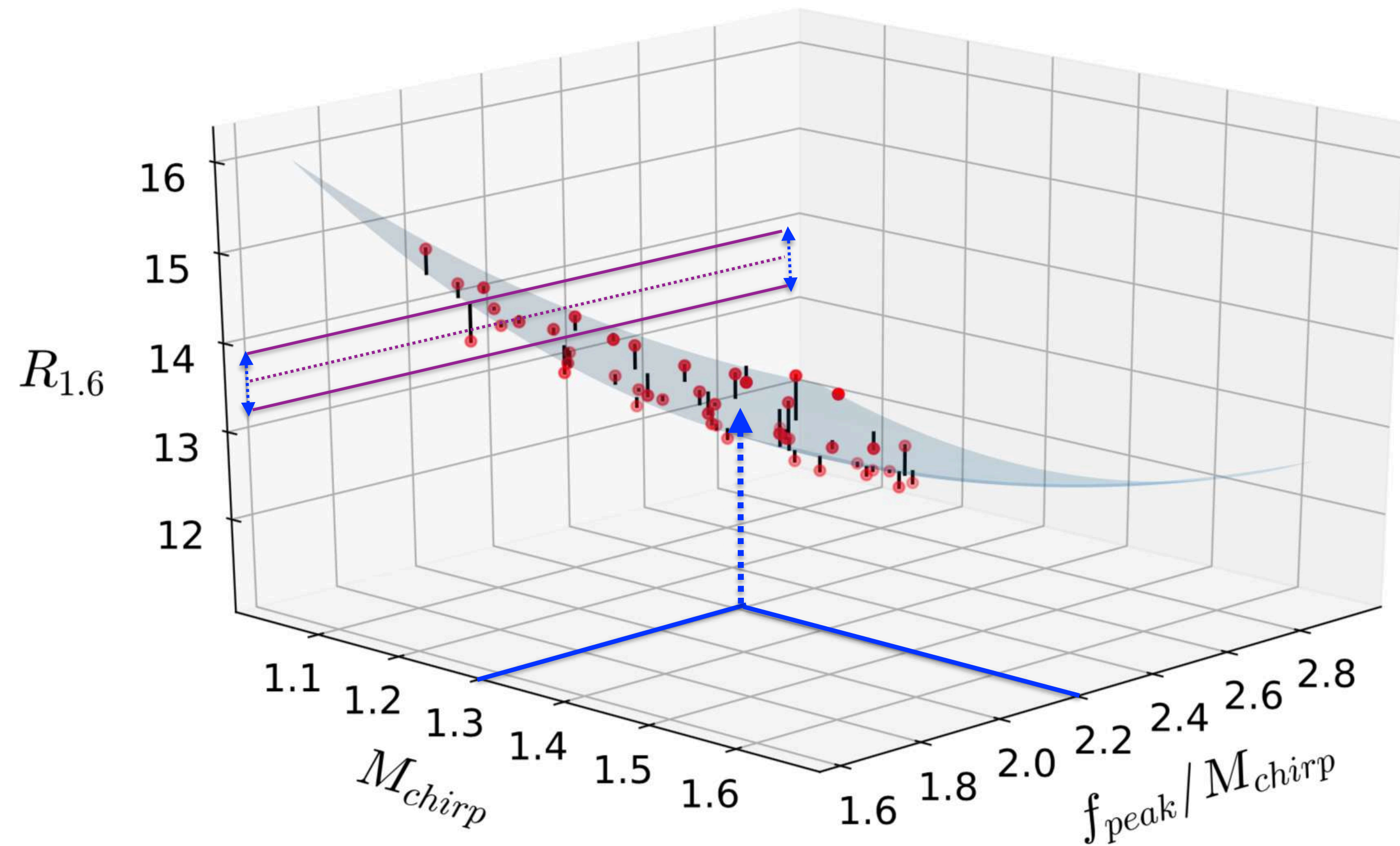
POST-MERGER SPECTROGRAMS



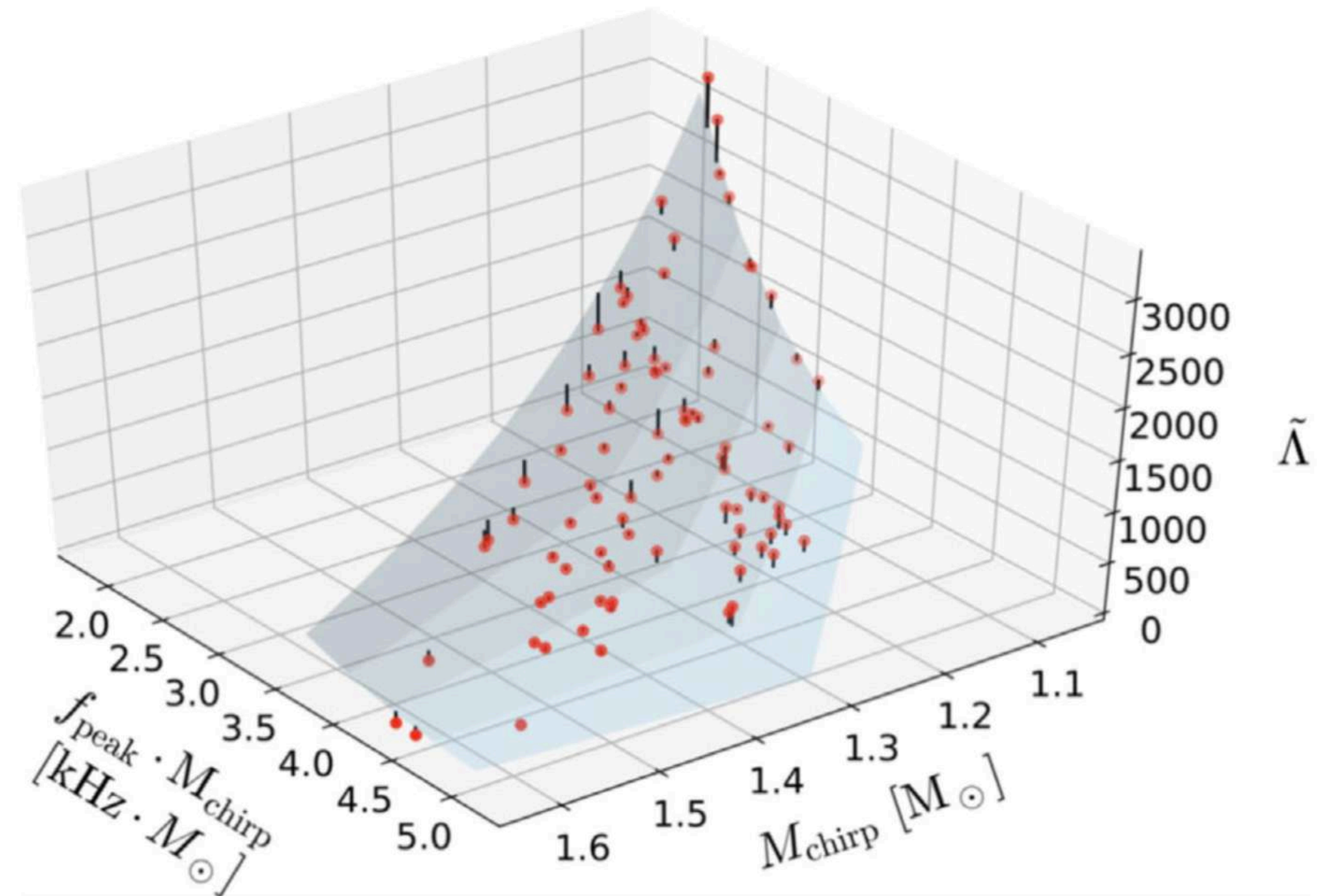
Clark, Bauswein, Stergioulas, Shoemaker (2016)

EMPIRICAL RELATIONS FOR GW ASTEROSEISMOLOGY OF BNS MERGERS

$$R_{1.6} = 43.796 - 19.984M_{\text{chirp}} - 12.921f_{\text{peak}}/M_{\text{chirp}} \\ + 4.674M_{\text{chirp}}^2 + 3.371f_{\text{peak}} + 1.26(f_{\text{peak}}/M_{\text{chirp}})^2$$



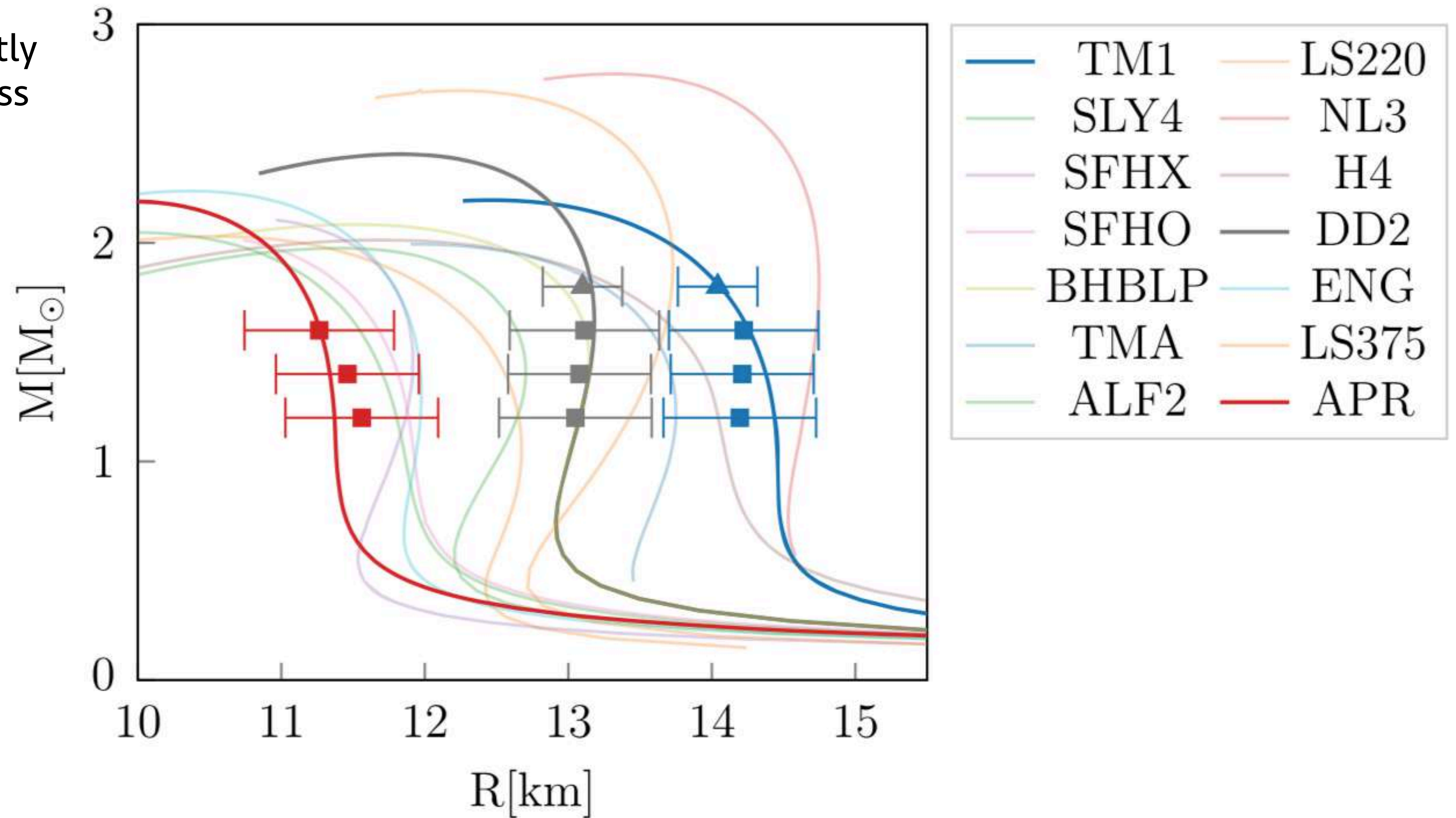
$$\tilde{\Lambda} = -1344 + 108.9M_{\text{chirp}}f_{\text{peak}} + 17208f_{\text{peak}}^{-2}$$



Vreinaris, Stergioulas & Bauswein (2020)

EOS CONSTRAINTS THROUGH POST-MERGER REMNANTS

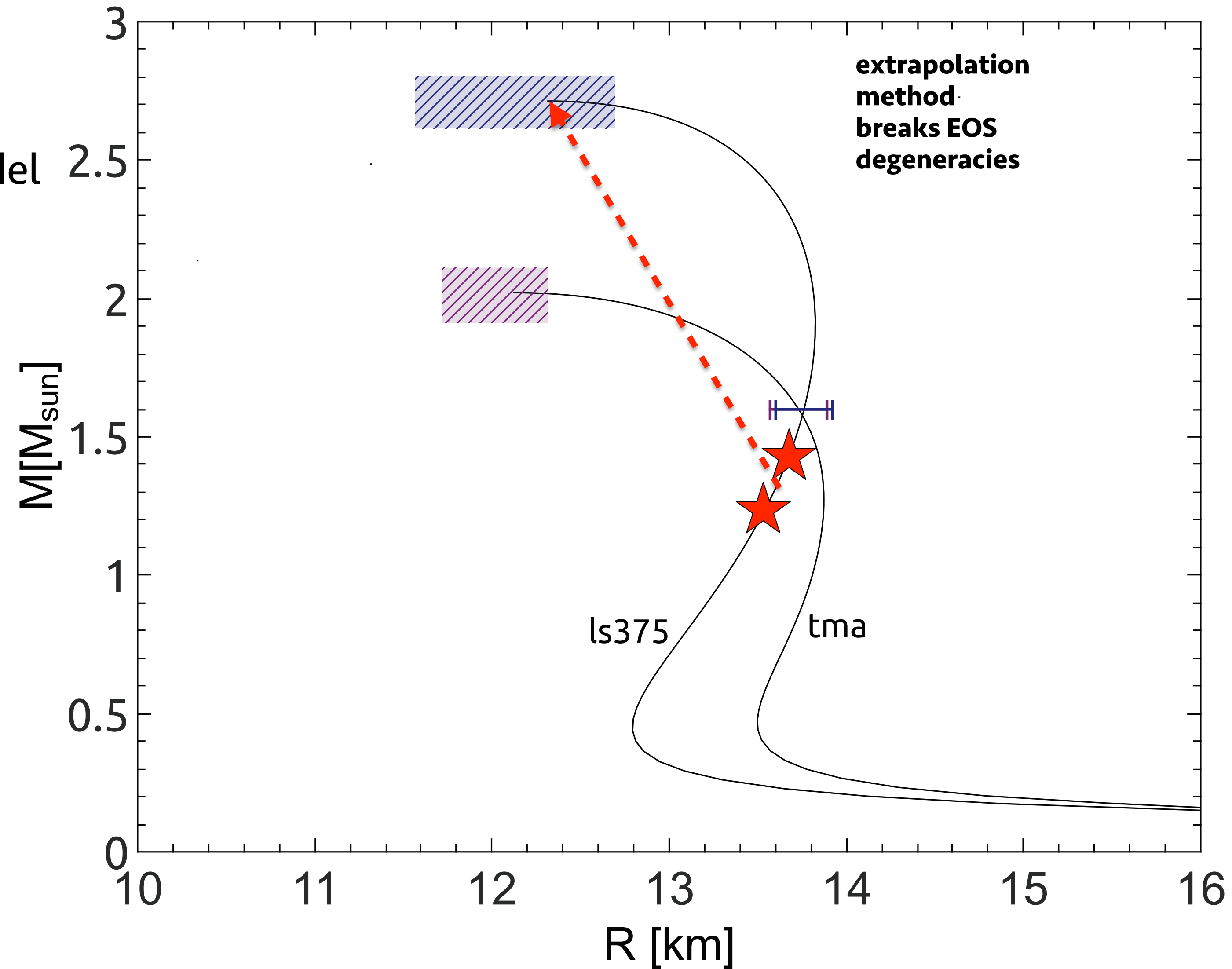
It will be possible to directly extract the radius in a mass range $1.2 - 1.8M_{\odot}$



Vretinakis, Stergioulas & Bauswein (2020)

EXTRAPOLATION METHOD

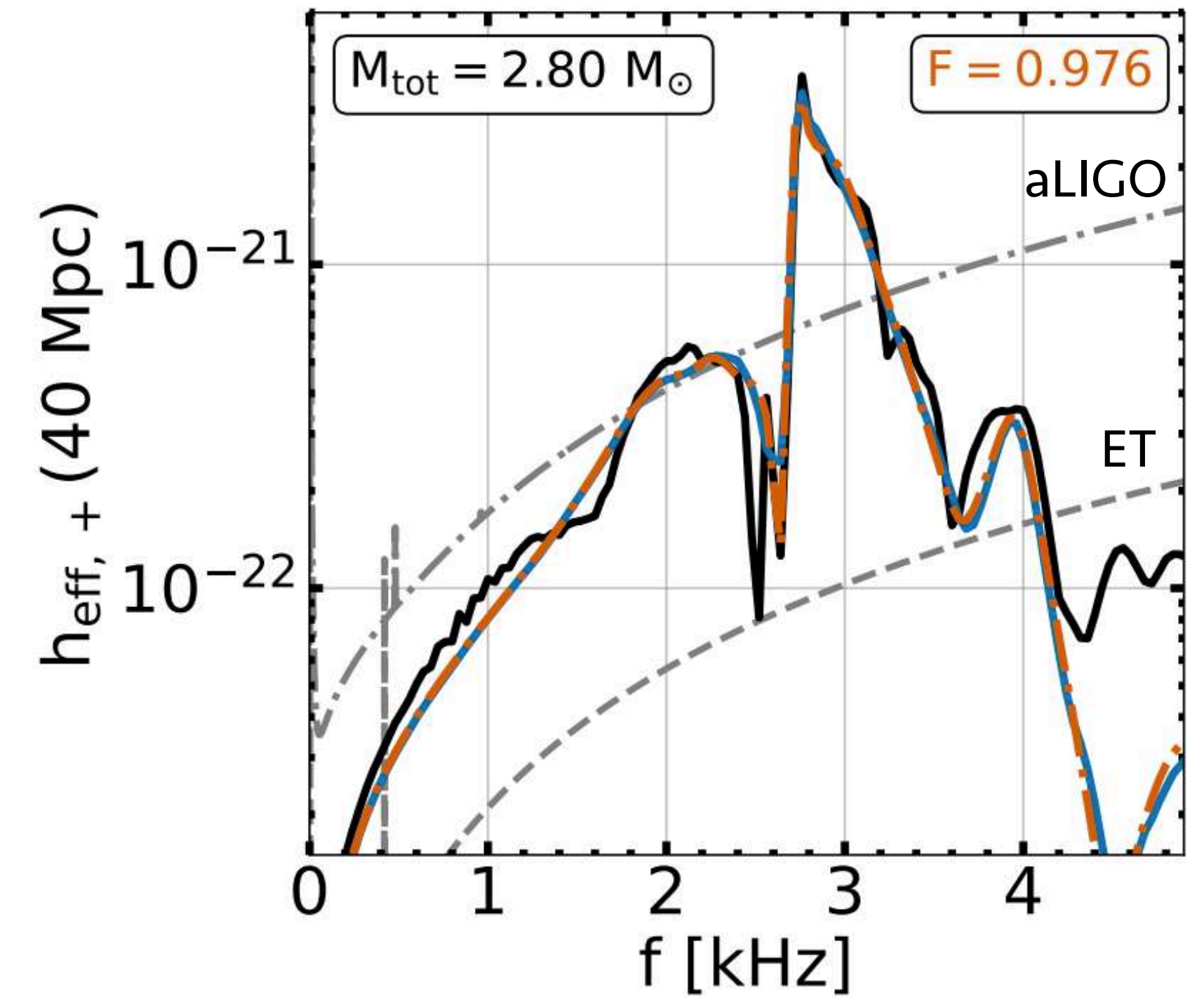
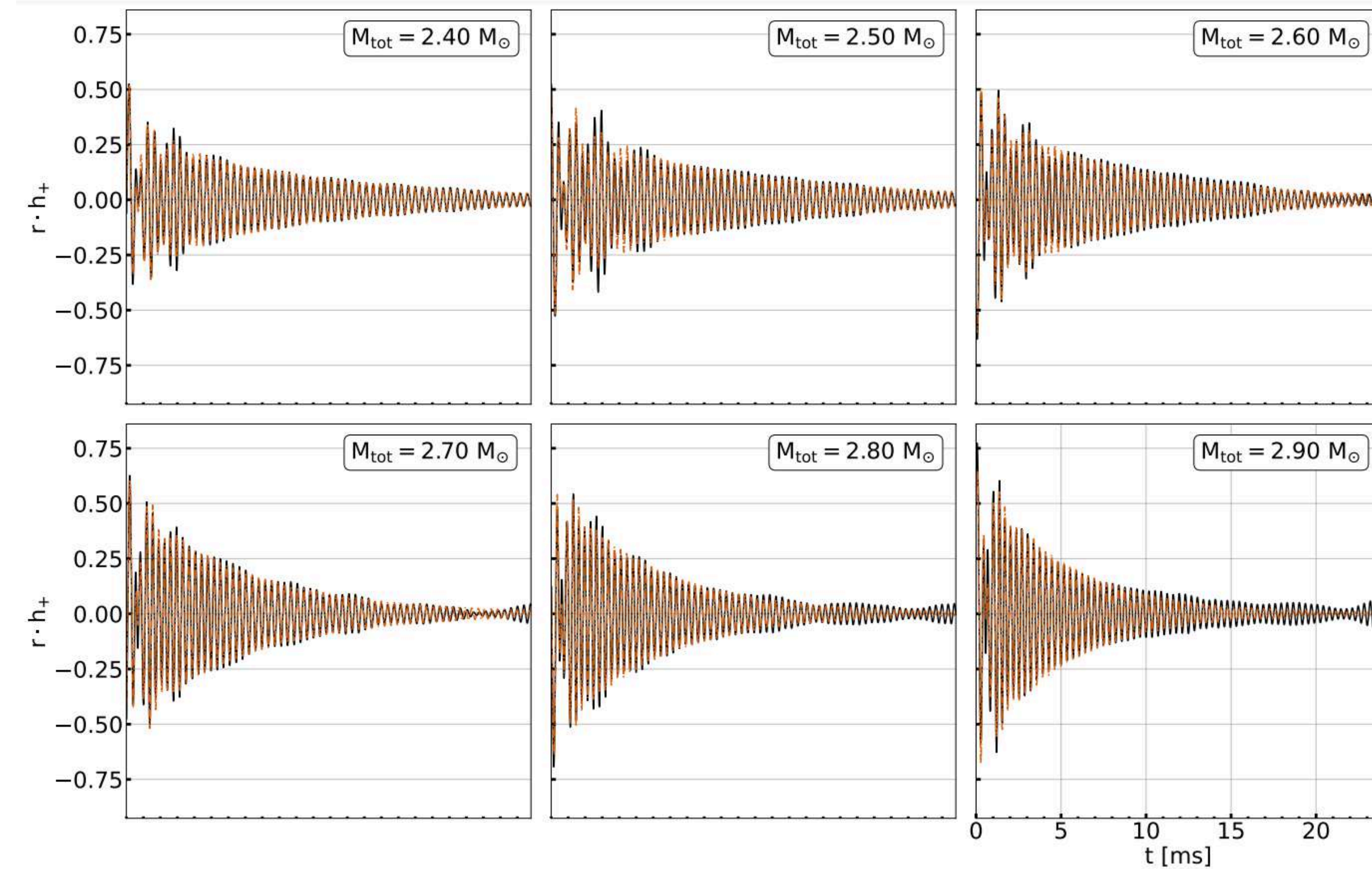
Extrapolation method allows for constraints on maximum mass model using only low-mass detections.



Bauswein, Stergioulas (2015)

NEW ANALYTIC WAVEFORM TEMPLATE

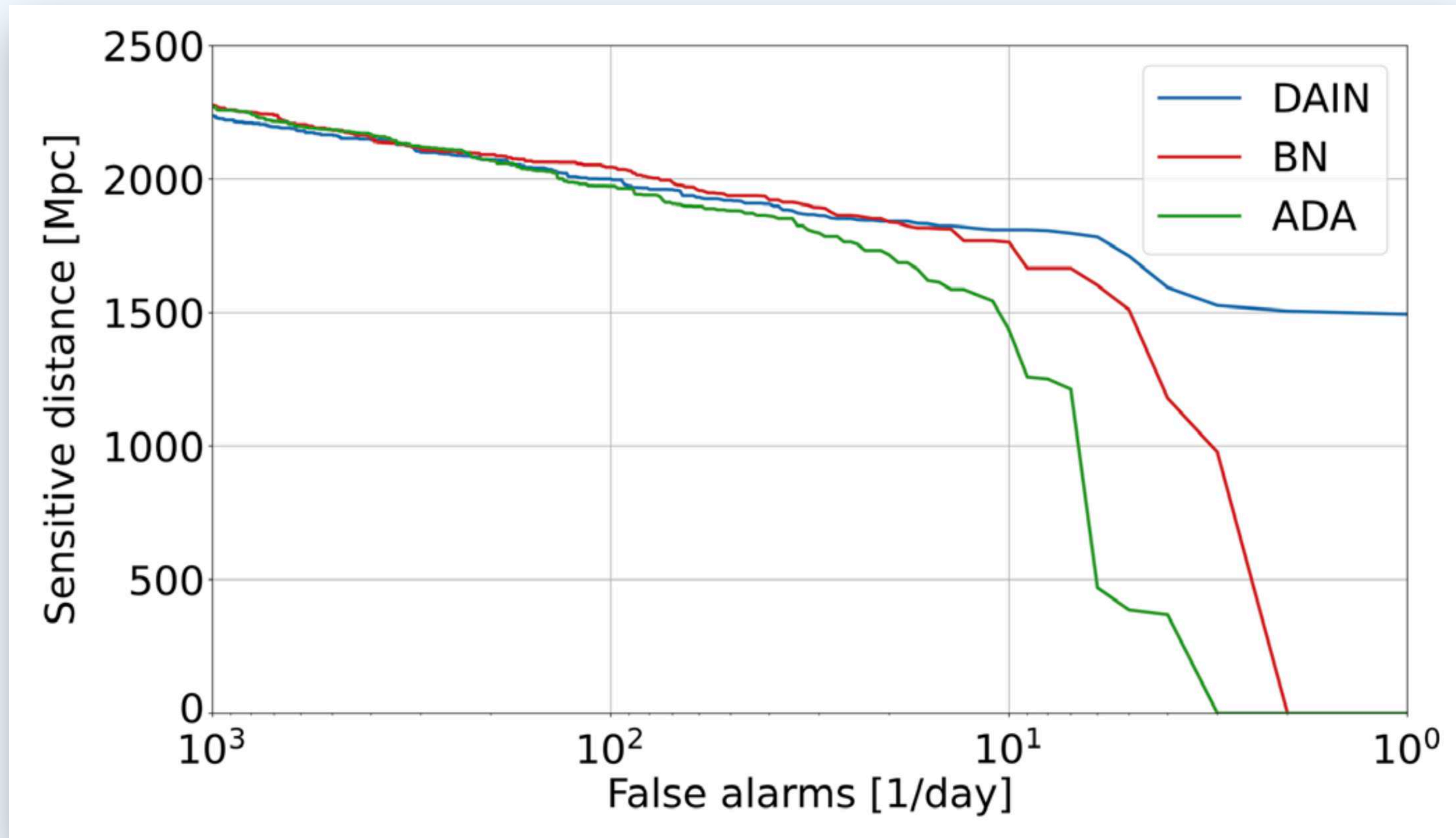
Relies only on **physical parameters**



Soultanis, Bauswein, Stergioulas (2022)

ADAPTIVE INPUT NORMALIZATION

Significant Improvement in Sensitive Distance using DAIN

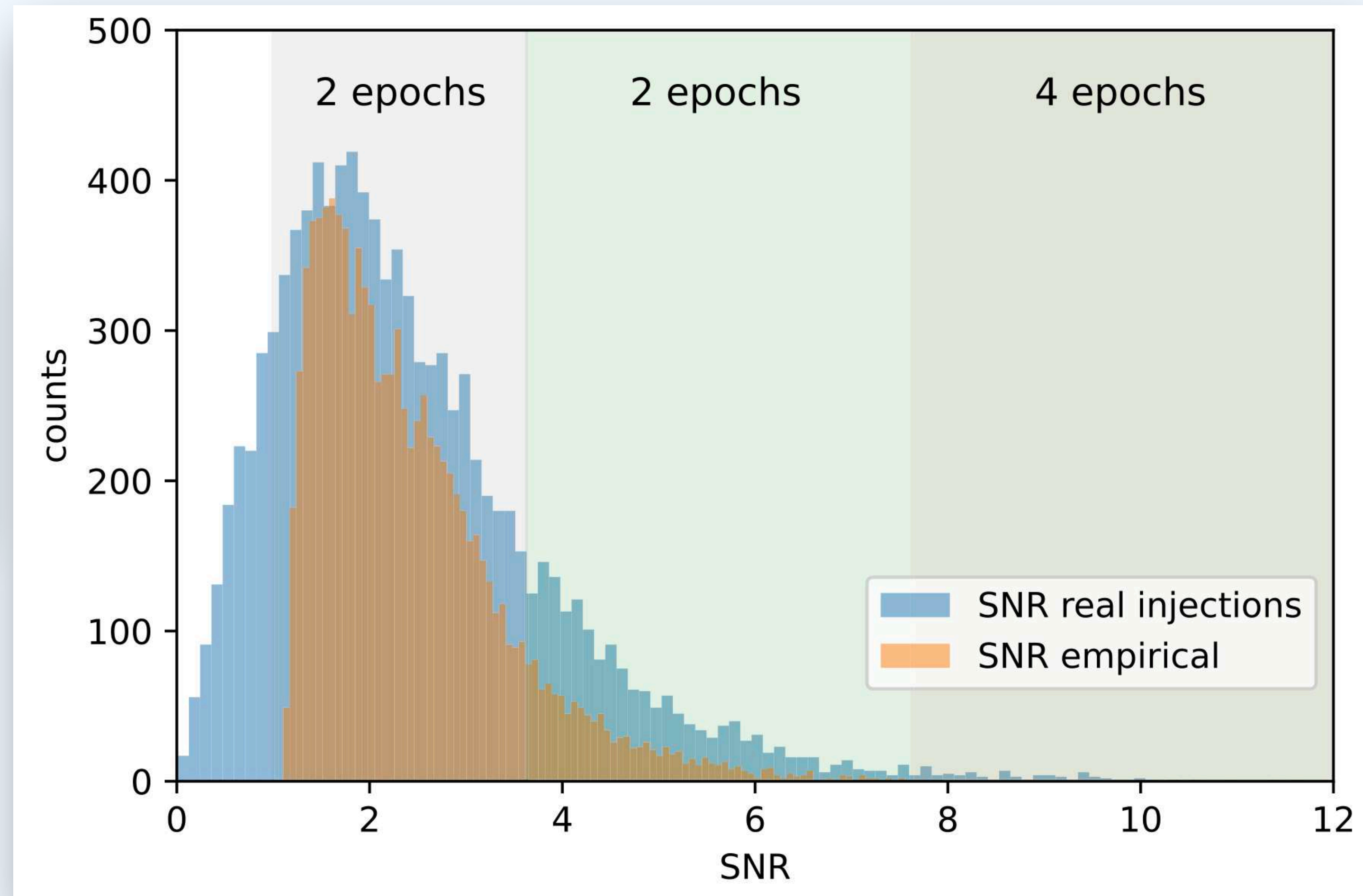


CURRICULUM LEARNING

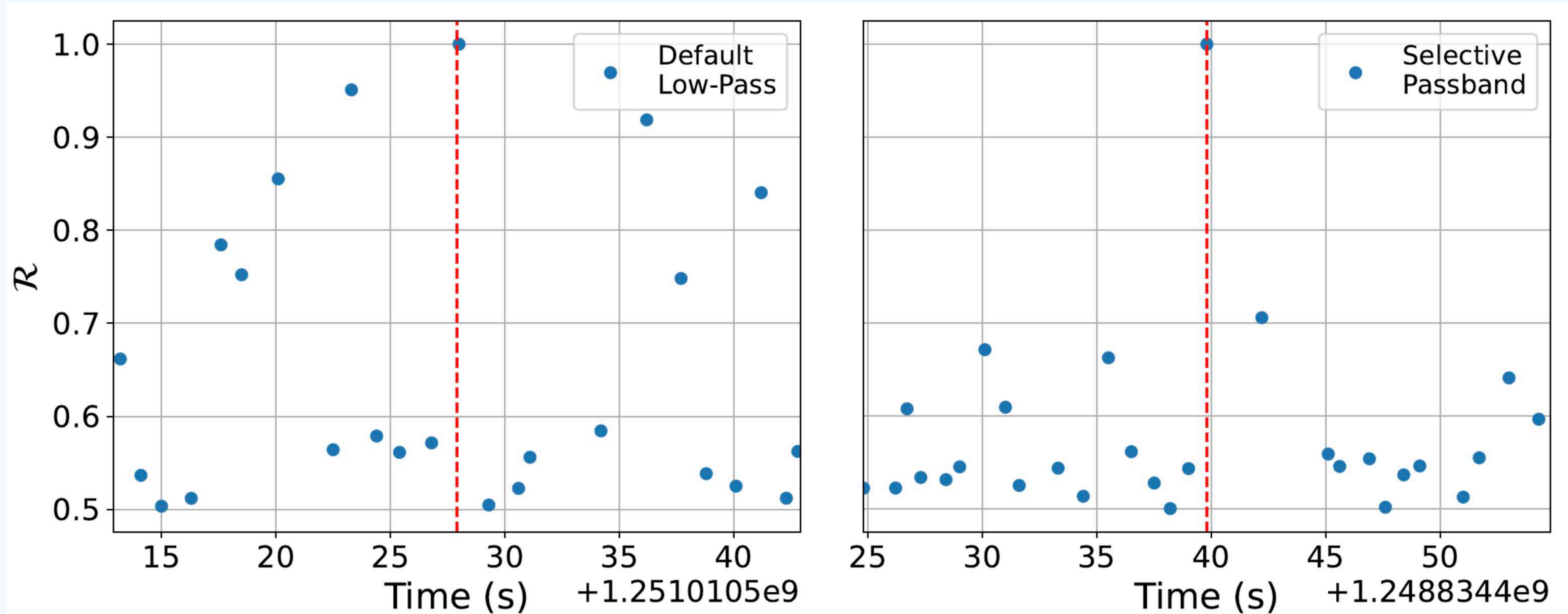
Curriculum learning based
on signal-to-noise ratio (**SNR**)

Epochs	Min(SNR)	Max(SNR)
4	7.63	100
2	3.63	100
2	1	3.63
2	1	7.63
Remaining	0	∞

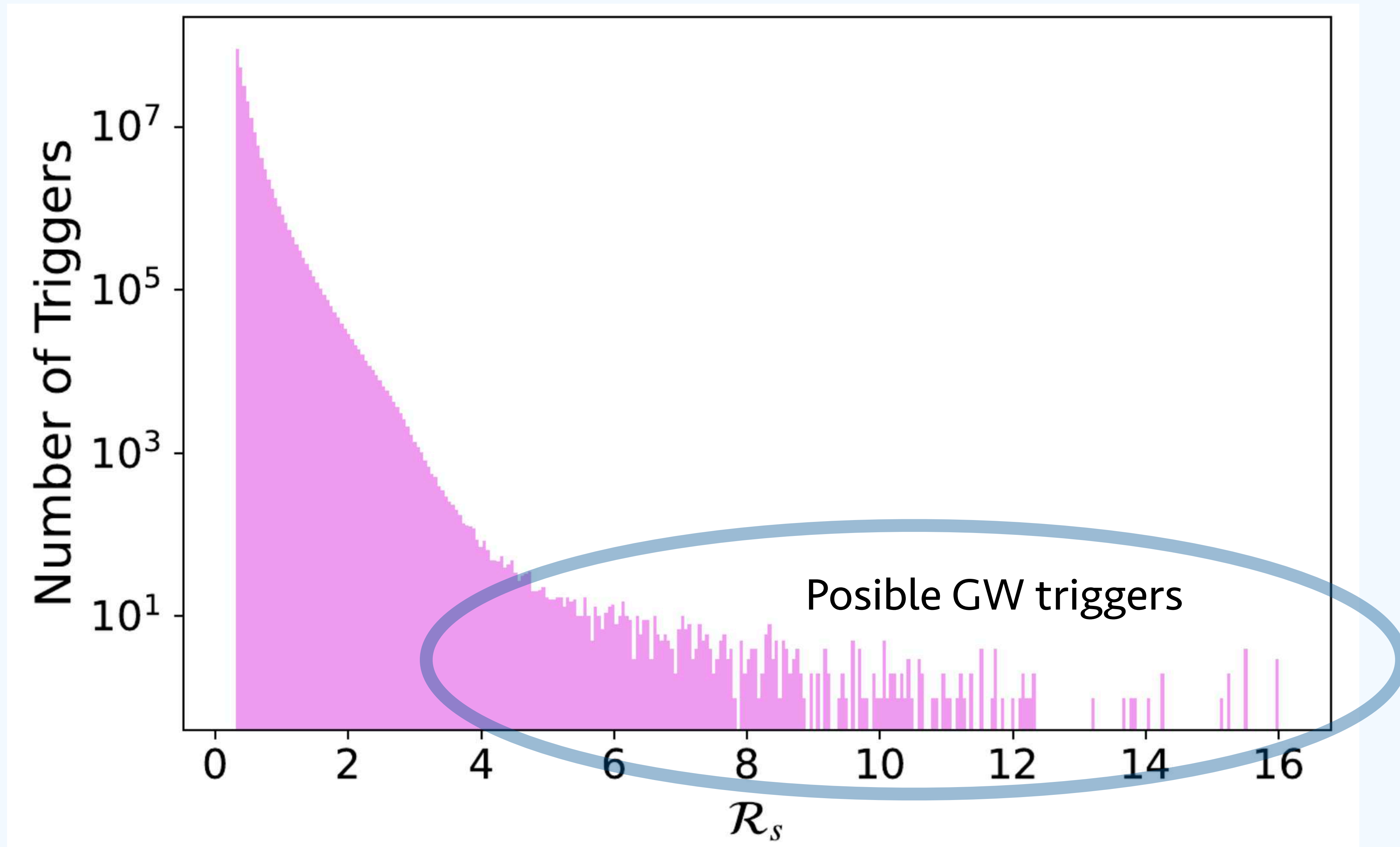
The network learns the louder
signals first and then refines its
weights to accommodate
weaker signals



HIERARCHICAL TRIGGER CLASSIFICATION SCHEME

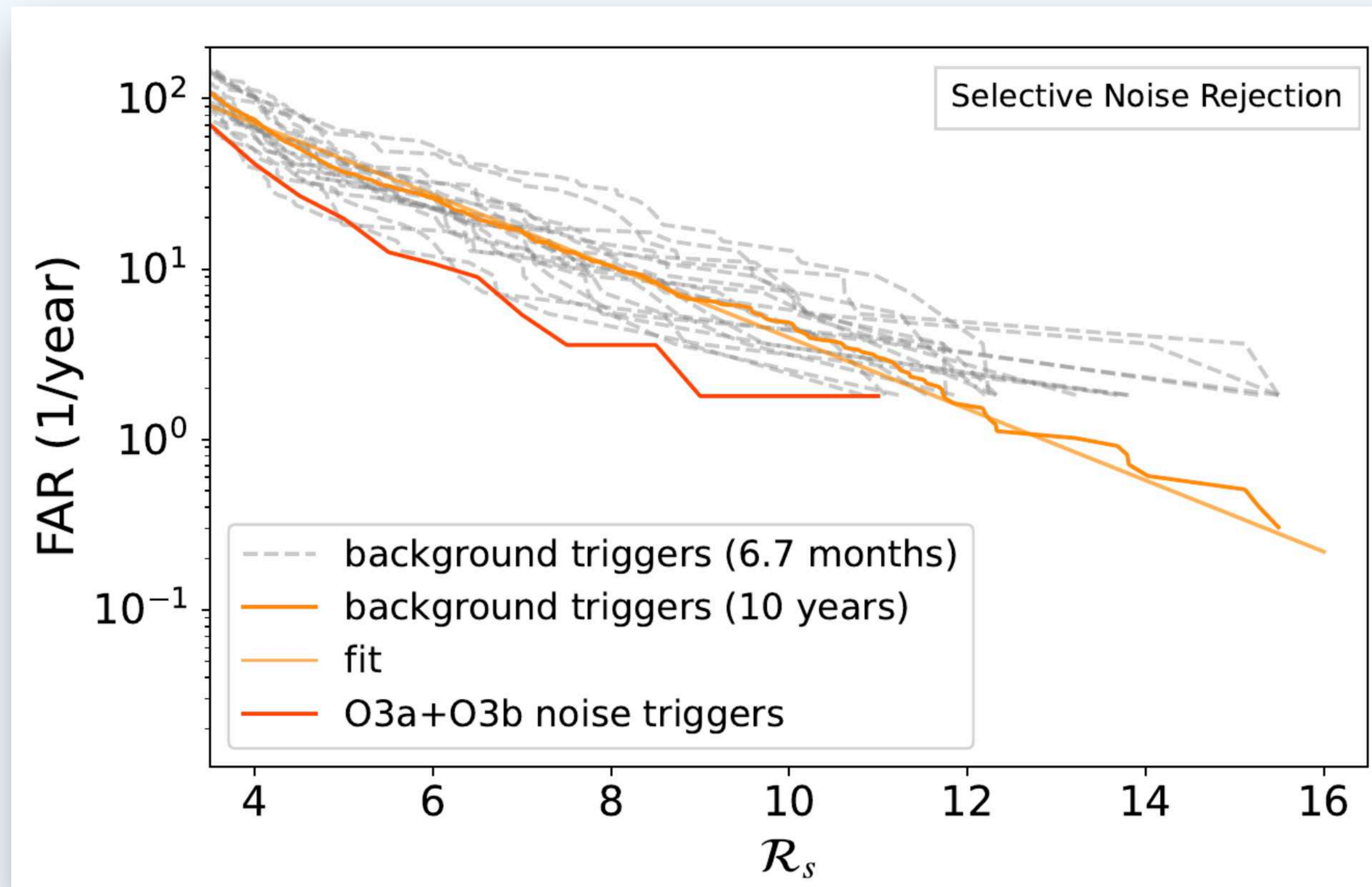


RANKING STATISTIC DISTRIBUTION



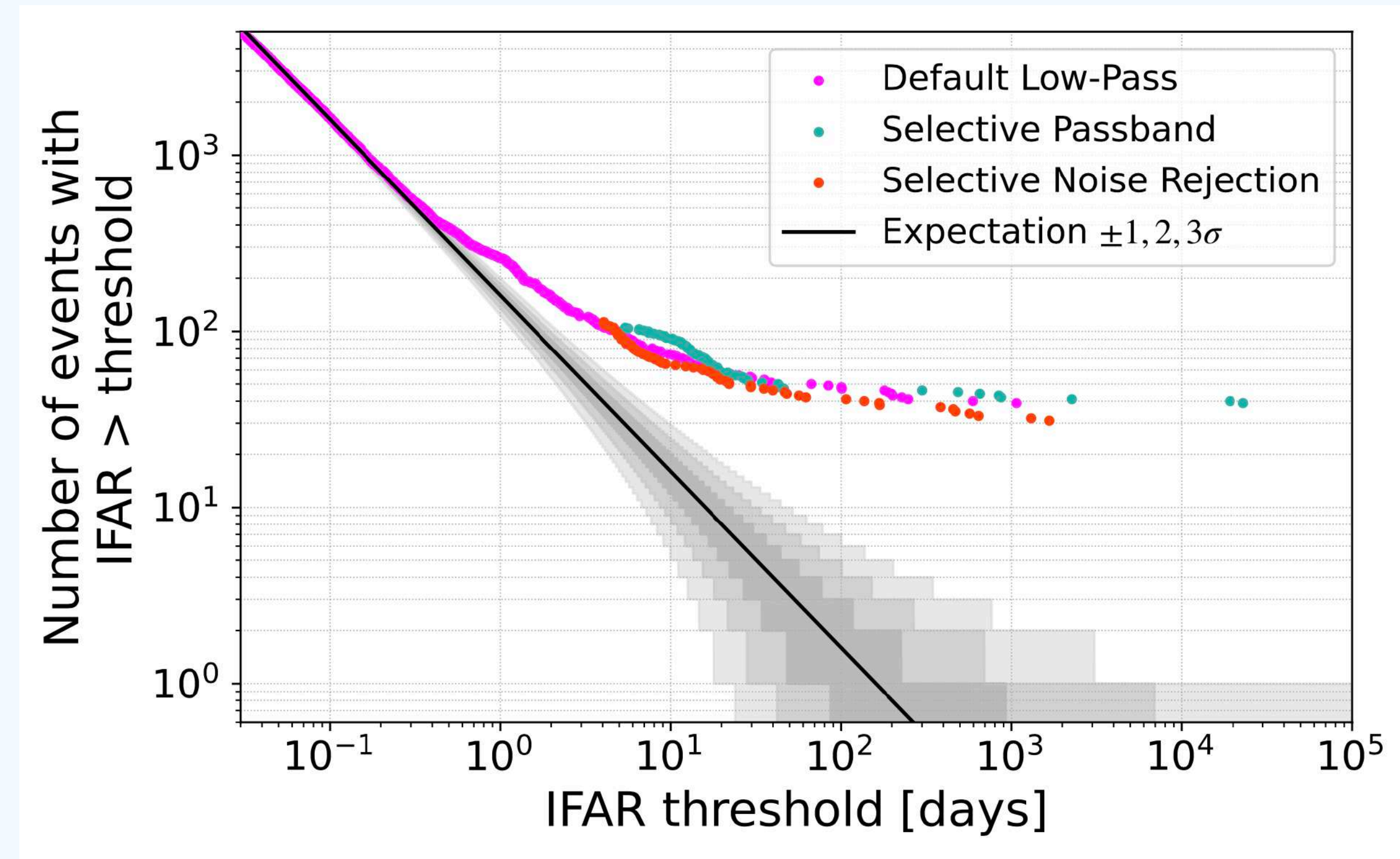
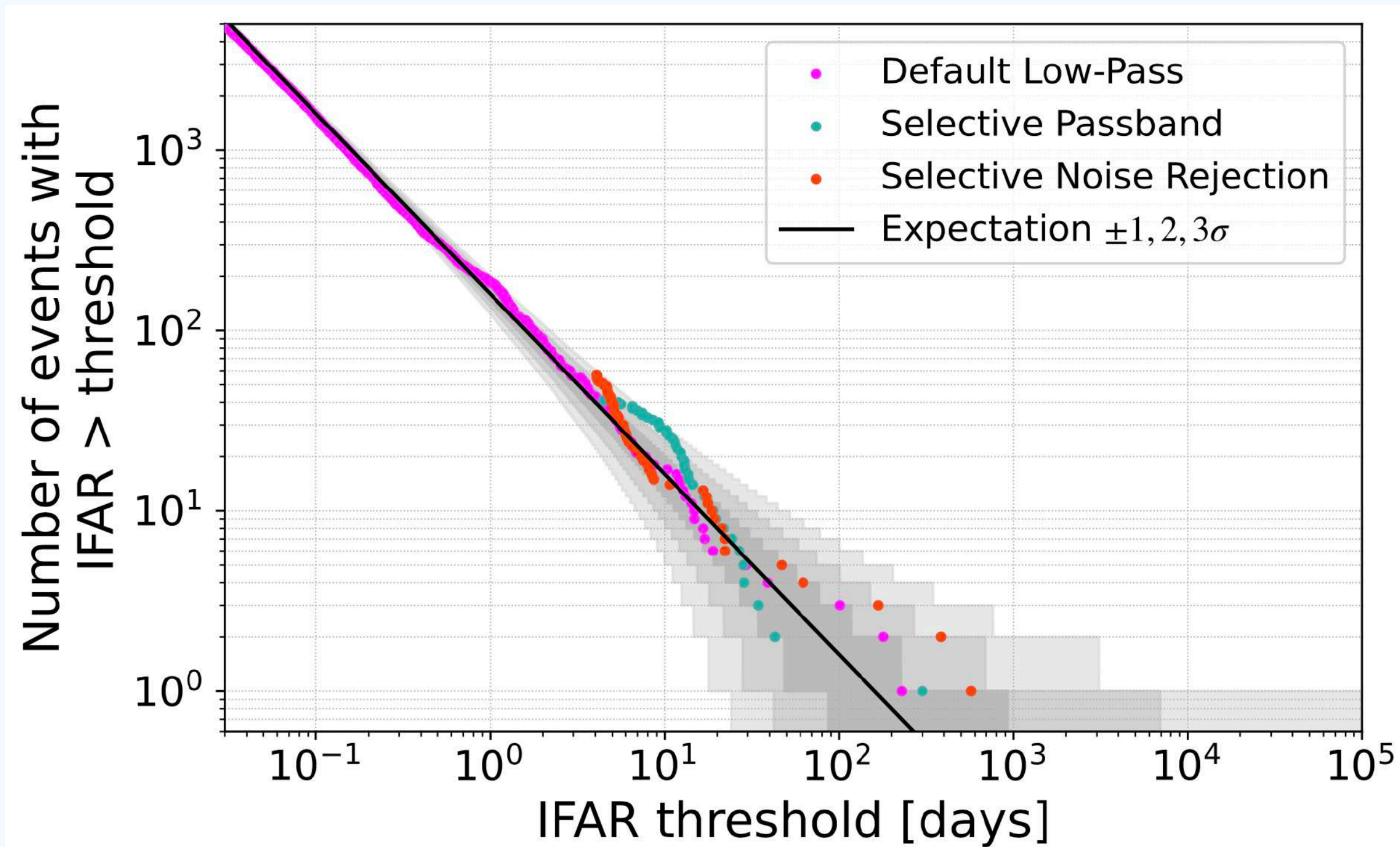
FALSE-ALARM RATE

FAR: We construct a 10-year background using time-slides of O3 noise

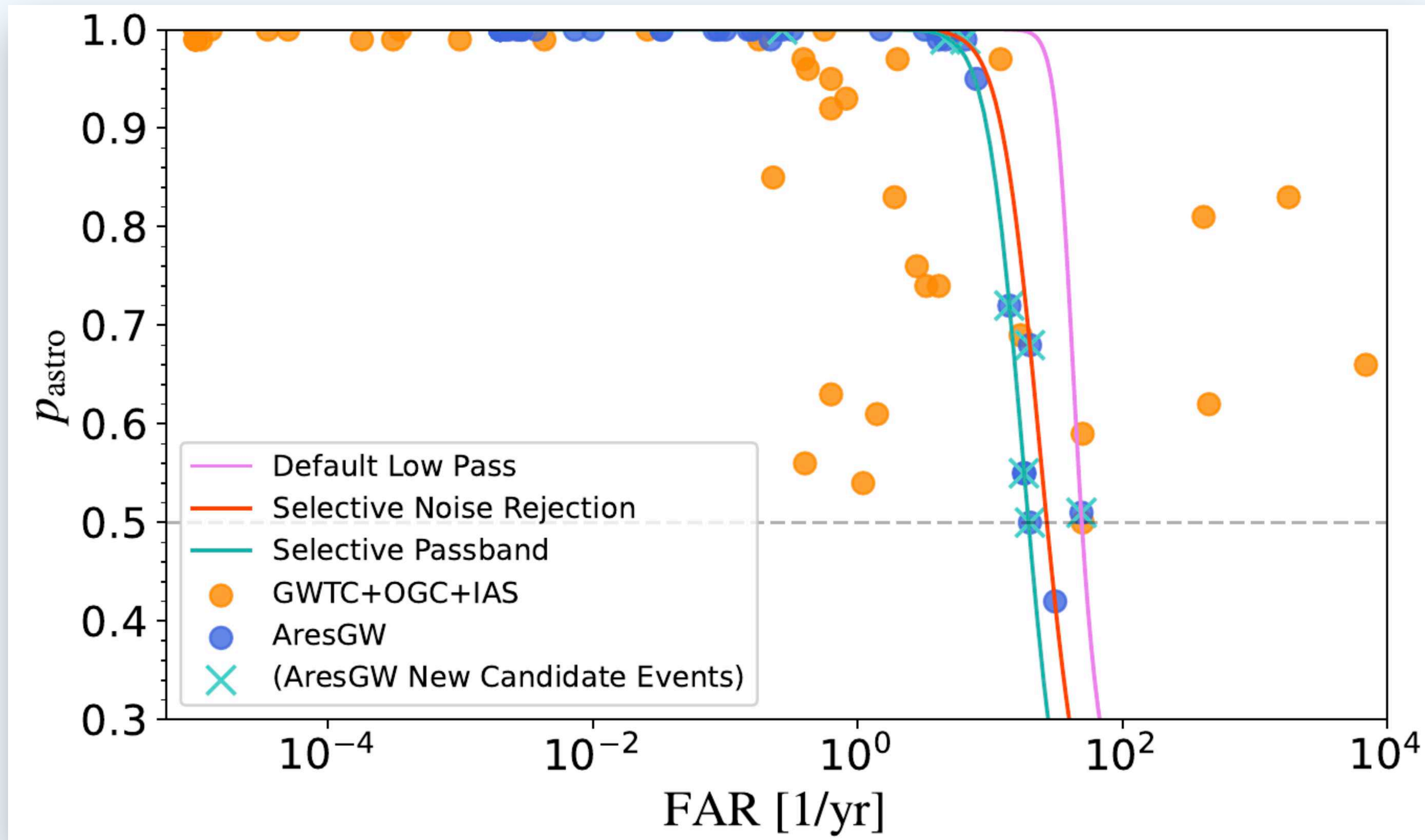


O3 STATISTICS

AresGW performance on O3 data



ASTROPHYSICAL PROBABILITY



PARAMETERS OF NEW GW DETECTIONS WITH AresGW

TABLE VIII: Parameter estimation for the new AresGW candidate events.

#	Event Name	$\mathcal{M}$ ($M_{\odot}$)	q	m_1 ($M_{\odot}$)	m_2 ($M_{\odot}$)	D_L (Mpc)	χ_{eff}	SNR (H1)	SNR (L1)	SNR $\hat{\rho}$ (network)
1	GW190511_125545	$28.95^{+9.45}_{-6.86}$	$0.72^{+0.25}_{-0.36}$	$40.7^{+16.2}_{-10.5}$	$28.2^{+11.6}_{-11.2}$	3707^{+3471}_{-2173}	$0.23^{+0.25}_{-0.29}$	2.29	7.34	7.29
2	GW190614_134749	$25.97^{+16.59}_{-6.20}$	$0.70^{+0.27}_{-0.36}$	$37.0^{+31.8}_{-10.7}$	$25.2^{+15.2}_{-9.7}$	6551^{+9562}_{-3558}	$0.05^{+0.34}_{-0.34}$	3.51	6.08	7.02
3	GW190607_083827	$30.48^{+7.21}_{-4.68}$	$0.78^{+0.19}_{-0.29}$	$40.5^{+12.0}_{-7.6}$	$31.0^{+9.1}_{-8.2}$	4928^{+2725}_{-2435}	$0.01^{+0.26}_{-0.30}$	4.04	7.29	8.33
4	GW190904_104631	$21.24^{+5.76}_{-4.40}$	$0.64^{+0.31}_{-0.33}$	$31.3^{+14.5}_{-8.5}$	$19.7^{+7.1}_{-7.2}$	5614^{+4441}_{-2864}	$0.05^{+0.30}_{-0.37}$	4.50	4.88	6.64
5	GW190523_085933	$23.82^{+10.24}_{-7.95}$	$0.49^{+0.45}_{-0.32}$	$41.7^{+19.3}_{-15.5}$	$19.4^{+14.6}_{-10.5}$	6091^{+6613}_{-3702}	$0.42^{+0.31}_{-0.45}$	3.48	5.14	6.02
6	GW200208_211609	$18.83^{+4.68}_{-3.18}$	$0.69^{+0.28}_{-0.40}$	$26.9^{+14.6}_{-6.3}$	$18.0^{+6.4}_{-6.9}$	3669^{+3413}_{-1985}	$0.01^{+0.37}_{-0.37}$	4.75	6.22	7.83
7	GW190705_164632	$27.21^{+7.34}_{-5.24}$	$0.52^{+0.41}_{-0.32}$	$44.7^{+24.8}_{-12.8}$	$23.0^{+11.7}_{-9.8}$	5692^{+4030}_{-2863}	$0.29^{+0.26}_{-0.34}$	4.42	6.88	8.11
8	GW190426_082124	$17.93^{+4.12}_{-3.42}$	$0.45^{+0.45}_{-0.28}$	$31.5^{+22.5}_{-11.3}$	$13.8^{+6.9}_{-5.2}$	3213^{+4555}_{-1573}	$-0.01^{+0.39}_{-0.50}$	5.15	4.46	6.41

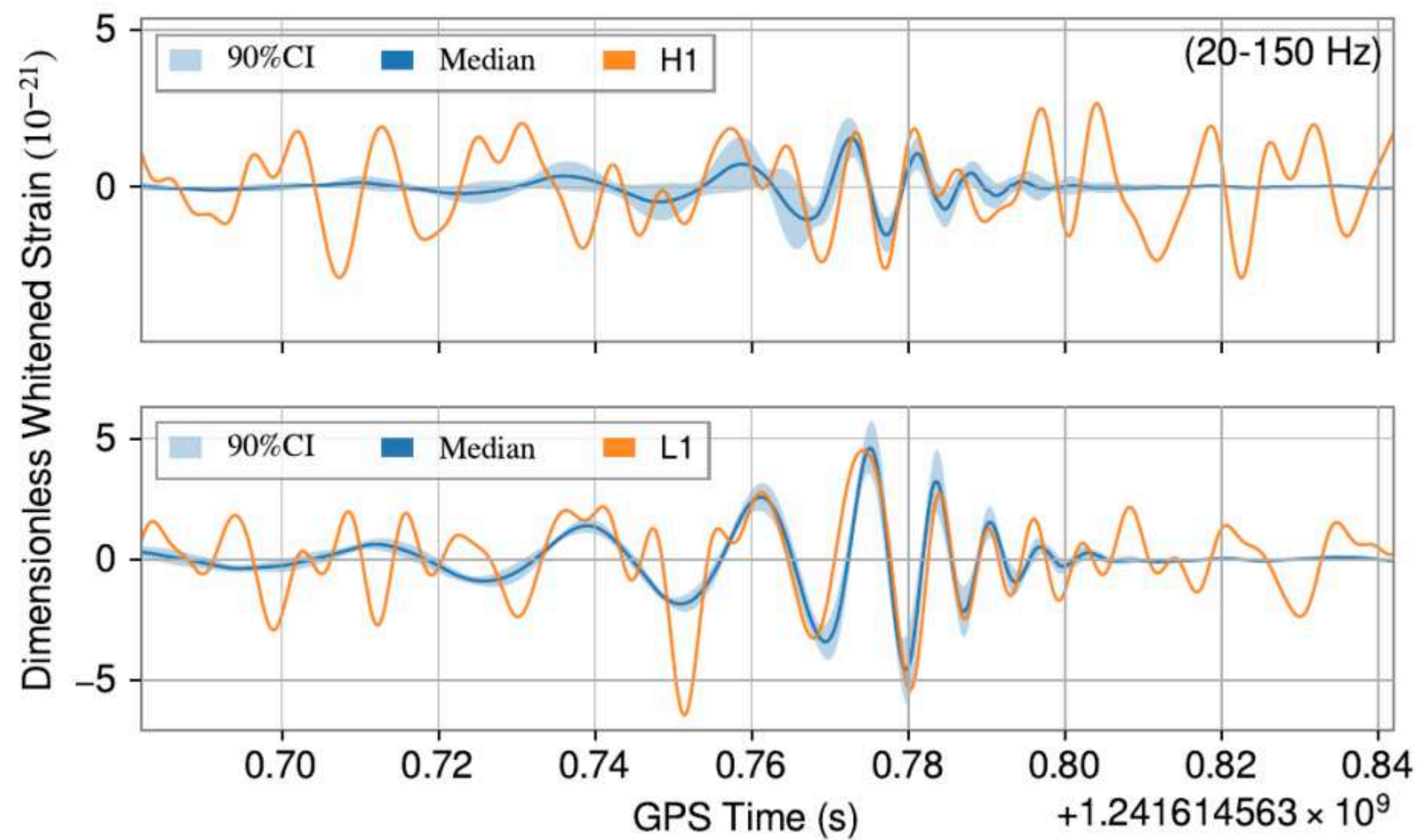


FIG. 35: Whitened, bandpassed strain data and reconstructed waveform for the new event GW190511_125545 identified by AresGW.

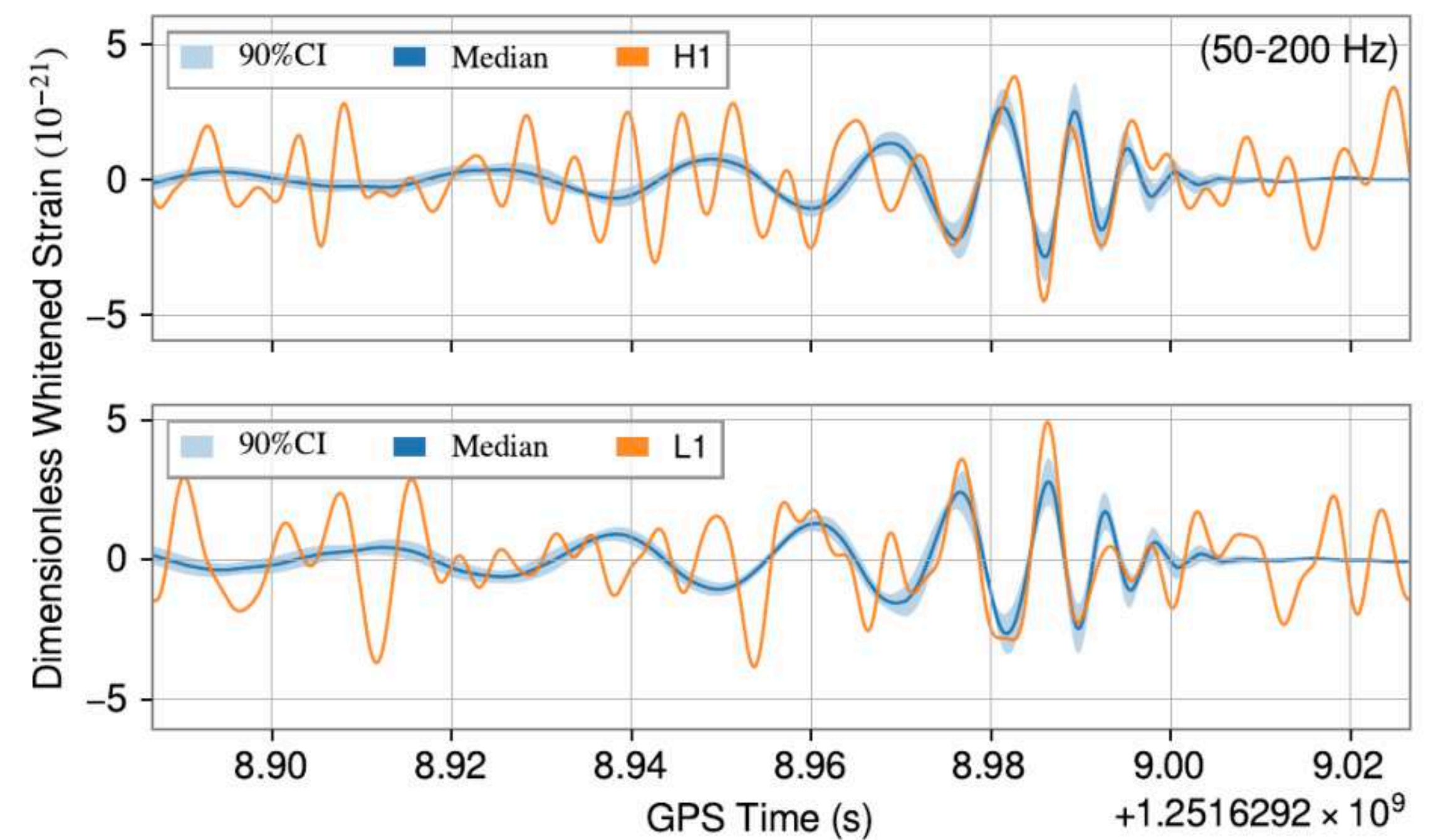


FIG. 38: Same as Fig. 35, but for the new event GW190904_104631.

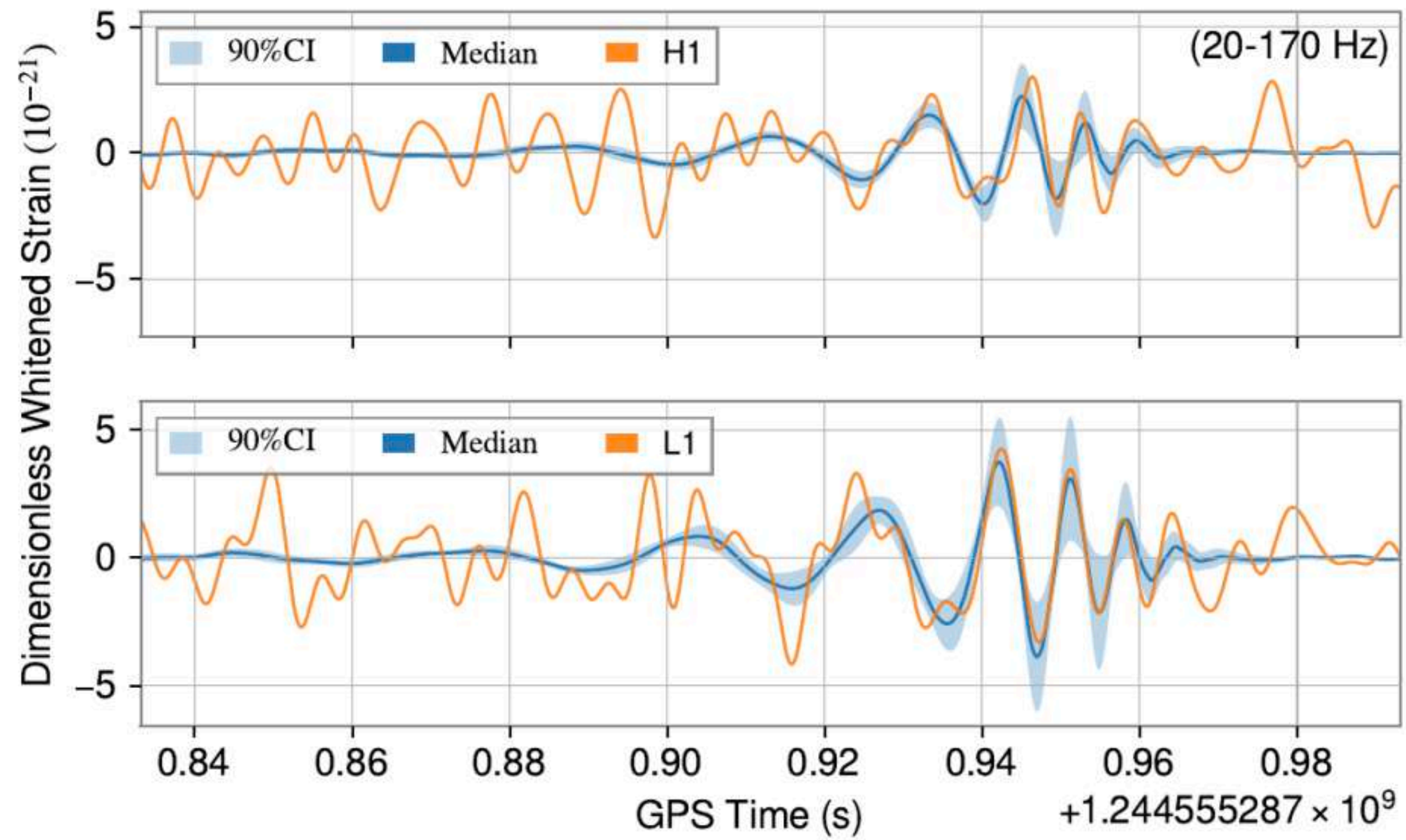


FIG. 36: Same as Fig. 35, but for the new event GW190614_134749.

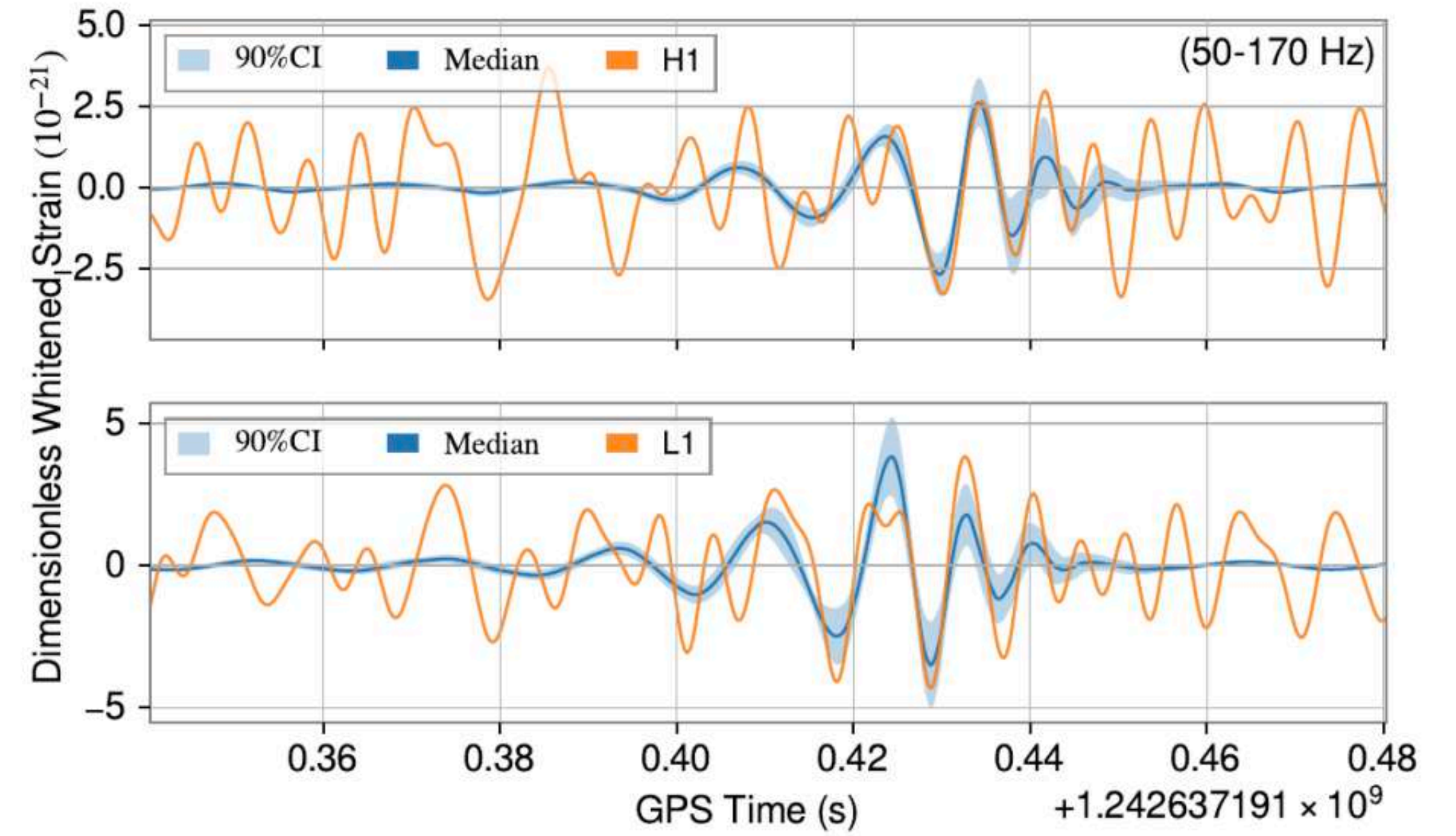


FIG. 39: Same as Fig. 35, but for the new event GW190523_085933.

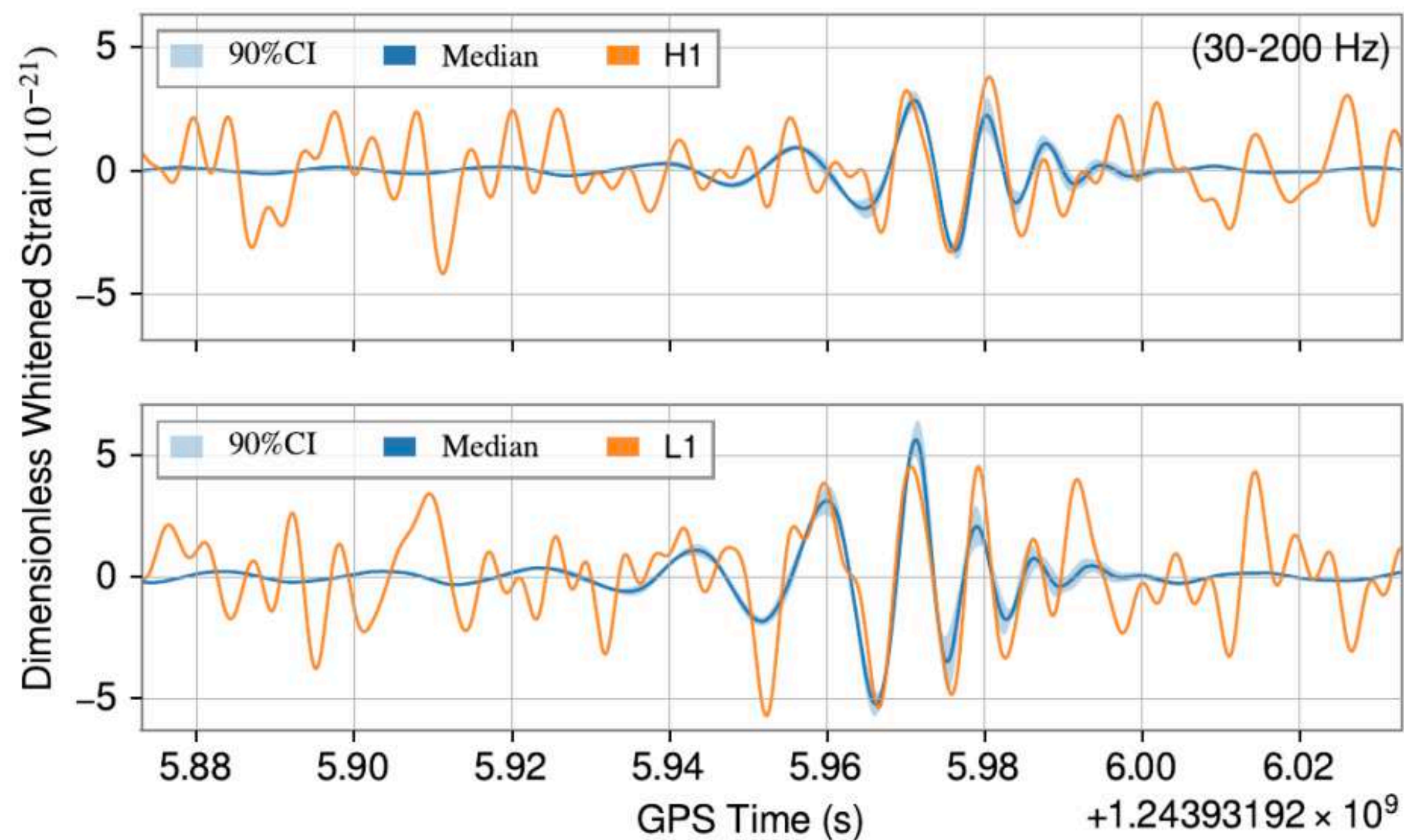


FIG. 37: Same as Fig. 35, but for the new event GW190607_083827.

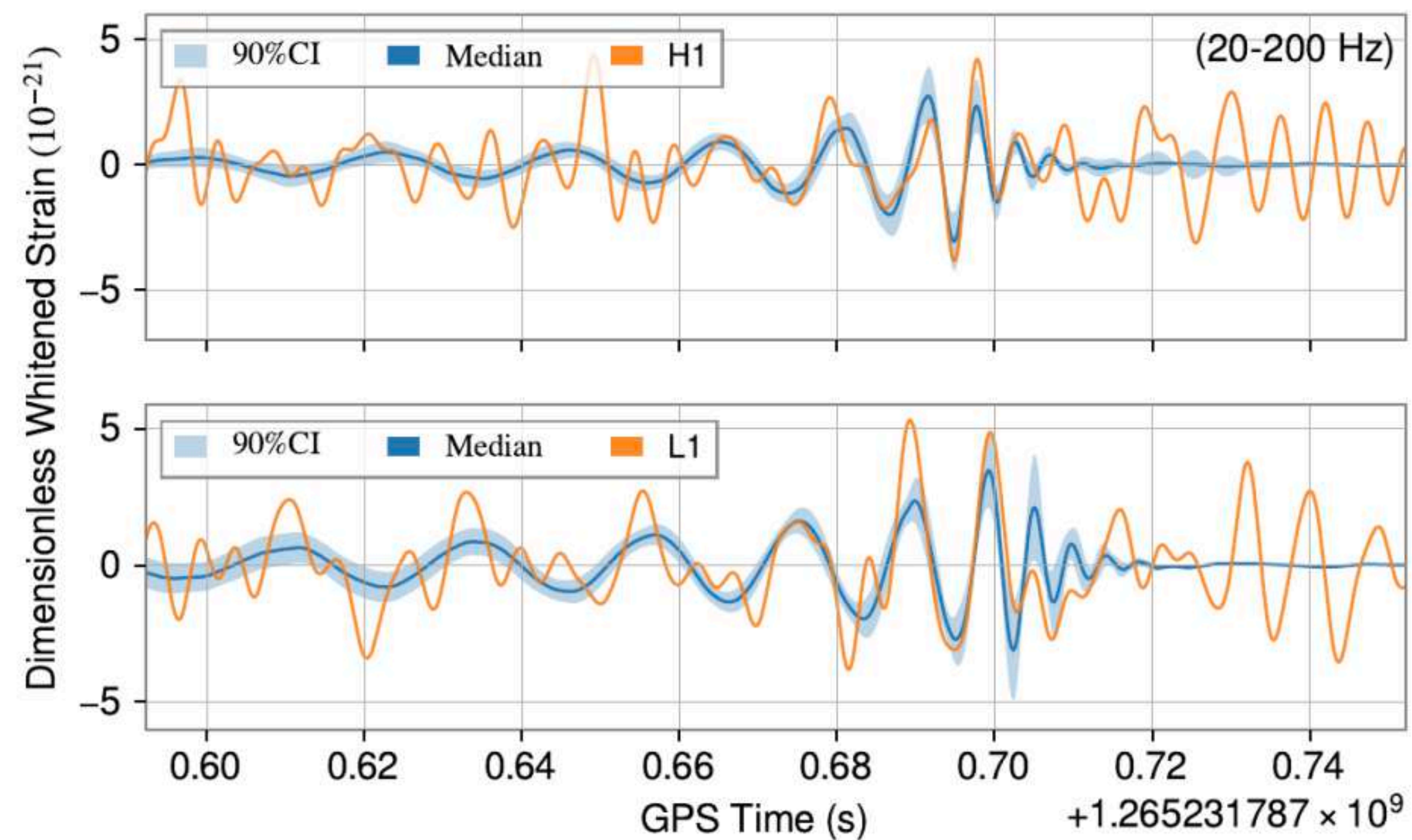


FIG. 40: Same as Fig. 35, but for the new event GW200208_211609.

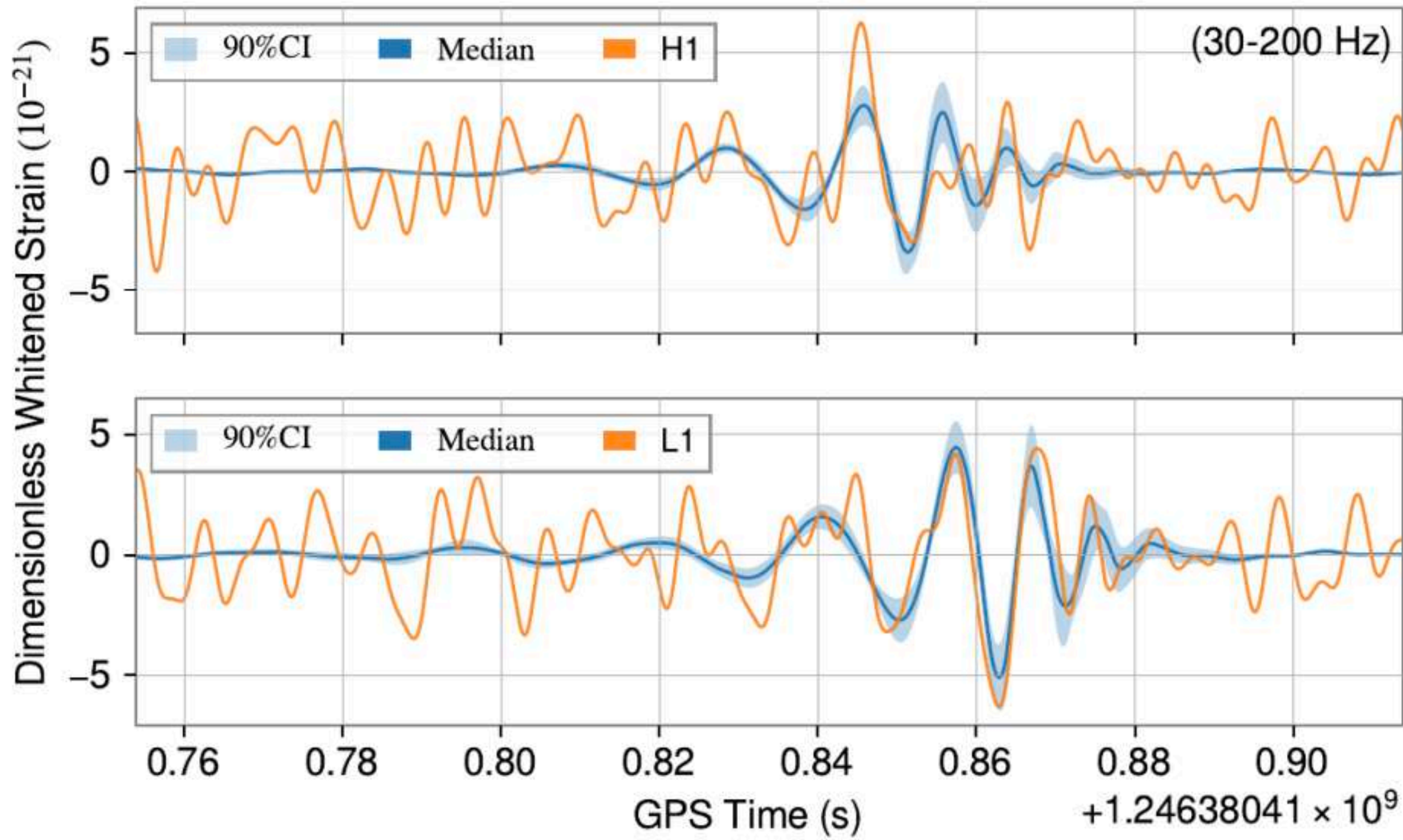


FIG. 41: Same as Fig. 35, but for the new event GW190705_164632.

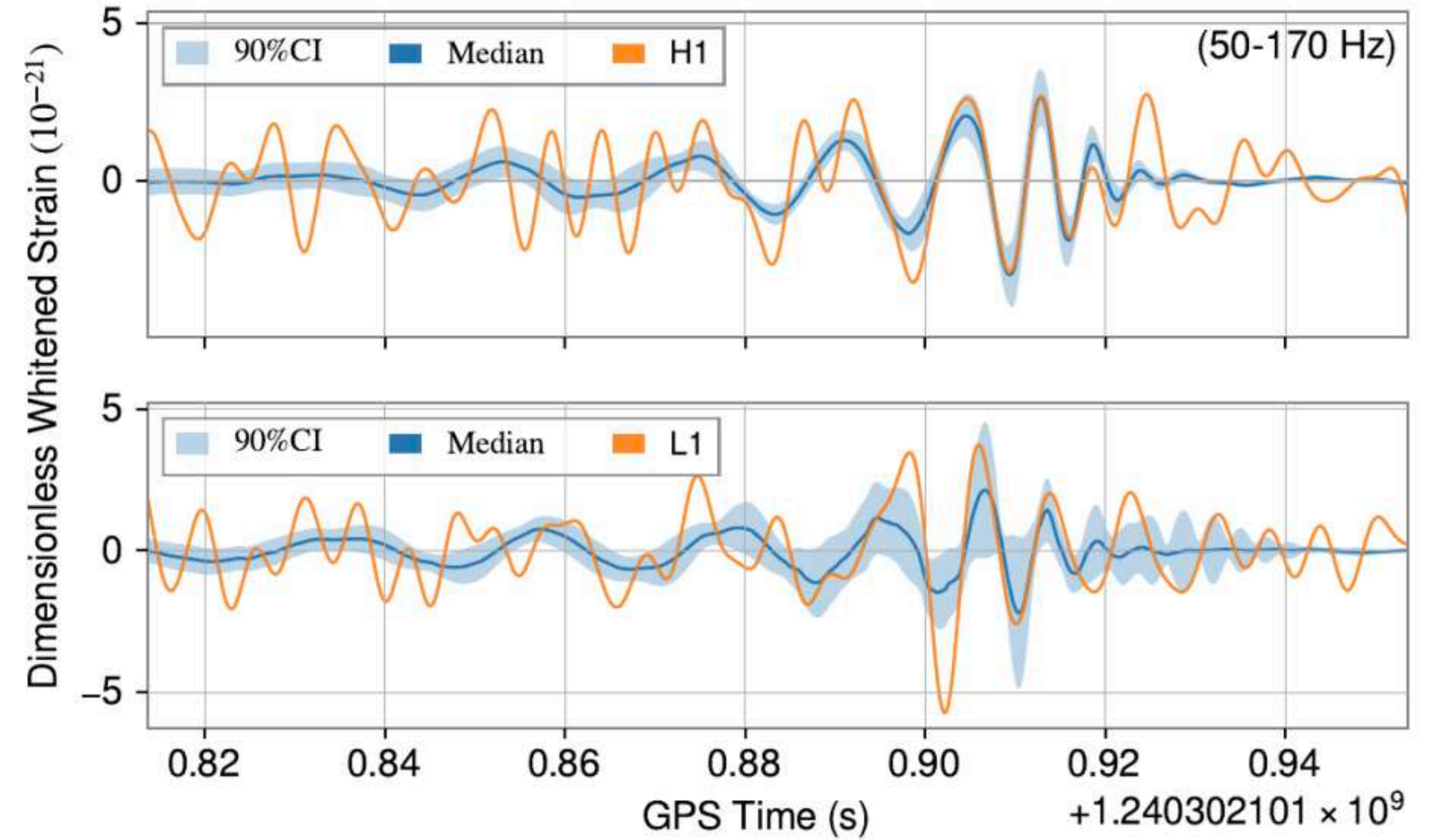
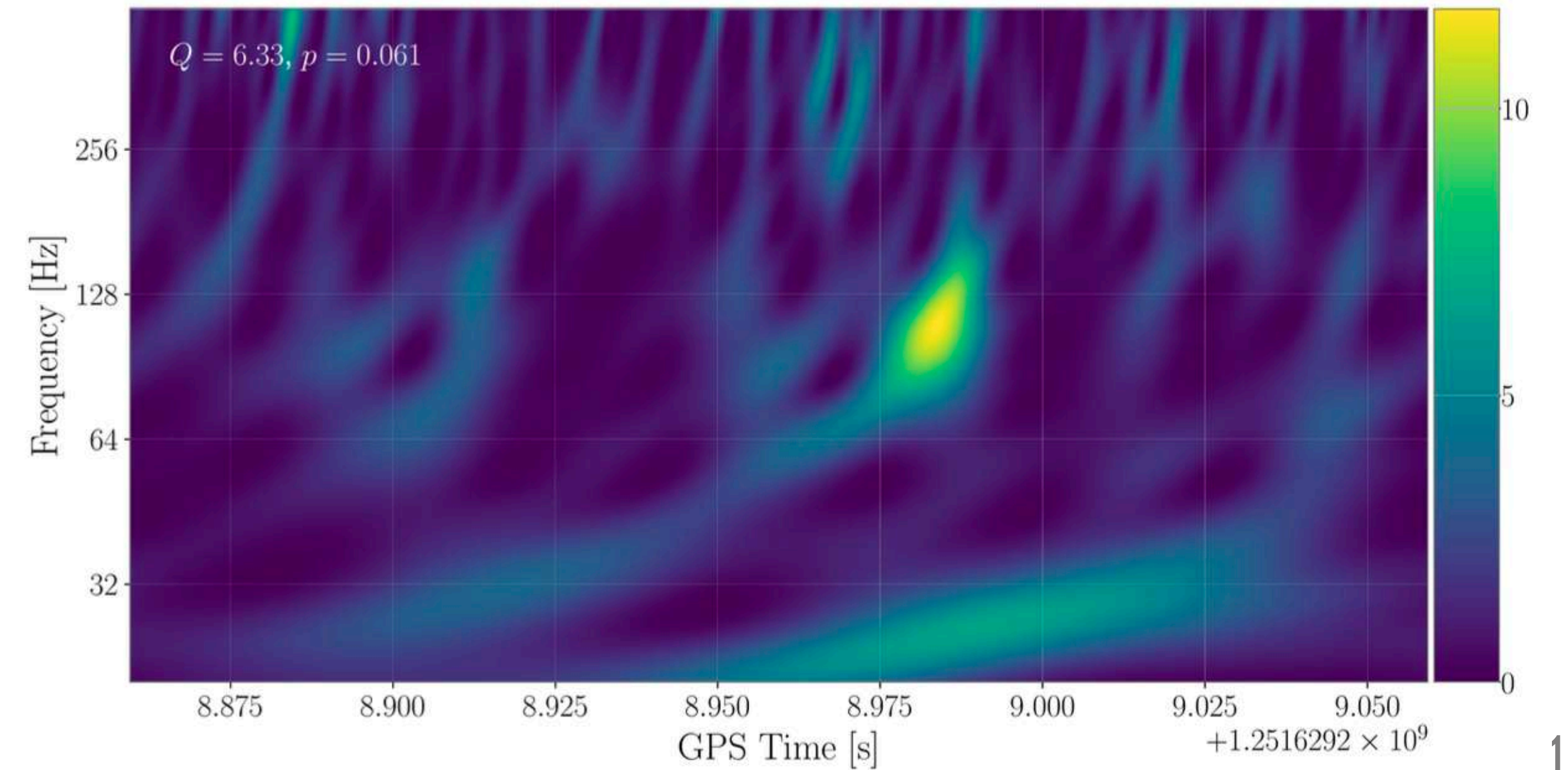
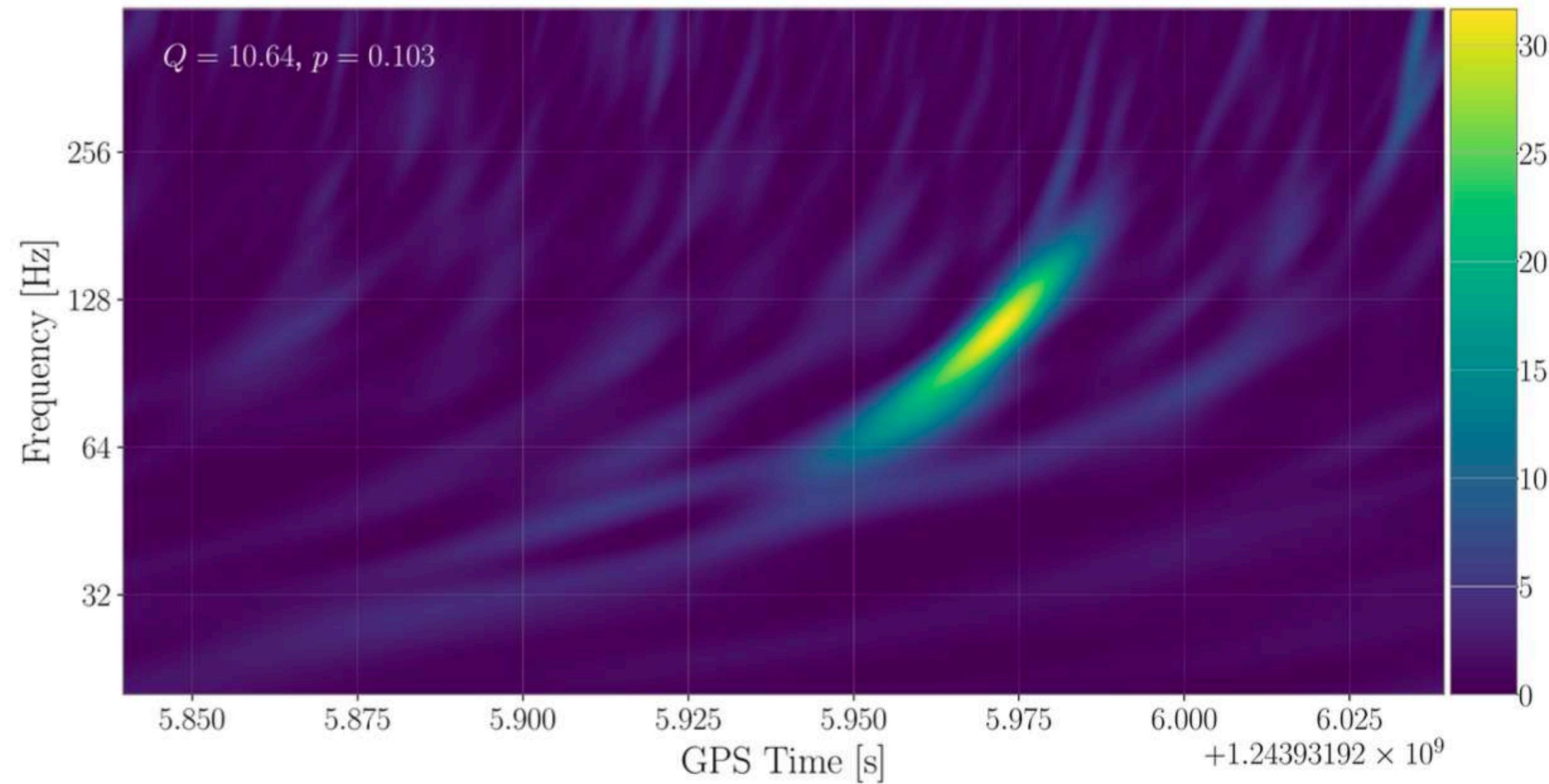
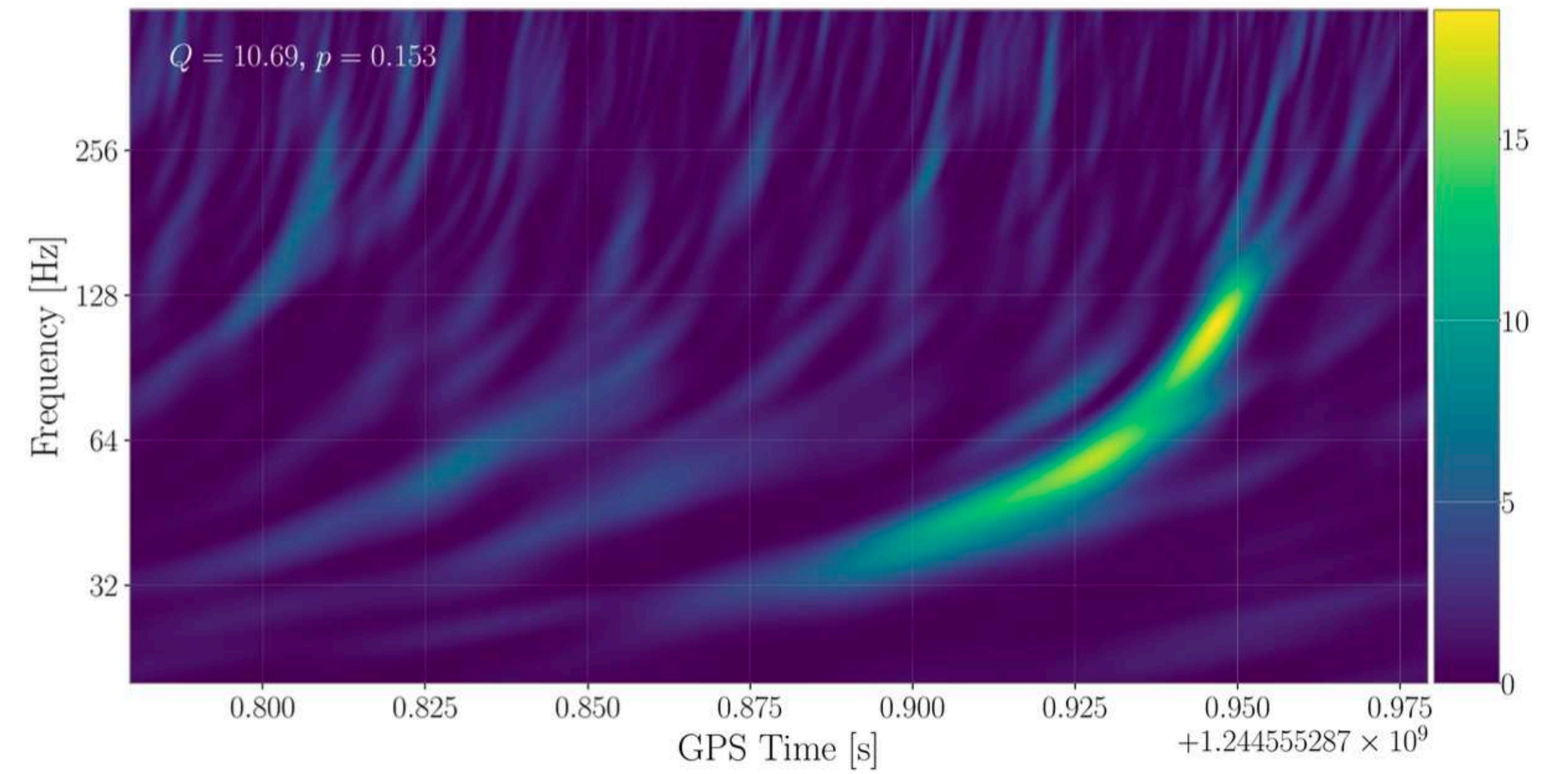
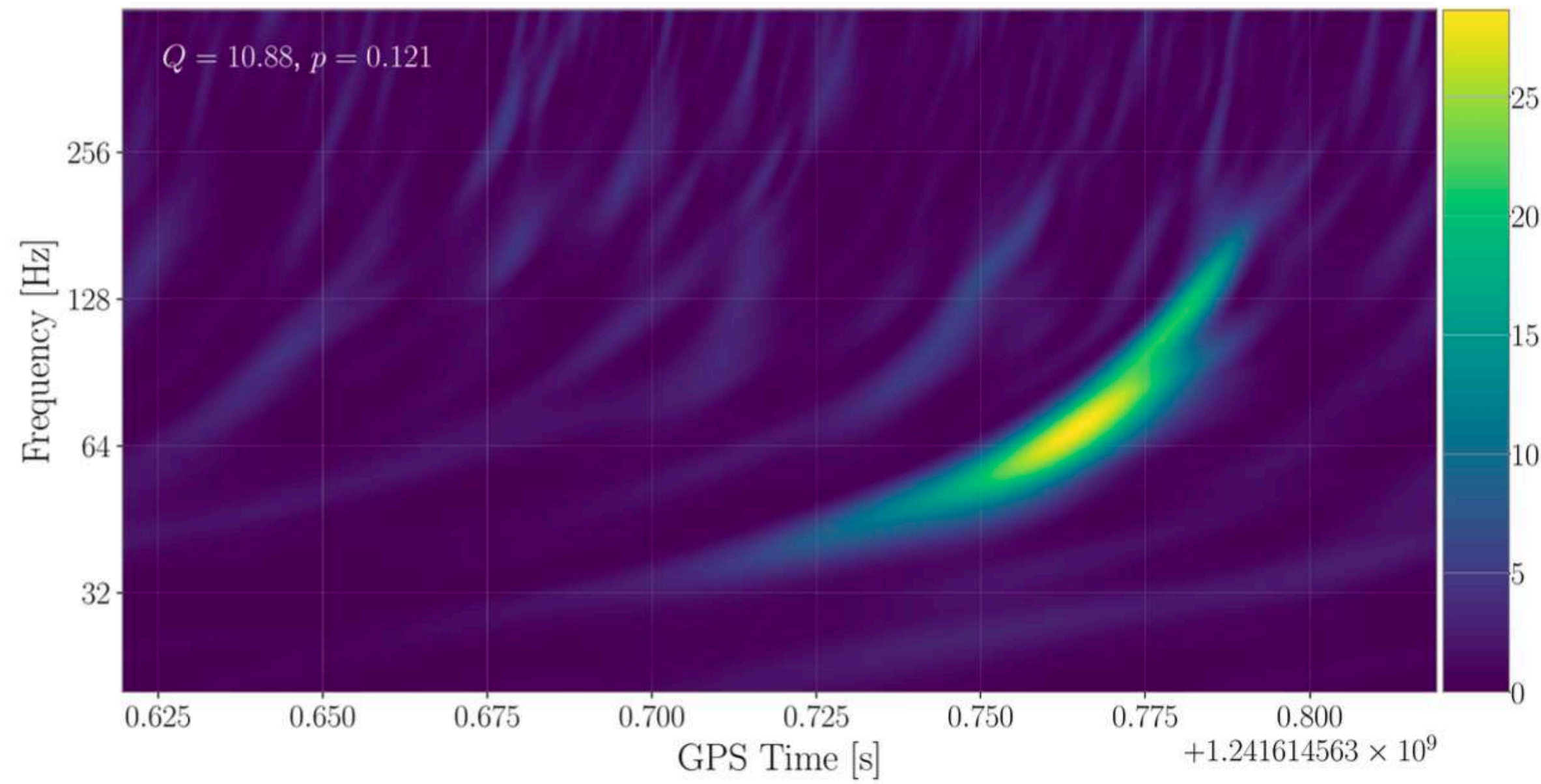
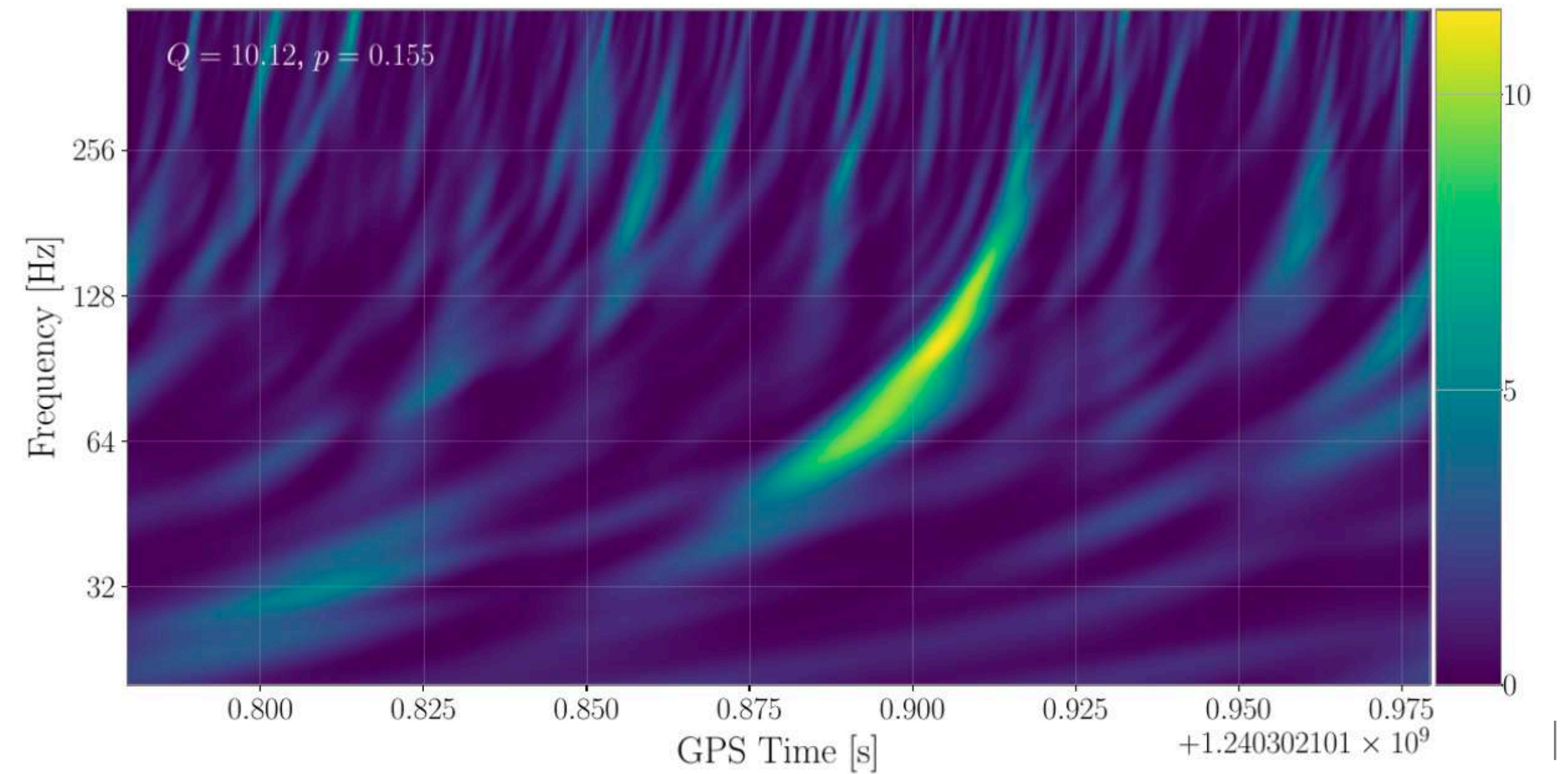
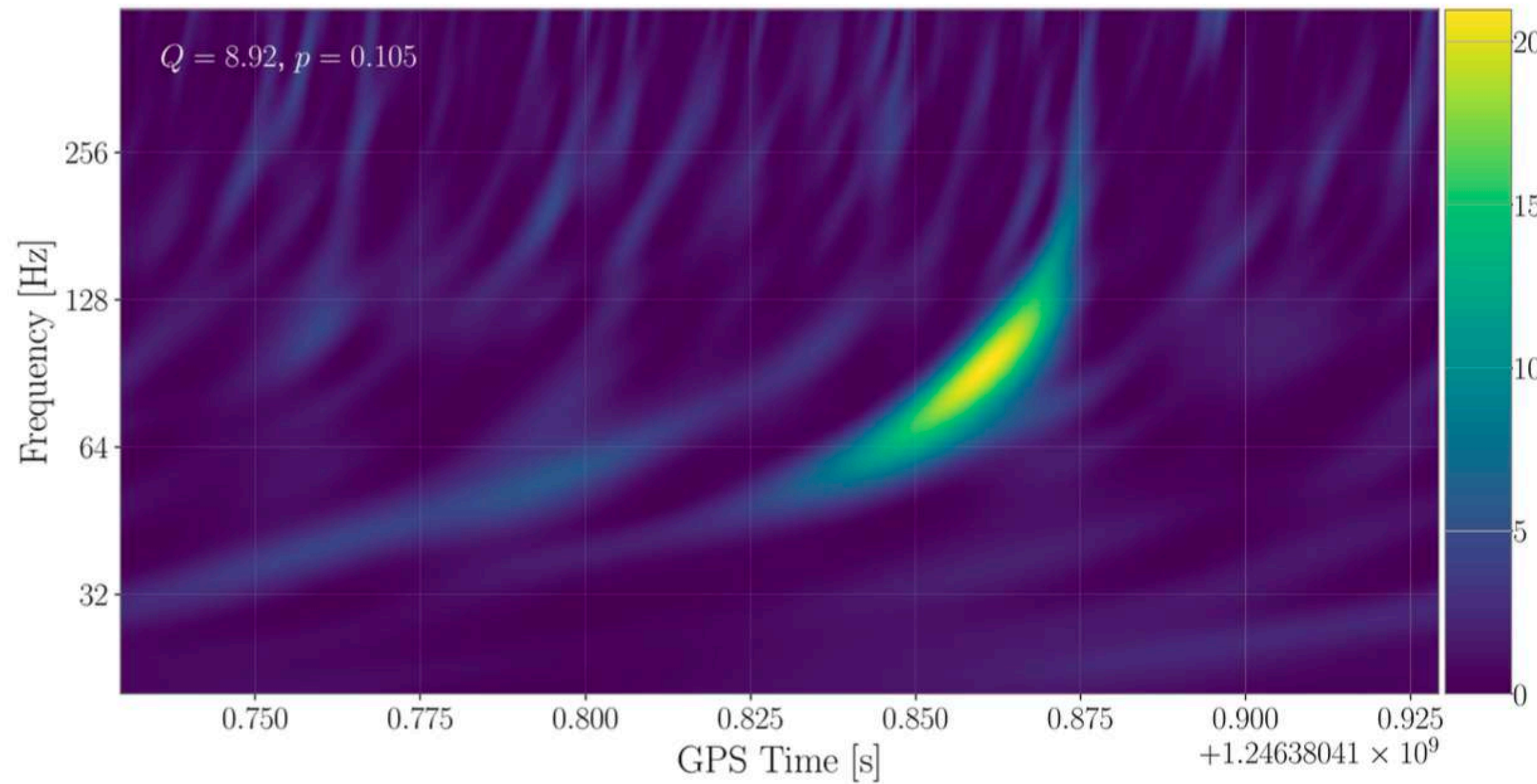
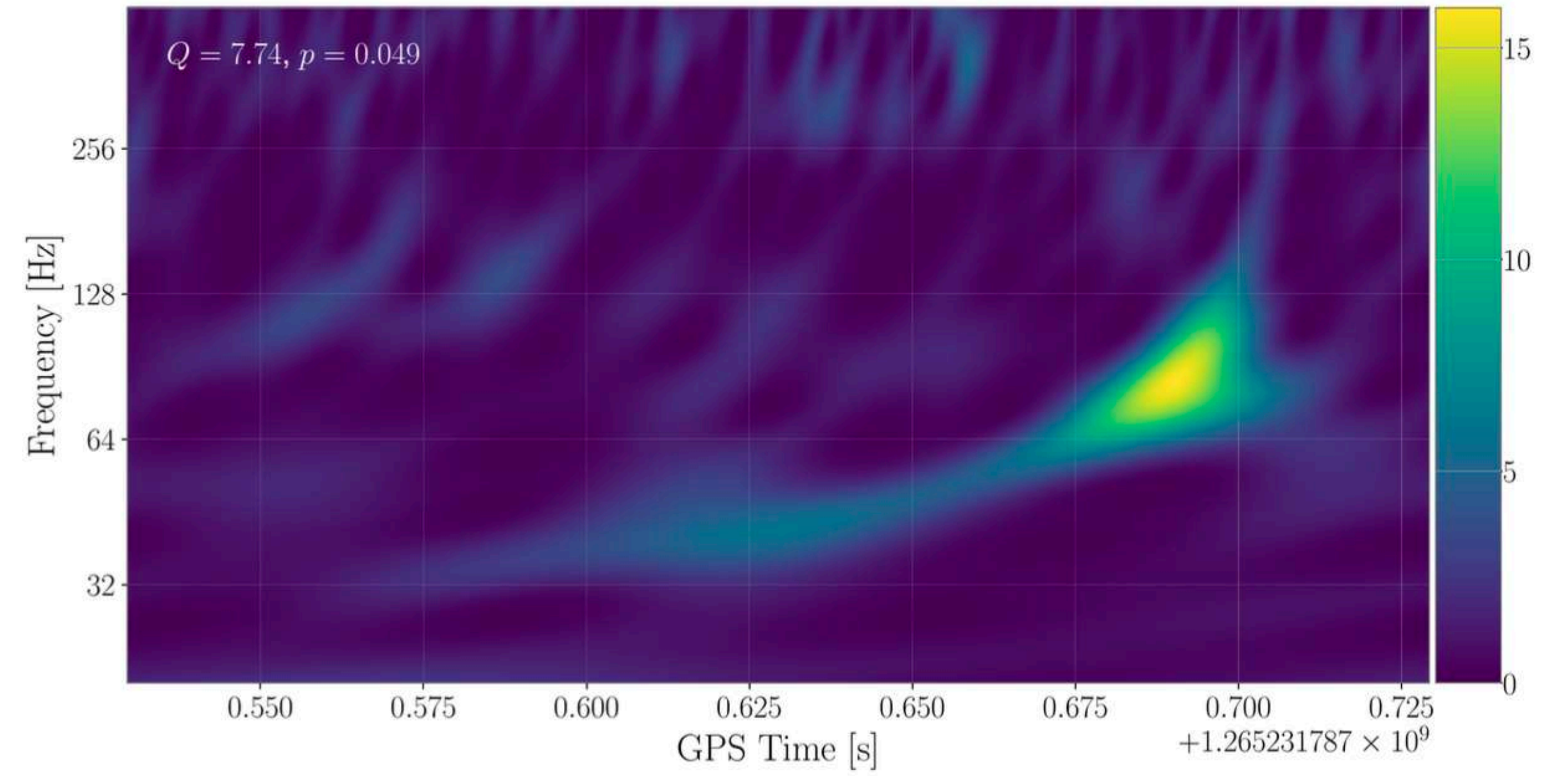
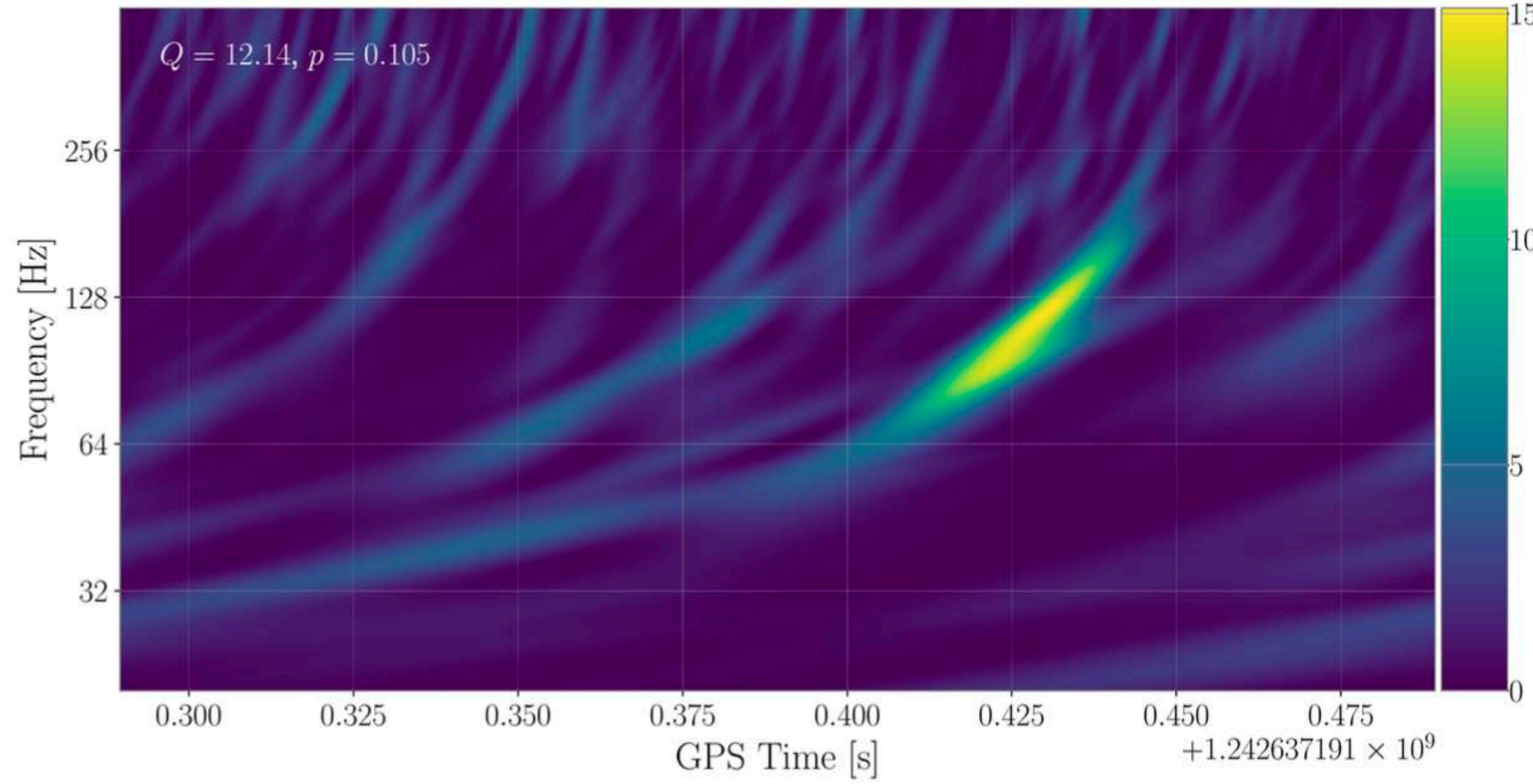


FIG. 42: Same as Fig. 35, but for the new event GW190426_082124.

ARESGW NEW CANDIDATE EVENTS



ARESGW NEW CANDIDATE EVENTS



DATASETS AND PARAMETER SPACE

Dataset 1

- Purely **Gaussian noise** (with aLIGOZeroDetHighPower PSD)
- **no spin**, no higher-order modes
- 10-50 Msun component masses (uniformly)

Dataset 2

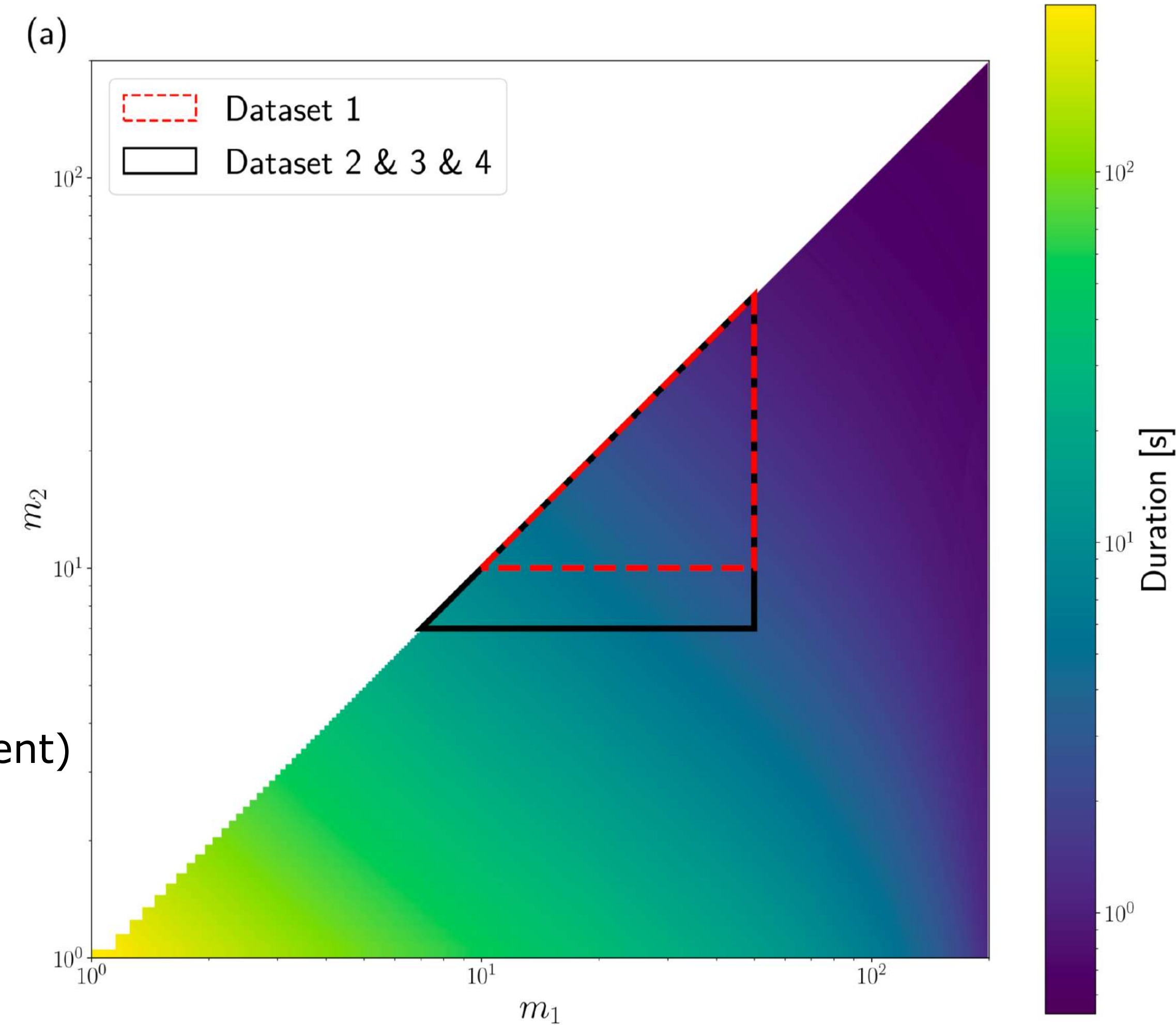
- **Gaussian noise** (but with O3a PSD)
- **aligned spin** (-0.99,0.99), no higher-order modes
- 7-50 Msun (uniformly)

Dataset 3

- **Gaussian noise** (but with O3a PSD, random for each 2h segment)
- **non-aligned spin** (with isotropic distribution in magnitude)
- higher-order modes up to (4,-4) as in IMRPhenomXPHM
- 7-50 Msun (uniformly)

Dataset 4

- as dataset 3, but with real noise sampled from O3a parts (excl. any GWTC-2 detections)



Evaluation

Evaluation:

1. Each algorithm is evaluated on the background dataset and returns a ranking statistic for each (false) positive event.
2. FAR at given ranking statistic $R = (\# \text{ of background events with ranking statistic} > R) / \text{duration } T$

$$\text{FAR}(\mathcal{R}) = \frac{N_{\text{FP},\mathcal{R}}}{T}$$

1. For uniform (*in volume*) injections up to a distance d_{max} , the sensitive volume is approximately

$$V(\text{FAR}) \approx V(d_{\text{max}}) \frac{N_{I,\text{FAR}}}{N_I}$$

where $N_{I,\text{FAR}}$ = found injections at given FAR and N_I = total # of found injections (within +/- Δt each).

However, the injections are not uniform in volume, but are sampled over the *chirp distance*, instead:

$$d_c = d \left(\frac{\mathcal{M}_{c,0}}{\mathcal{M}_c} \right)^{5/6}$$

with $\mathcal{M}_{c,0} = 1.4/2^{1/5} M_{\odot}$. To account for that:

$$V(\text{FAR}) \approx \frac{V(d_{\text{max}})}{N_I} \sum_{i=1}^{N_{I,\text{FAR}}} \left(\frac{\mathcal{M}_{c,i}}{\mathcal{M}_{c,\text{max}}} \right)^{5/2}$$